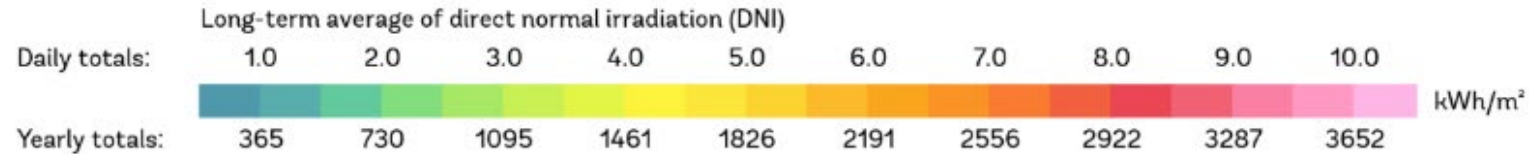
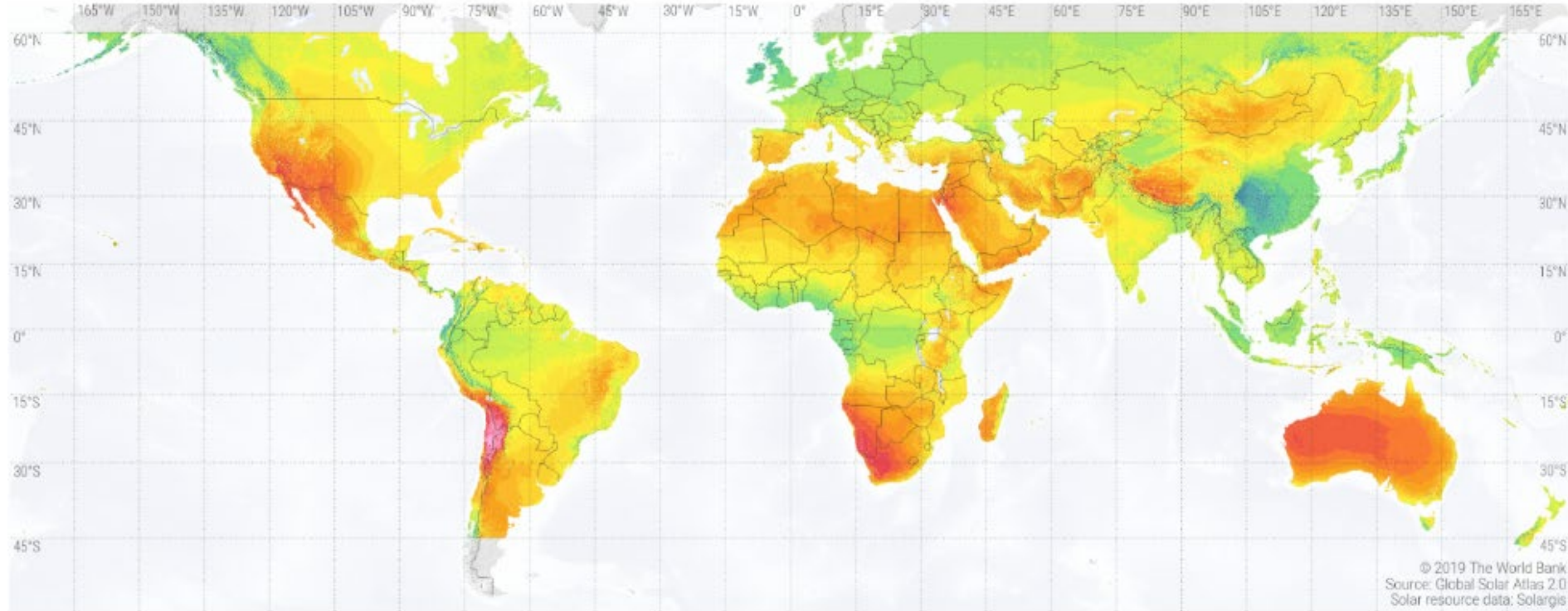


A method to develop centrifugal compressor performance maps for off-design and dynamic simulation studies of sCO₂ cycles



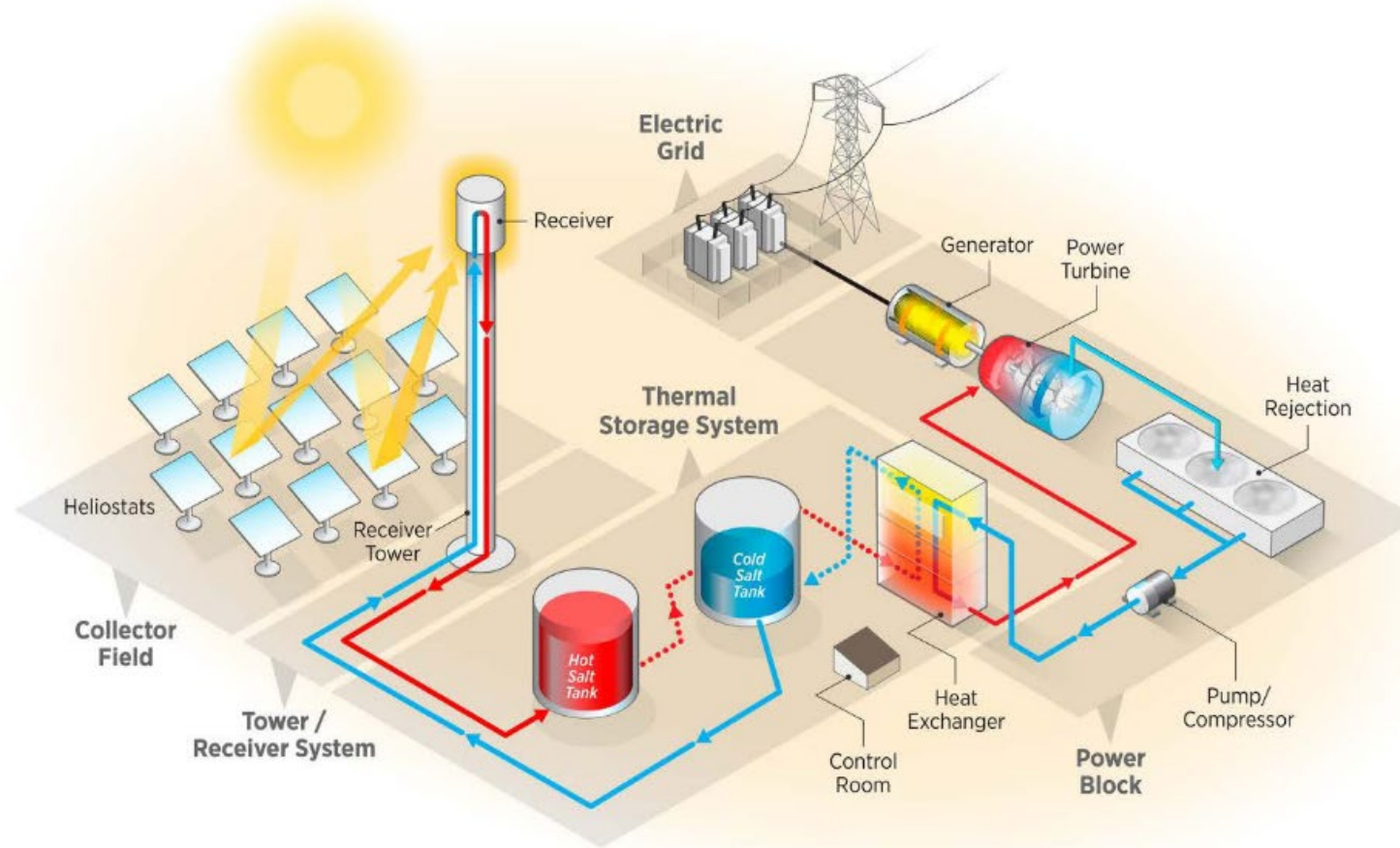
Presented by Colin Francois du Sart (Colin.duSart@uct.ac.za), University of Cape Town
Co-authored by Pieter Rousseau & Ryno Laubscher, Stellenbosch University

SOLAR RESOURCE MAP DIRECT NORMAL IRRADIATION



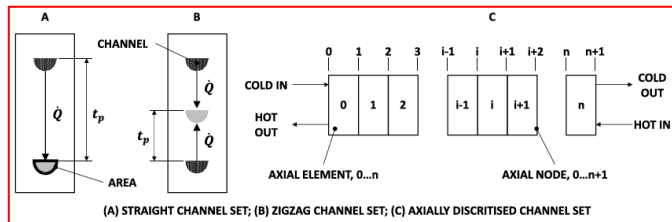
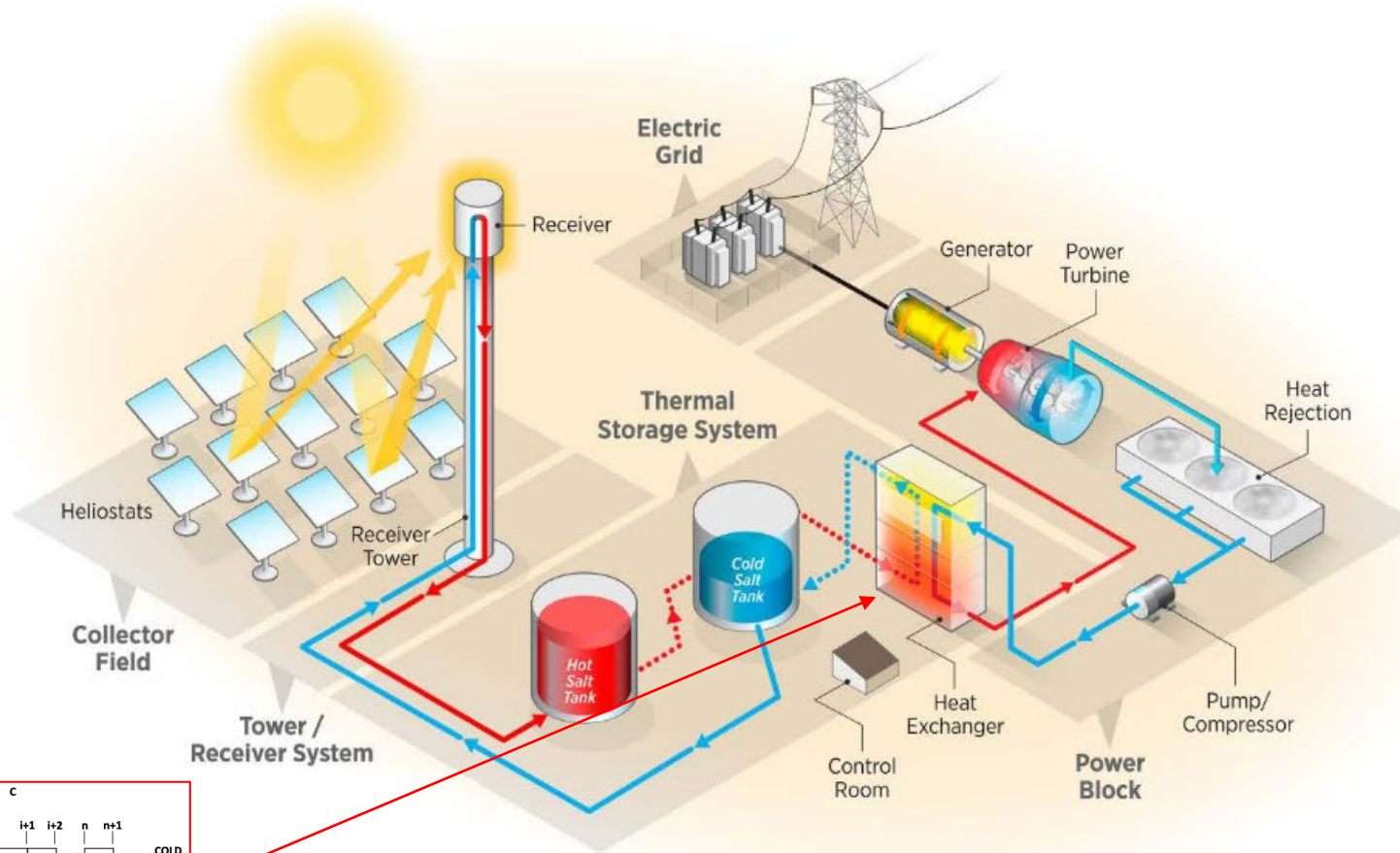
This map is published by the World Bank Group, funded by ESMAP, and prepared by Solargis. For more information and terms of use, please visit <http://globalsolaratlas.info>.

Global direct normal irradiation map, from The World Bank (2019)



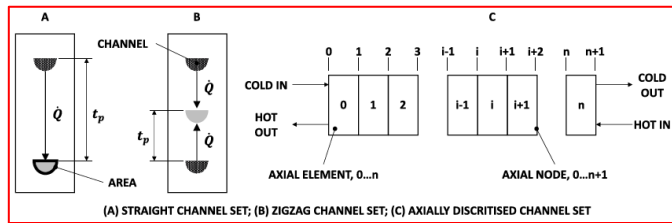
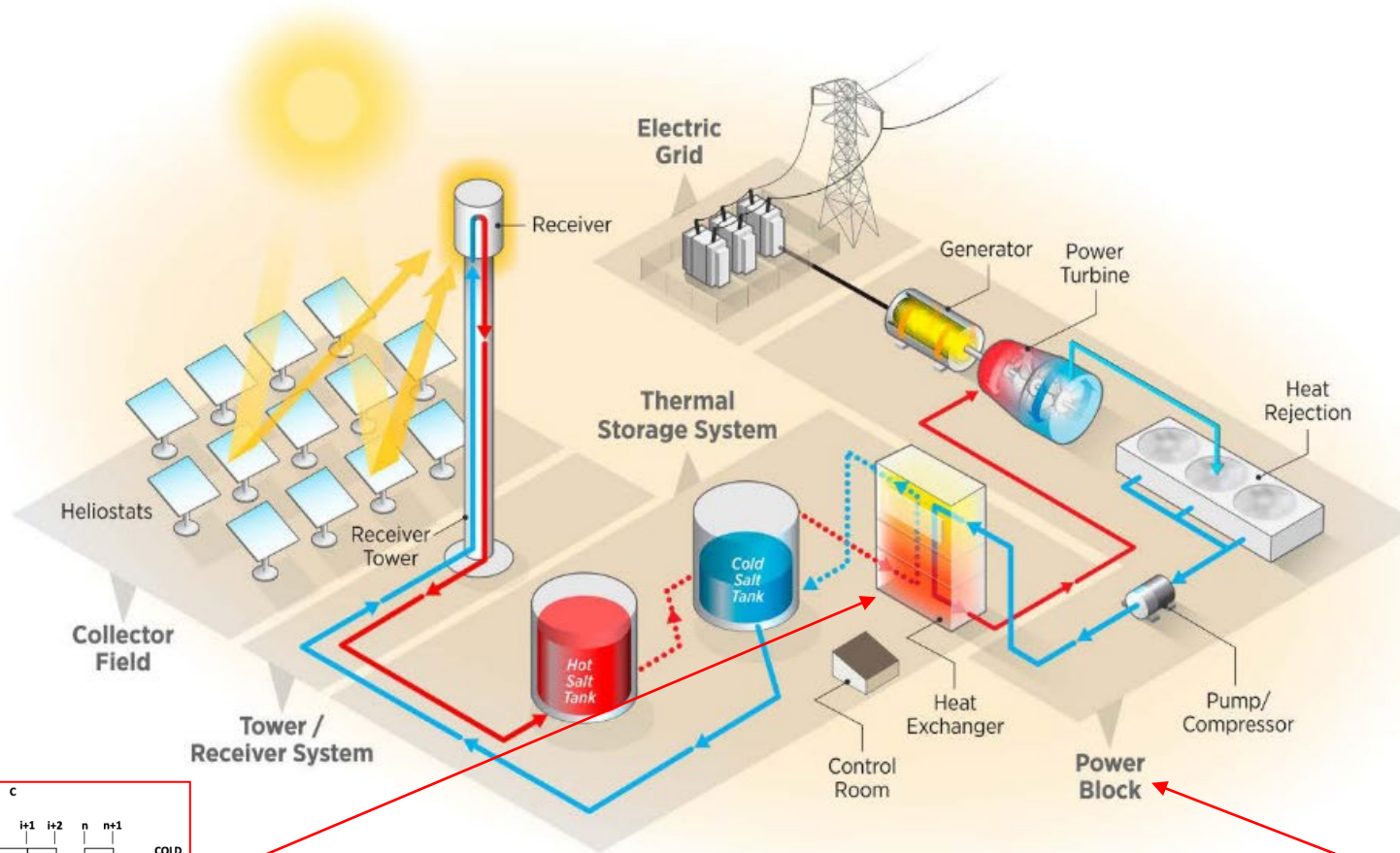
Schematic of a sCO₂-CSP plant with TES, from Mehos et al. (2017)

Introduction

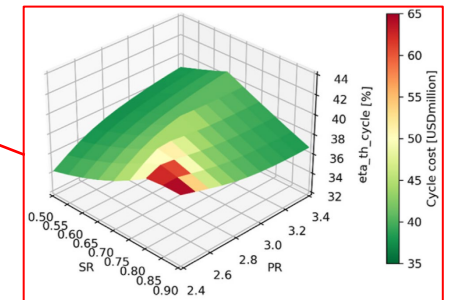


Schematic of a sCO₂-CSP plant with TES, from Mehos et al. (2017)

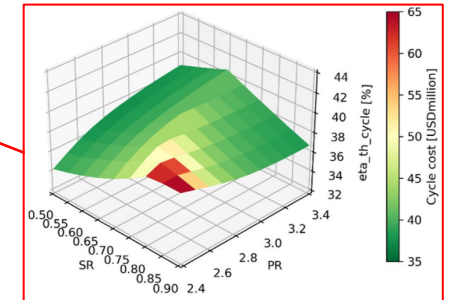
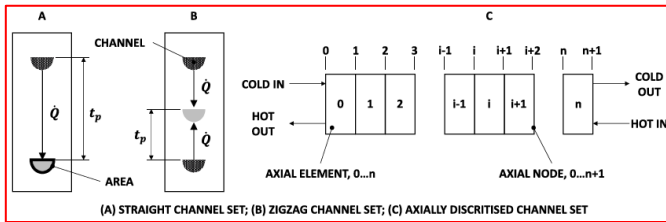
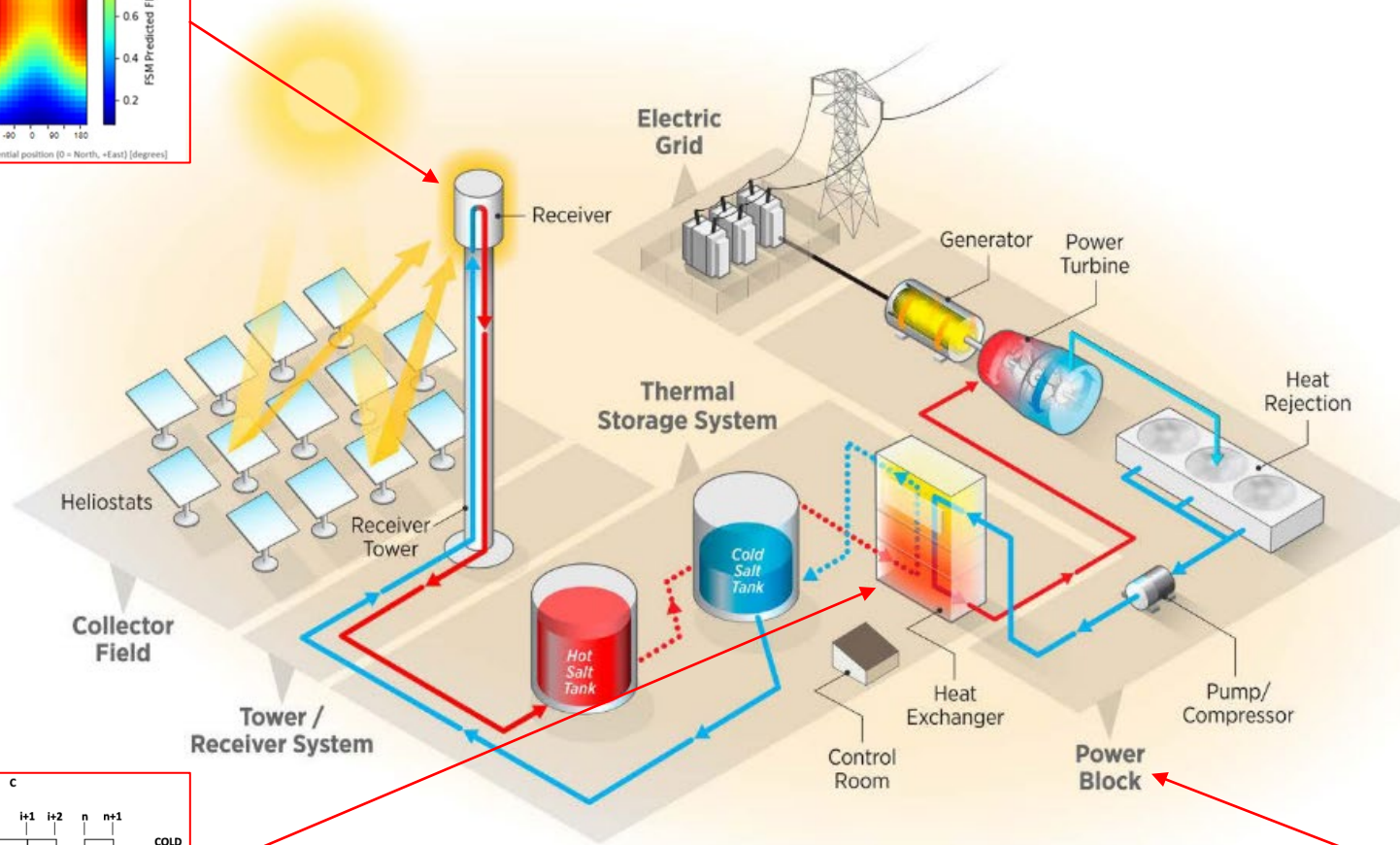
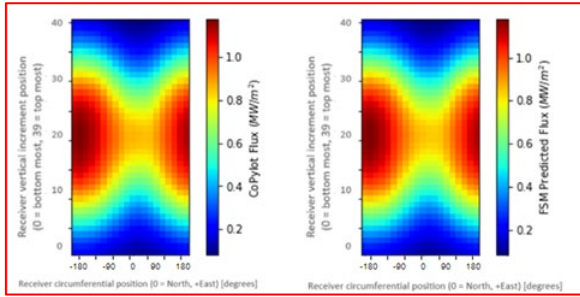
Introduction



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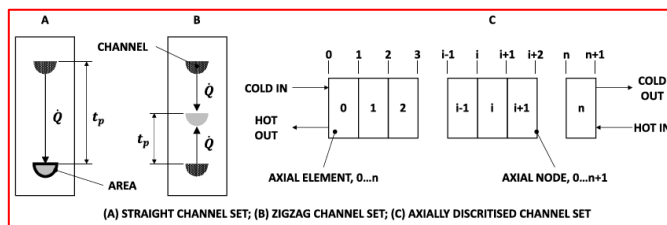
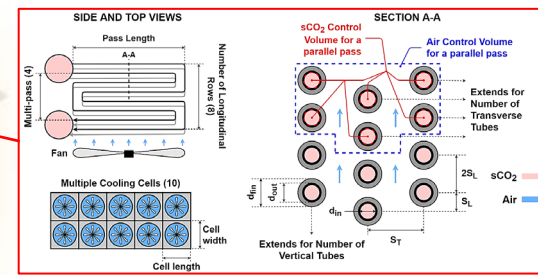
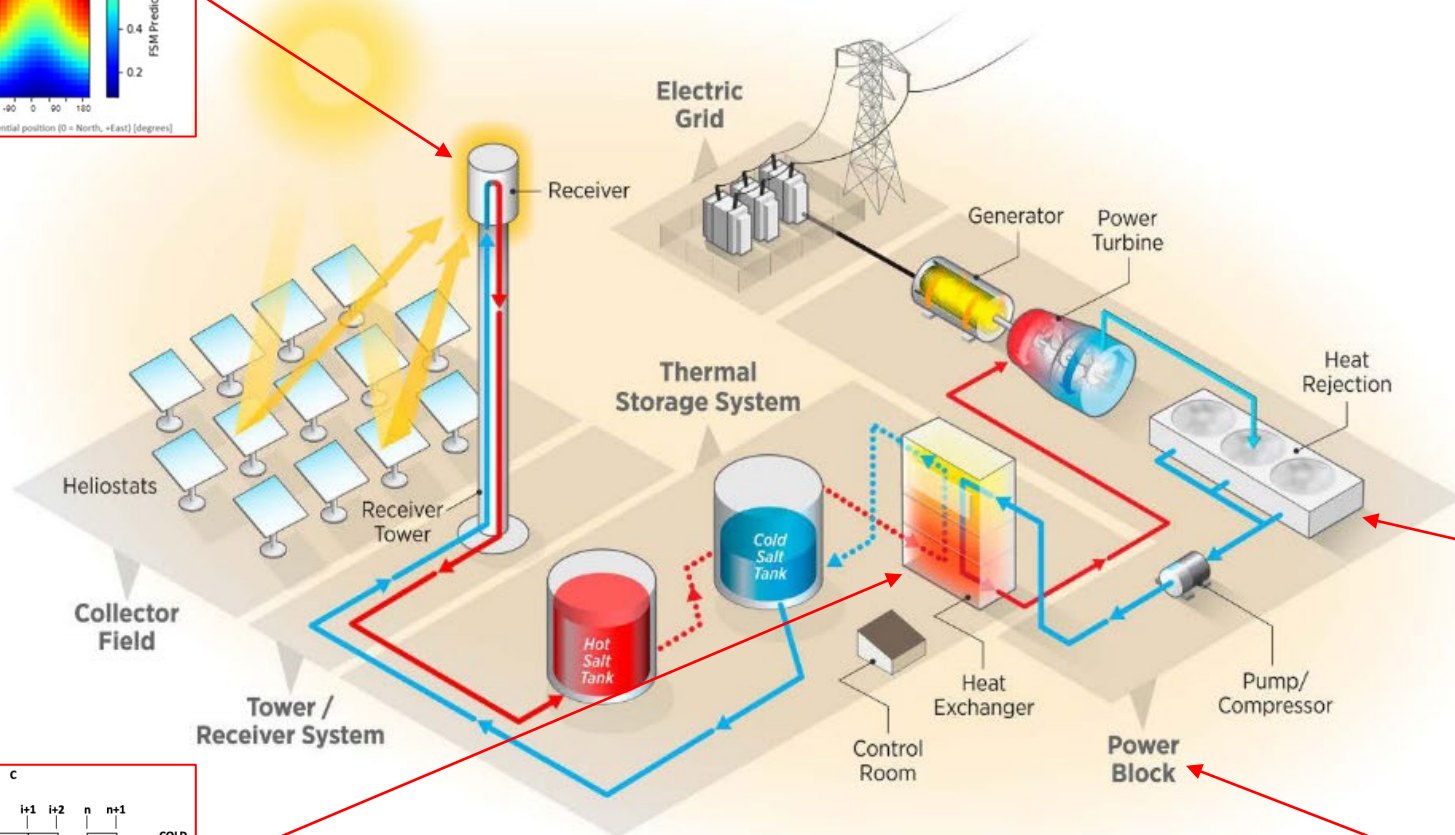
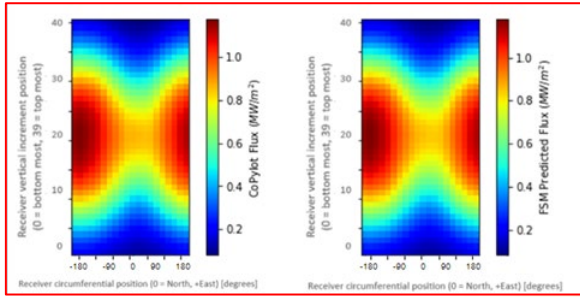


Introduction

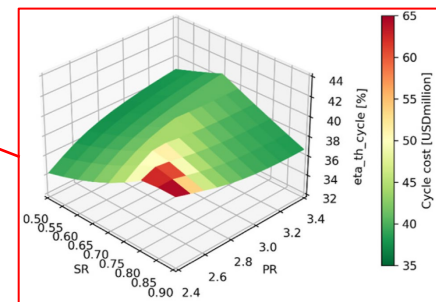


Schematic of a sCO₂-CSP plant with TES, from Mehos et al. (2017)

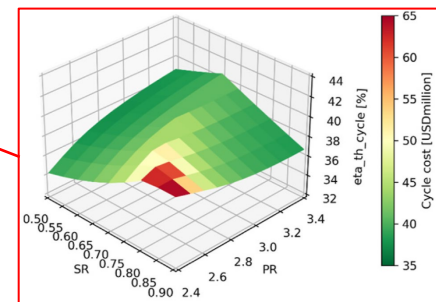
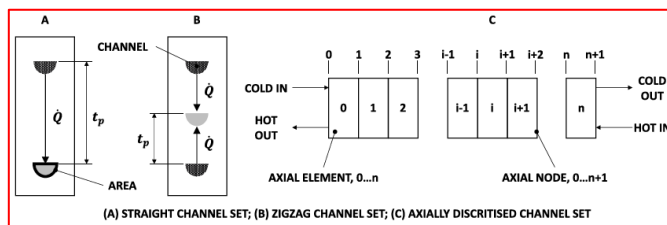
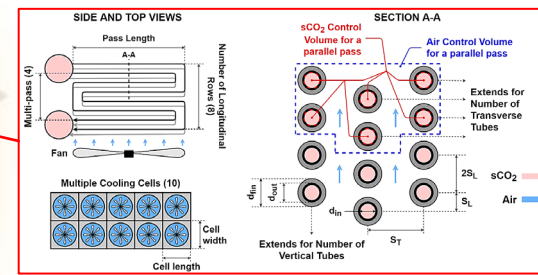
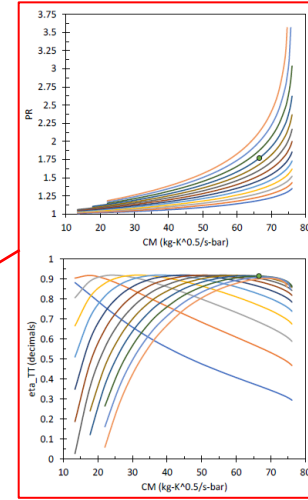
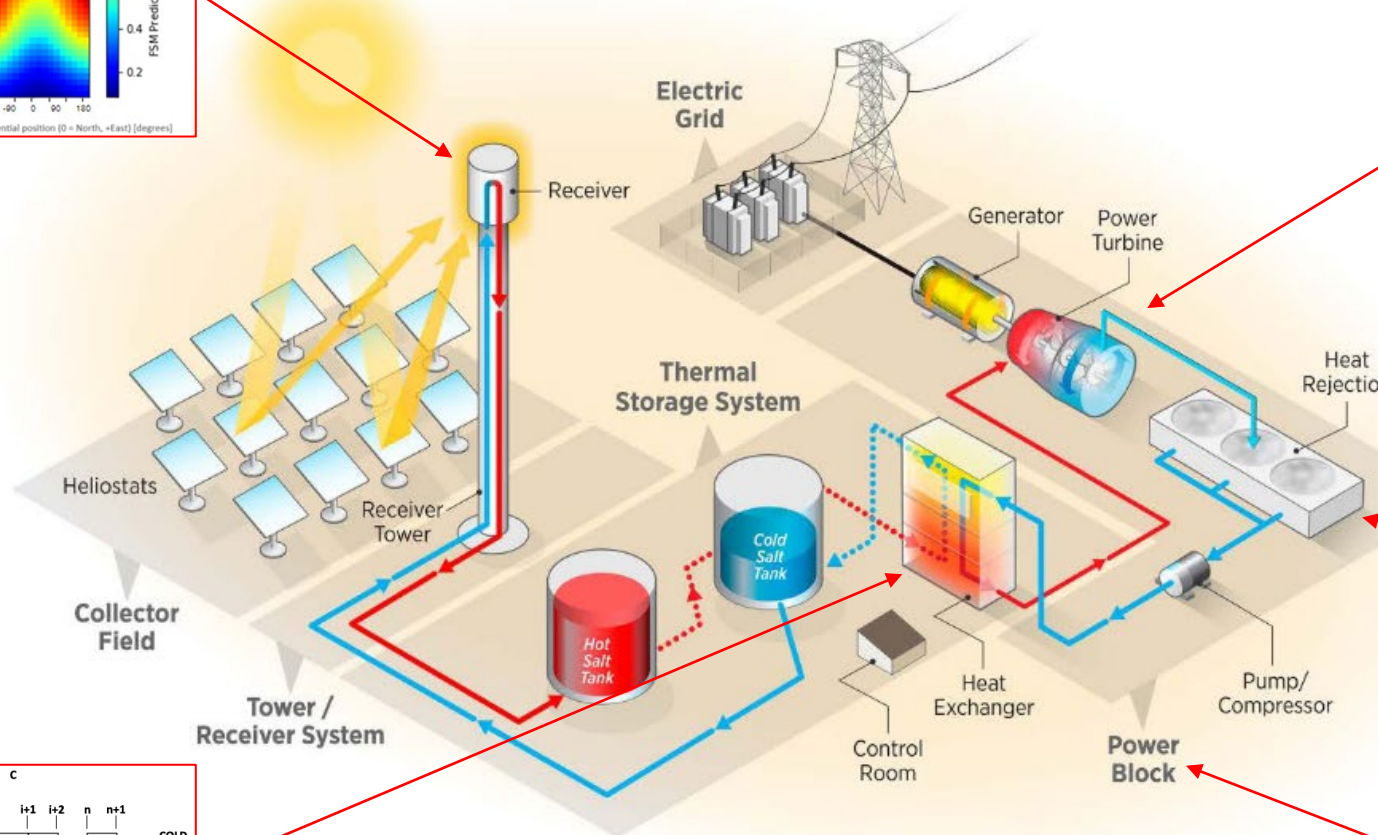
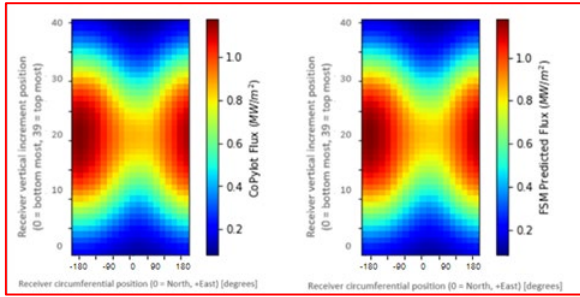
Introduction



Schematic of a sCO₂-CSP plant with TES, from Mehos et al. (2017)



Introduction



Schematic of a sCO₂-CSP plant with TES, from Mehos et al. (2017)

| | | Dostal et al. (2004) | Carstens (2007) | Seidel (2010) | Kulhanek & Dostal (2011a) | Turchi et al. (2013) | Dyreby (2014) | Neises & Turchi (2014) | Padilla et al. (2015) | Osorio et al. (2016) | Binotti et al. (2017) | Luu et al. (2017a) | Luu et al. (2017b) | Neises & Turchi (2019) | Thanganadar et al (2020) | Correa et al (2021) | Yang et al (2023) |
|---|--------------------------------------|----------------------|-----------------|---------------|---------------------------|----------------------|---------------|------------------------|-----------------------|----------------------|-----------------------|--------------------|--------------------|------------------------|--------------------------|---------------------|-------------------|
| Study type | Steady-state | x | | | x | x | x | x | x | | | | | | | x | |
| | Quasi-steady | | | x | | | | | | x | x | x | | x | x | | x |
| | Dynamic | | x | | | | | | | | | | x | | | | |
| Turbomachinery models | Isentropic | | | x | x | x | | x | x | x | x | x | | x | x | | |
| | Dyreby's method/ curve fit | | | | | | x | | | | | | x | | x | x | x |
| | Performance maps by others/ software | x | x | | | | | | | | | | | | | | |
| | Tailor-made design and maps | | | | | | | | | | | | | | | | |
| | Inertia effects | | | | | | | | | | | | | | | | |
| Off-design performance, control and simulations | Off-design performance | | | | | | x | | | | | | | | | | x |
| | Off-design control | x | | | | | | | | | | | | | | x | |
| | Daily simulation | | | | | | | | | x | | x | x | | | | |
| | Annual simulation | | | x | | | | | | | x | | | | x | | |
| | Fast transients | | x | | | | | | | | | | | | | | |

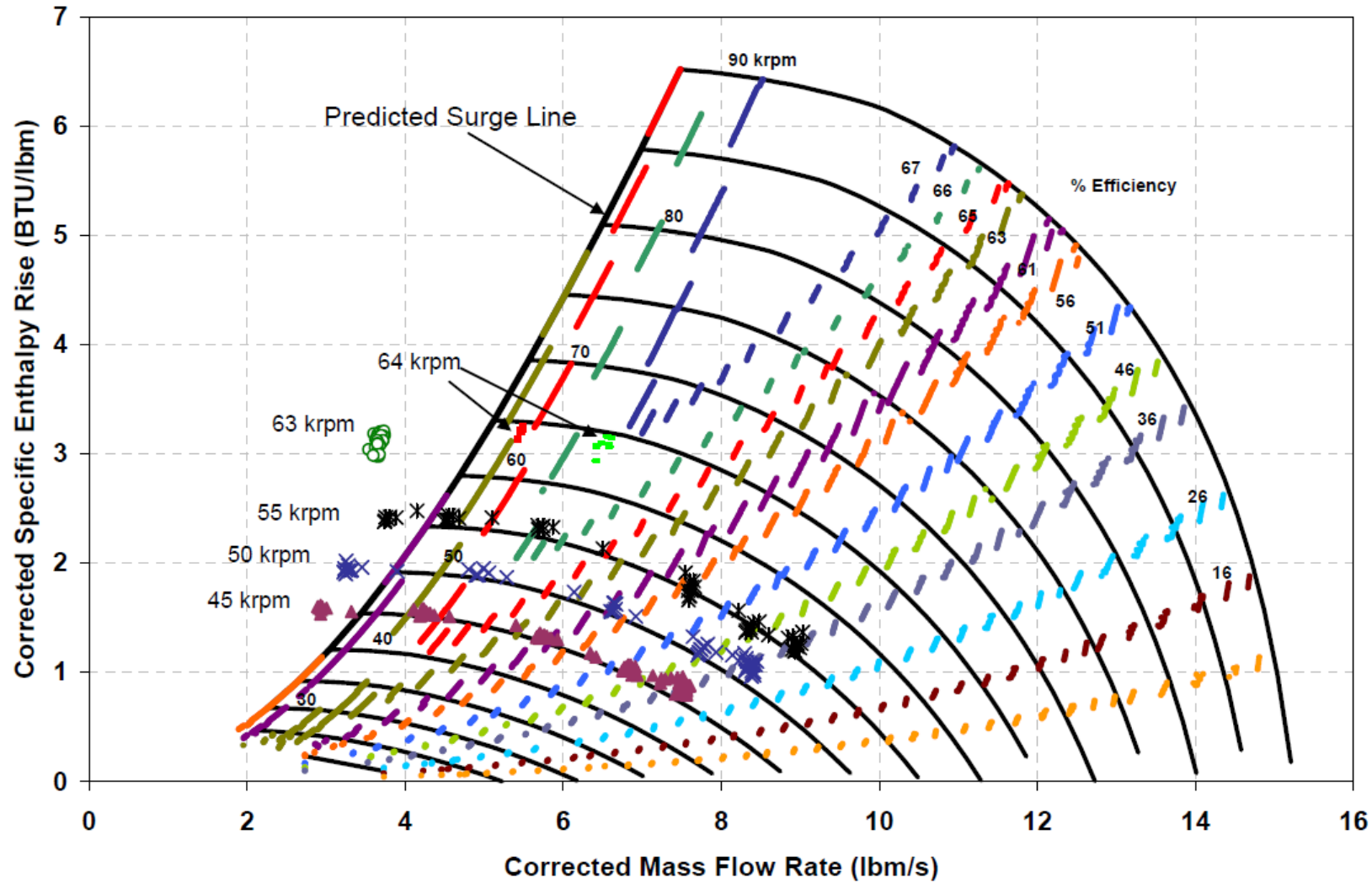
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|---|--------------------------------------|----------------------|-----------------|---------------|---------------------------|----------------------|---------------|------------------------|-----------------------|----------------------|-----------------------|--------------------|--------------------|------------------------|--------------------------|---------------------|-------------------|
| Study type | Steady-state | x | | | x | x | x | x | x | | | | | | | x | |
| | Quasi-steady | | | x | | | | | | x | x | x | | x | x | | x |
| | Dynamic | | x | | | | | | | | | | x | | | | |
| Turbomachinery models | Isentropic | | | x | x | x | | x | x | x | x | x | | x | x | | |
| | Dyreby's method/ curve fit | | | | | | x | | | | | | x | | x | x | x |
| | Performance maps by others/ software | x | x | | | | | | | | | | | | | | |
| | Tailor-made design and maps | | | | | | | | | | | | | | | | |
| | Inertia effects | | | | | | | | | | | | | | | | |
| Off-design performance, control and simulations | Off-design performance | | | | | | x | | | | | | | | | | x |
| | Off-design control | x | | | | | | | | | | | | | | x | |
| | Daily simulation | | | | | | | | | x | | x | x | | | | |
| | Annual simulation | | | x | | | | | | | x | | | | x | | |
| | Fast transients | | x | | | | | | | | | | | | | | |

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| | Quasi-steady | | | x | | | | | | x | x | x | | x | x | | x |
| | Dynamic | | x | | | | | | | | | | x | | | | |
| Turbomachinery models | Isentropic | | | x | x | x | | x | x | x | x | x | | x | x | | |
| | Dyreby's method/ curve fit | | | | | | x | | | | | | x | | x | x | x |
| | Performance maps by others/ software | x | x | | | | | | | | | | | | | | |
| | Tailor-made design and maps | | | | | | | | | | | | | | | | |
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| Off-design performance, control and simulations | Off-design performance | | | | | | x | | | | | | | | | | x |
| | Off-design control | x | | | | | | | | | | | | | | x | |
| | Daily simulation | | | | | | | | | x | | x | x | | | | |
| | Annual simulation | | | x | | | | | | | x | | | | x | | |
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| | Quasi-steady | | | x | | | | | | x | x | x | | x | x | | x |
| | Dynamic | | x | | | | | | | | | | x | | | | |
| Turbomachinery models | Isentropic | | | x | x | x | | x | x | x | x | x | | x | x | | |
| | Dyreby's method/ curve fit | | | | | | x | | | | | | x | | x | x | x |
| | Performance maps by others/ software | x | x | | | | | | | | | | | | | | |
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| | Off-design control | x | | | | | | | | | | | | | | x | |
| | Daily simulation | | | | | | | | | x | | x | x | | | | |
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| Study type | Steady-state | x | | | x | x | x | x | x | | | | | | | x | |
| | Quasi-steady | | | x | | | | | | x | x | x | | x | x | | x |
| | Dynamic | | x | | | | | | | | | | x | | | | |
| Turbomachinery models | Isentropic | | | x | x | x | | x | x | x | x | x | | x | x | | |
| | Dyreby's method/ curve fit | | | | | | x | | | | | | x | | x | x | x |
| | Performance maps by others/ software | x | x | | | | | | | | | | | | | | |
| | Tailor-made design and maps | | | | | | | | | | | | | | | | |
| | Inertia effects | | | | | | | | | | | | | | | | |
| Off-design performance, control and simulations | Off-design performance | | | | | | x | | | | | | | | | | x |
| | Off-design control | x | | | | | | | | | | | | | | x | |
| | Daily simulation | | | | | | | | | x | | x | x | | | | |
| | Annual simulation | | | x | | | | | | | x | | | | x | | |
| | Fast transients | | x | | | | | | | | | | | | | | |

Dyreby's method



SNL compressor performance map, from Wright et al. (2010)

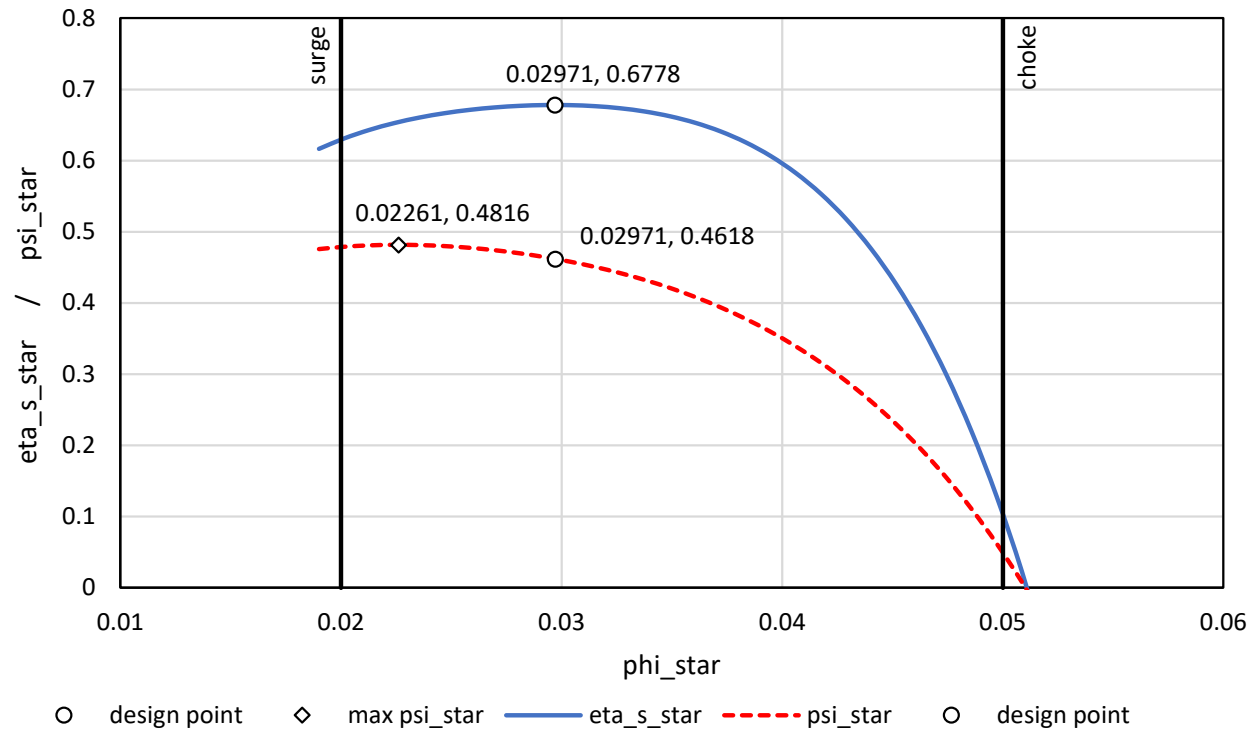
$$\eta^* = -0.7069 + 168.6\phi^* - 8089\phi^{*2} + 182725\phi^{*3} - 1.638e^6\phi^{*4}$$

$$\psi^* = 0.04049 + 54.7\phi^* - 2505\phi^{*2} + 53224\phi^{*3} - 498626\phi^{*4}$$

$$\phi^* = \phi \left(\frac{N}{N_{nom}} \right)^{0.2} = \frac{\dot{m}}{\rho_1 u_2 D_2^2} \left(\frac{N}{N_{nom}} \right)^{0.2}$$

$$\eta^* = \eta \left(\frac{N_{nom}}{N} \right)^{(20\phi^*)^5}$$

$$\psi^* = \psi \left(\frac{N_{nom}}{N} \right)^{(20\phi^*)^3} = \frac{w_{c.s}}{u_2^2} \left(\frac{N_{nom}}{N} \right)^{(20\phi^*)^3}$$



Head and efficiency correlations, from Dyreby (2014)

KAIST-TMD:

- Private 1D mean-line based tool to size centrifugal compressors and generate performance maps.
- Developed by Lee (2016) for the design of sCO₂ centrifugal compressors.
- Used by collaborators i.e., Cho et al. (2019) and Jeong et al (2020) for compressor-focused studies.

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AlFa CCD:

- Private 1D mean-line based tool to size centrifugal compressors and generate performance maps.
- Developed by Ameli et al (2018) for the design of sCO₂ centrifugal compressors.

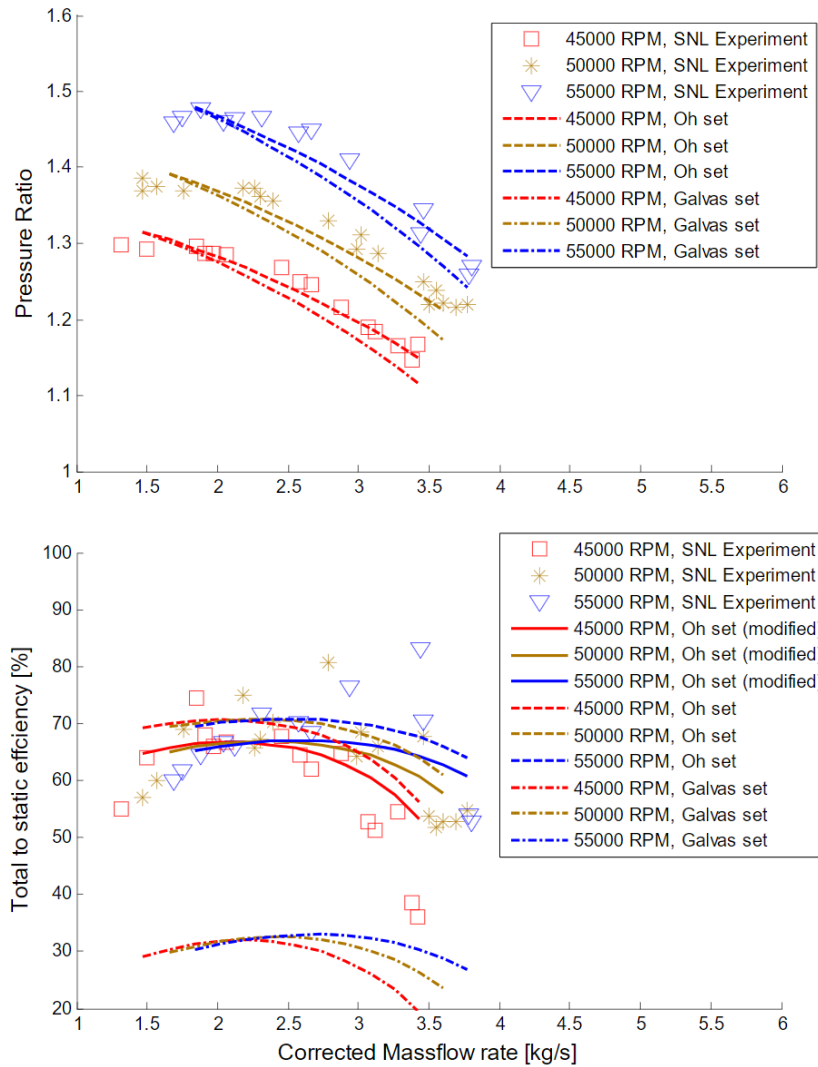
1D mean-line codes



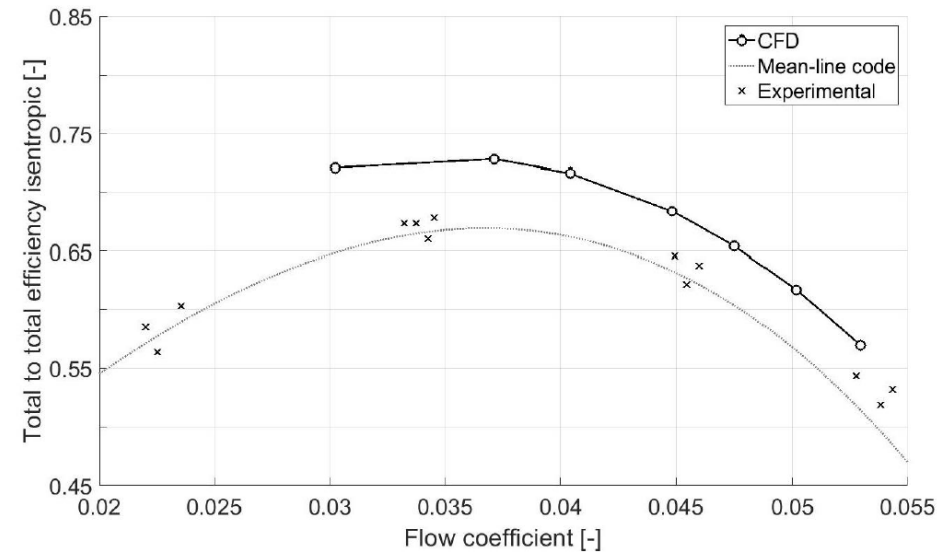
Compared to this work:

- Fewer compressor components considered.
- Models not fully documented.
- Different correlation sets applied.
- Verification results leave room for improvement.

1D mean-line codes

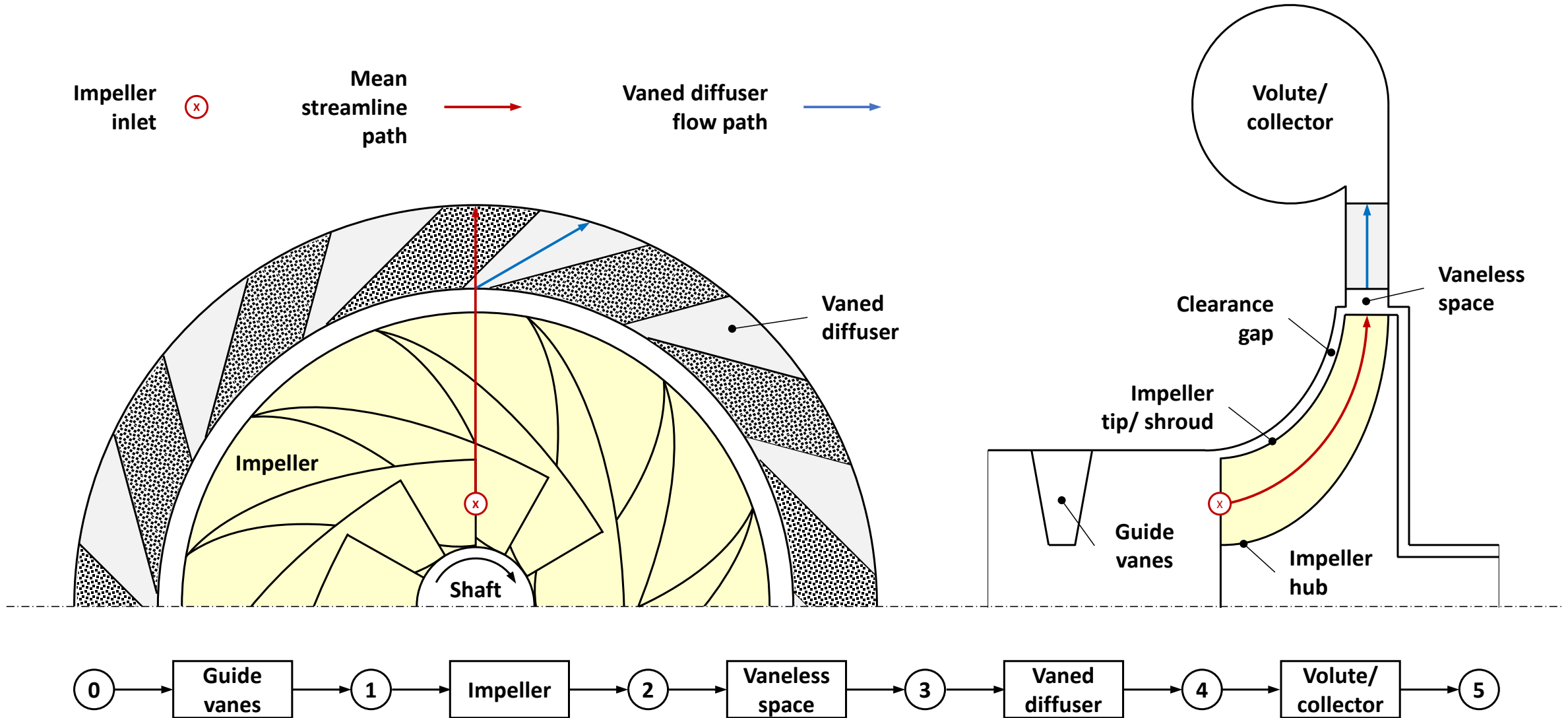


Verification results, from Lee (2016)



Verification results, from Ameli et al. (2018)

Model development

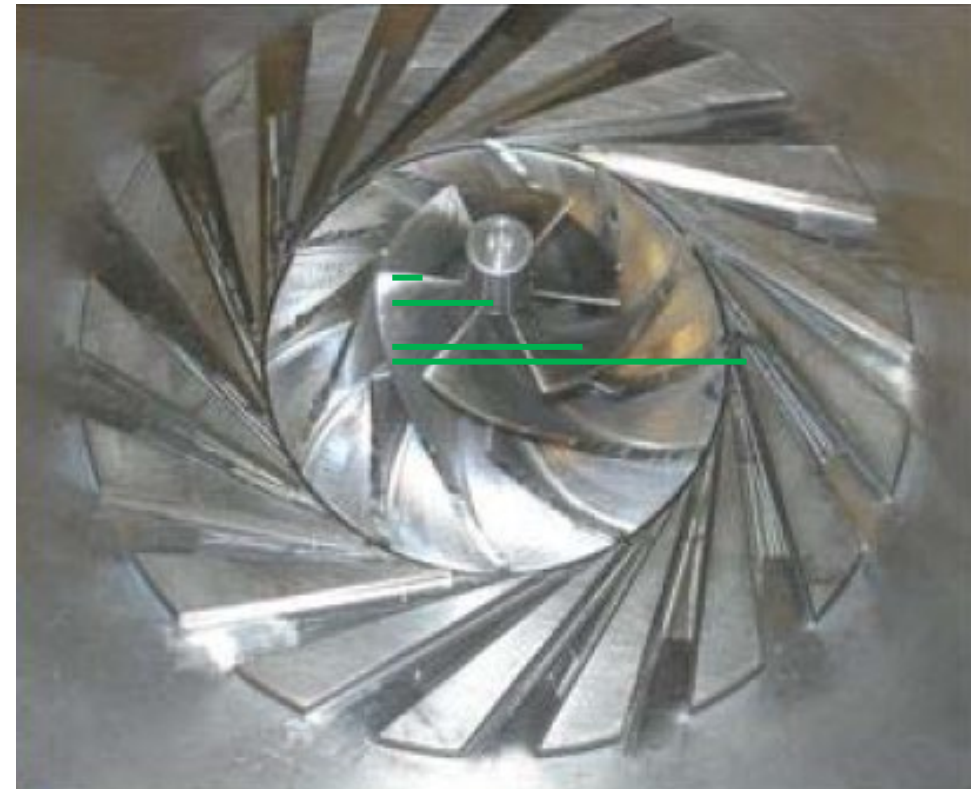
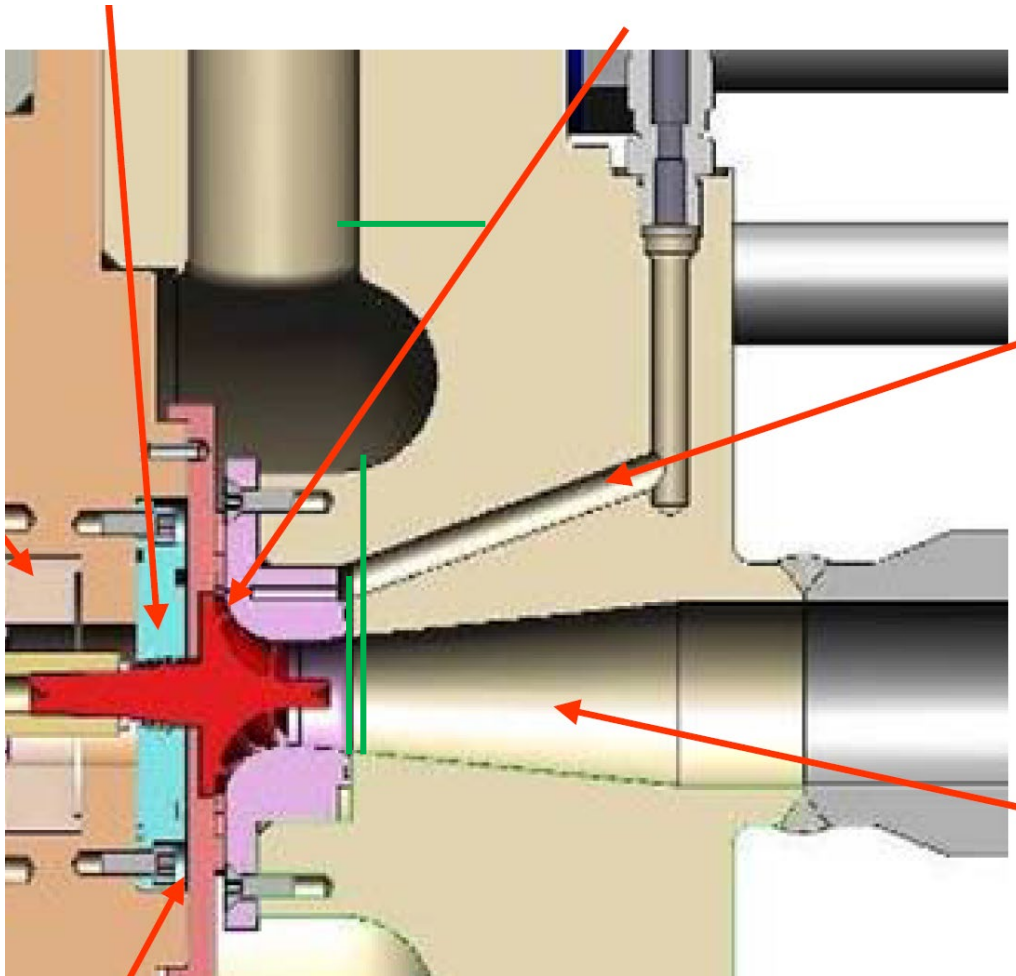




SNL compressor wheel, from Wright et al. (2010)

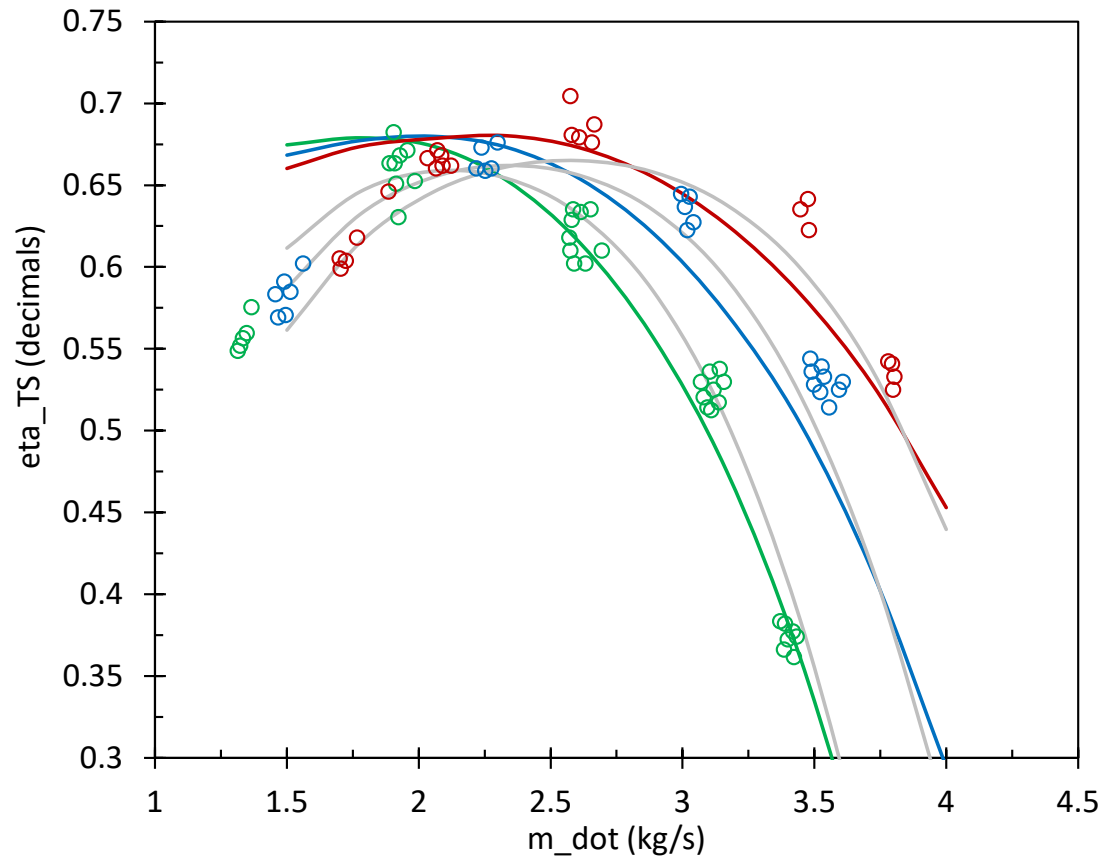
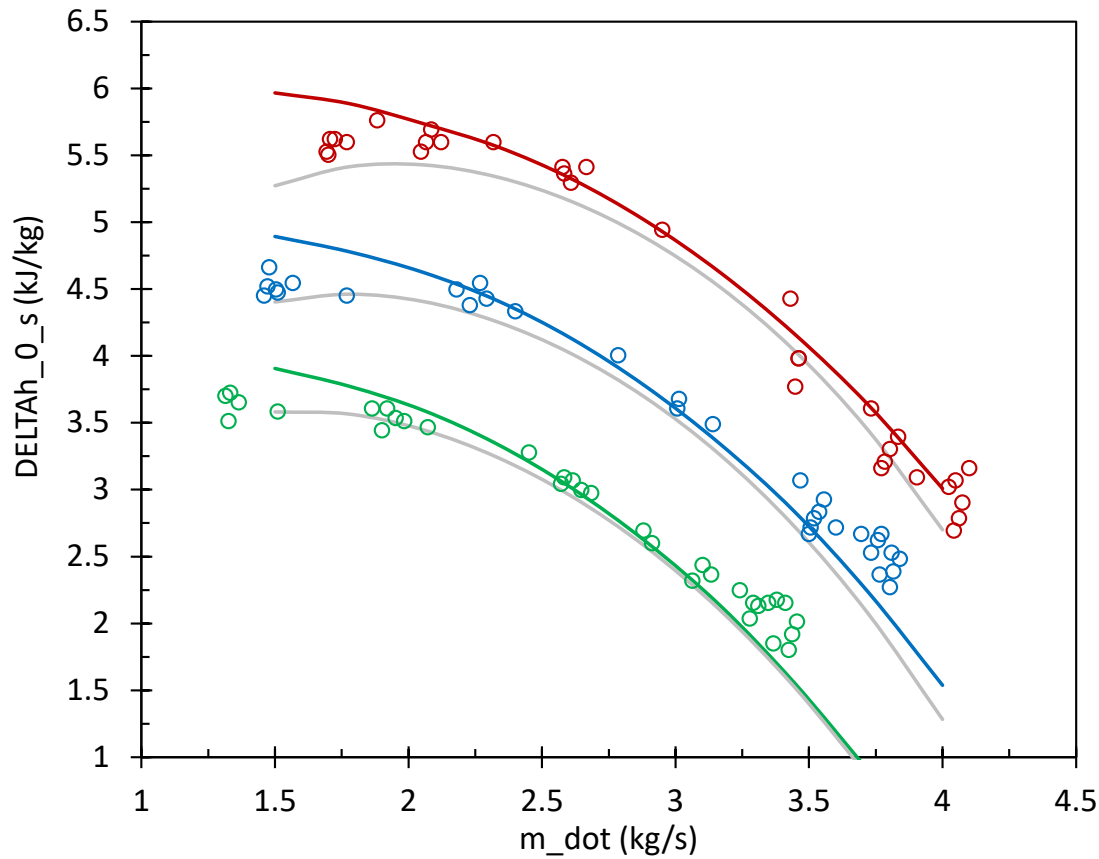
| Specification | Units | Value |
|--|-------|-------|
| <i>Known, from Wright et al. (2010)</i> | | |
| Number of full blades | - | 6 |
| Number of splitter blades | - | 6 |
| Number of vaned diffuser channels | - | 17 |
| Blade angle at impeller inlet | ° | 50.0 |
| Blade angle at impeller exit (backswept) | ° | 50.0 |
| Vaned diffuser angle at diffuser inlet | ° | 71.5 |
| Hub radius | mm | 2.54 |
| Shroud radius | mm | 9.37 |
| Impeller exit radius | mm | 18.68 |
| Tip clearance | mm | 0.254 |
| Blade thickness | mm | 0.76 |
| Blade height at exit | mm | 1.71 |
| Nominal mass flow rate | kg/s | 3.53 |
| Total pressure at inlet | kPa | 7687 |
| Total temperature at inlet | °C | 32.15 |
| <i>Assumed</i> | | |
| Ratio of splitter blade to full blade meridional length | - | 0.5 |
| Blade angle at impeller inlet (at hub, mean position and shroud) | ° | 50.0 |
| Vaned diffuser inlet diameter | mm | 40 |
| Vaned diffuser exit diameter | mm | 75 |
| Vaned diffuser height | mm | 1.71 |
| Collector exit diameter | mm | 29.89 |

Model verification



Images of SNL compressor, from Wright et al. (2010)

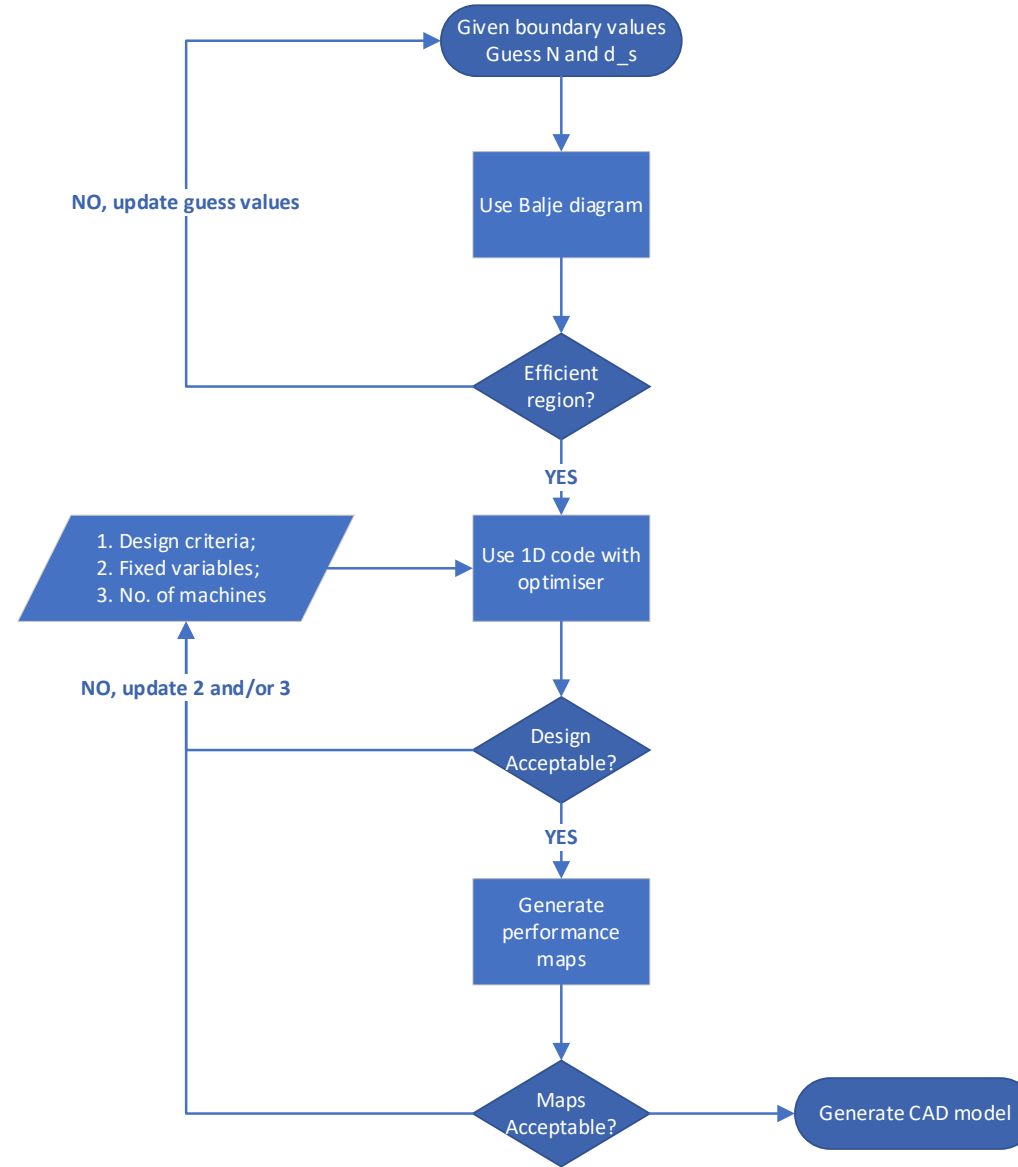
Model verification



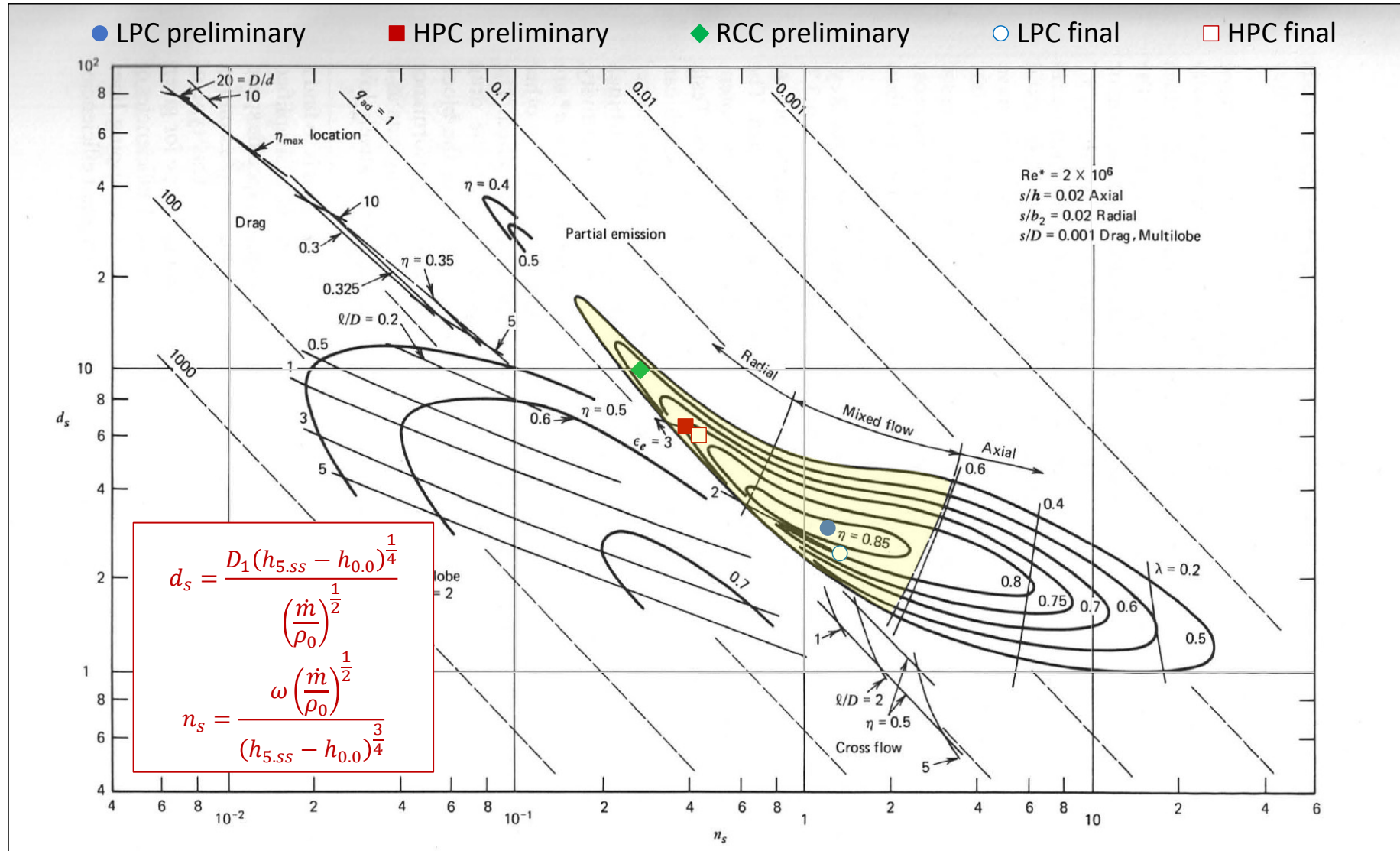
○ 45 krpm ○ 50 krpm ○ 55 krpm — 45 krpm Model — 50 krpm Model — 55 krpm Model — 45 krpm Dyreby — 50 krpm Dyreby — 55 krpm Dyreby

Verification results, test data from Wright et al. (2010)

Sizing method



Initial sizing



Marked up specific diameter-speed diagram, original image from Balje (1981)

| Specification | Units | LPC | HPC |
|--|-------|----------------|-------|
| <i>Design criteria</i> | | | |
| Mass flow rate | kg/s | 397 | 397 |
| Total pressure at inlet | kPa | 7353 | 9768 |
| Total temperature at inlet | °C | 45 | 45 |
| Total pressure ratio | - | 1.356 | 2.560 |
| Total-to-total efficiency (target) | % | 89 | 89 |
| <i>Fixed variables</i> | | | |
| Number of full blades | - | 19 | 19 |
| Number of vaned diffuser channels | - | 28 | 28 |
| Nominal design speed | rpm | 9000 | 9000 |
| <i>Optimised variables</i> | | | |
| Hub to shroud radius ratio | - | [0.3, 0.6] | |
| Shroud to tip radius ratio | - | [0.35, 0.65] | |
| Vaned diffuser inlet to impeller exit radius ratio | - | [1.025, 1.075] | |
| Vaned diffuser exit to inlet radius ratio | - | [1.25, 1.75] | |
| Inlet swirl angle | ° | [0, 35] | |
| Blade angle at impeller inlet (mean position) | ° | [25, 50] | |
| Blade angle at impeller exit (backswept) | ° | [25, 50] | |

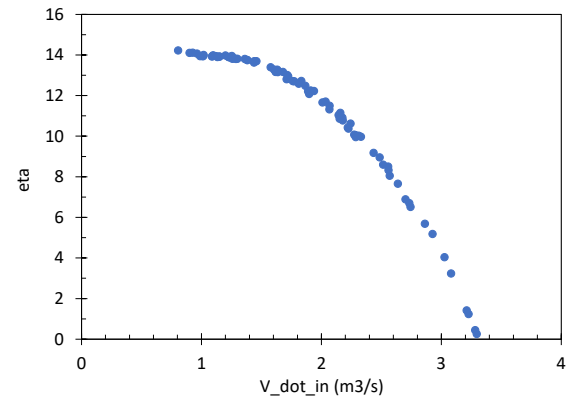
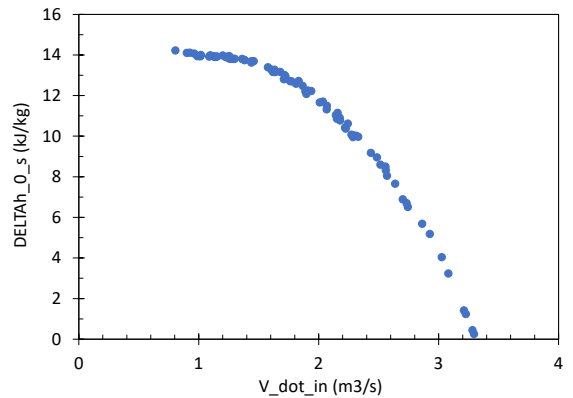
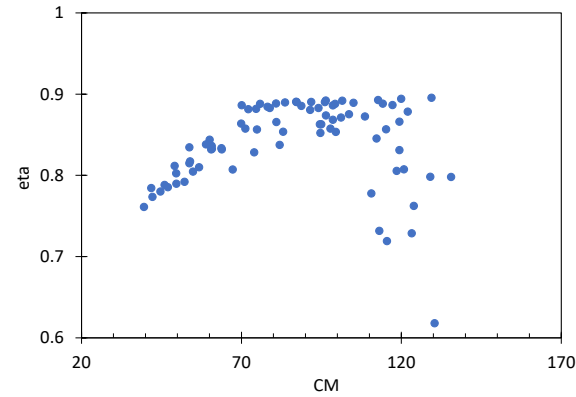
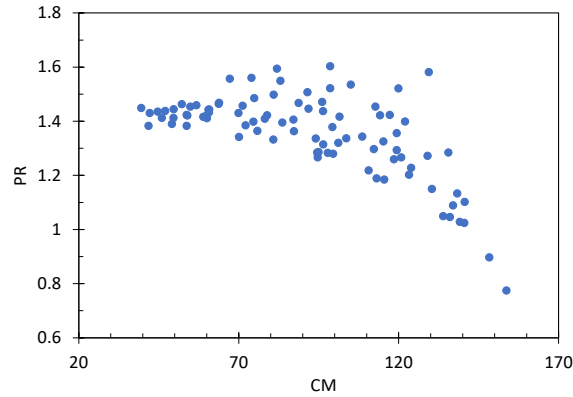
$$OBJECTIVE = X_1 \left(\left| \frac{\eta_{TT} - \eta_{TT.target}}{\eta_{TT.target}} \right| \right) + X_2 \left(\left| \frac{\eta_{TS} - \eta_{TT.target}}{\eta_{TT.target}} \right| \right)$$

$$X_1 = 0.9; X_2 = 0.1$$

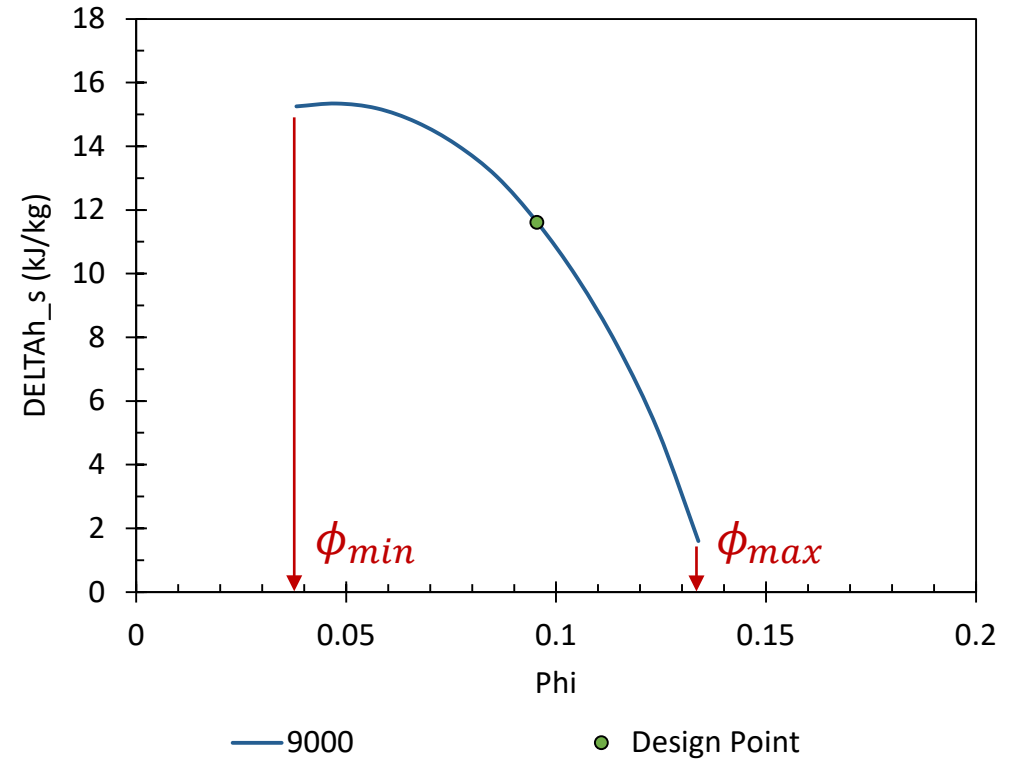
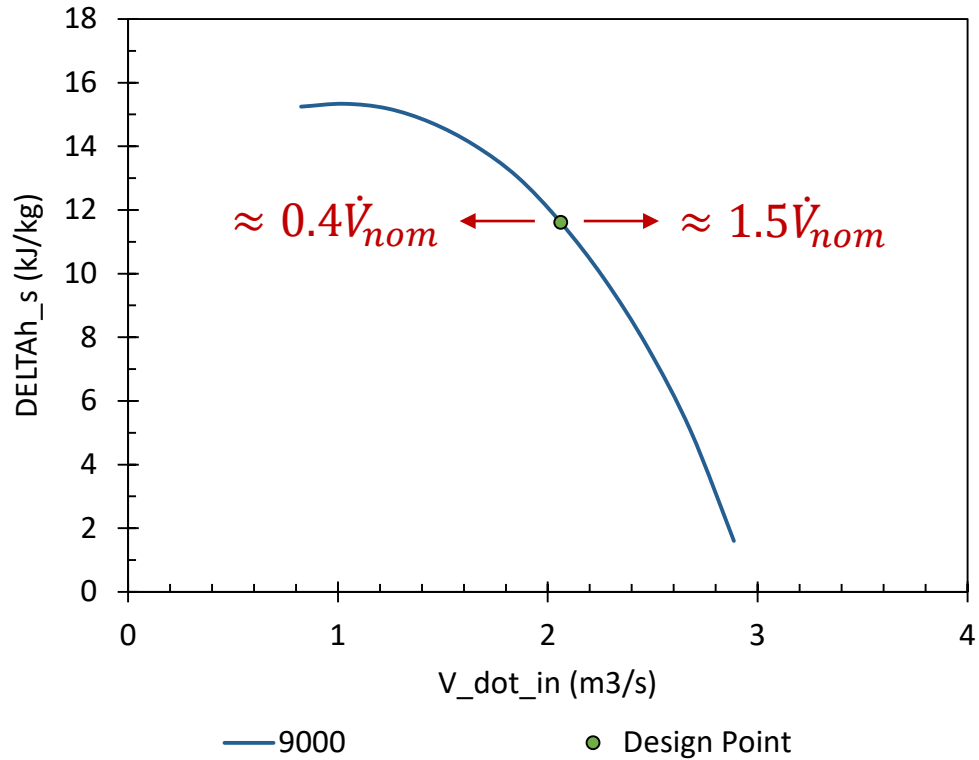
| Specification | Units | LPC | HPC |
|--|--------------------|--------|---------|
| <i>Calculated geometry</i> | | | |
| Inlet swirl angle | ° | 35 | 17.5 |
| Blade angle at impeller inlet (at hub, mean position and shroud) | ° | 25.5 | 37.5 |
| Blade angle at impeller exit (backswept) | ° | 49.5 | 37.5 |
| Vaned diffuser mean flow path angle | ° | 60.5 | 68.5 |
| Blade height at exit; vaned diffuser height | mm | 29.280 | 8.334 |
| Inlet guide vane upstream diameter | mm | 200.7 | 137.0 |
| Hub diameter | mm | 70.0 | 70.5 |
| Shroud diameter | mm | 232.6 | 157.6 |
| Impeller exit diameter | mm | 358.0 | 450.2 |
| Vaned diffuser inlet diameter | mm | 384.9 | 483.9 |
| Vaned diffuser exit diameter | mm | 672.6 | 846.8 |
| Volute exit diameter | mm | 211.3 | 105.5 |
| Axial length | mm | 115.80 | 91.33 |
| Inertia | kg-mm ² | 78 968 | 181 881 |
| <i>Performance at design point</i> | | | |
| Minimum flow coefficient | - | 0.0382 | 0.0084 |
| Maximum flow coefficient | - | 0.1339 | 0.0314 |
| Volume flow rate at inlet | m ³ /s | 2.062 | 0.8986 |
| Isentropic head | kJ/kg | 11.61 | 27.30 |
| Total-to-total efficiency (actual) | % | 88.79 | 89.07 |
| Total-to-static efficiency | % | 80.59 | 80.19 |
| Compressor power | MW | -5.193 | -12.166 |

Performance maps

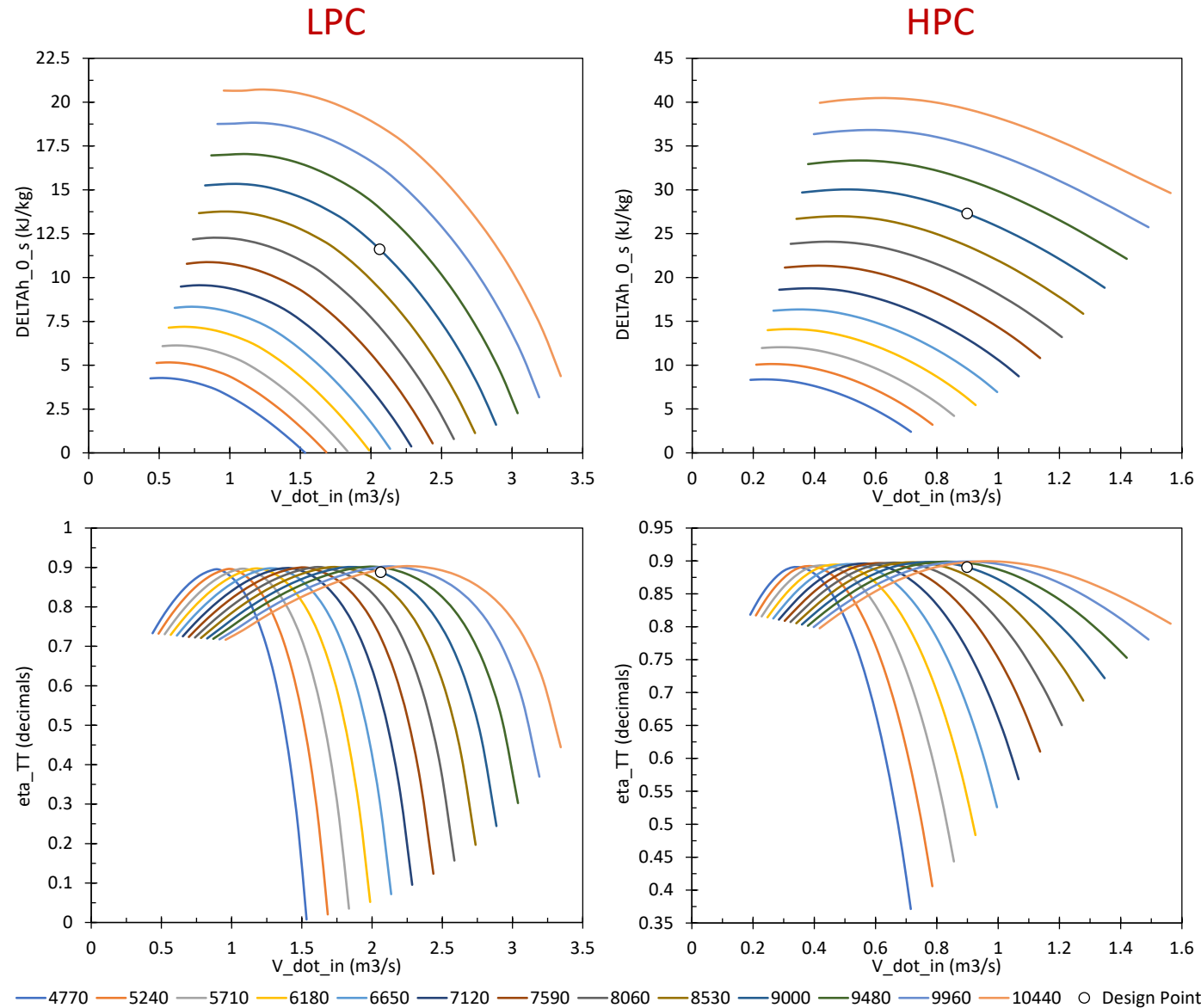
| Pressure (kPa) | Temperature (degC) | Mass Flow (kg/s) | PR | eta_TT | CM | CS | DELTAh_0_s (kJ/kg) | eta_TT | Q_dot_in (m3/s) | Speed (rpm) |
|----------------|--------------------|------------------|------|--------|--------|--------|--------------------|--------|-----------------|-------------|
| 6549.01 | 38.65 | 483.80 | 1.15 | 0.62 | 130.40 | 504.60 | 5.69 | 0.64 | 2.86 | 9000 |
| 7381.07 | 52.71 | 556.27 | 1.05 | 0.27 | 136.00 | 504.60 | 1.24 | 0.19 | 3.23 | 9000 |
| 6649.79 | 45.57 | 411.97 | 1.22 | 0.78 | 110.60 | 504.60 | 8.05 | 0.78 | 2.57 | 9000 |
| 6820.67 | 49.59 | 358.89 | 1.28 | 0.86 | 94.52 | 504.60 | 10.37 | 0.86 | 2.23 | 9000 |
| 8142.50 | 49.29 | 541.28 | 1.29 | 0.83 | 119.40 | 504.60 | 9.18 | 0.83 | 2.44 | 9000 |
| . | . | . | . | . | . | . | . | . | . | . |
| . | . | . | . | . | . | . | . | . | . | . |
| . | . | . | . | . | . | . | . | . | . | . |



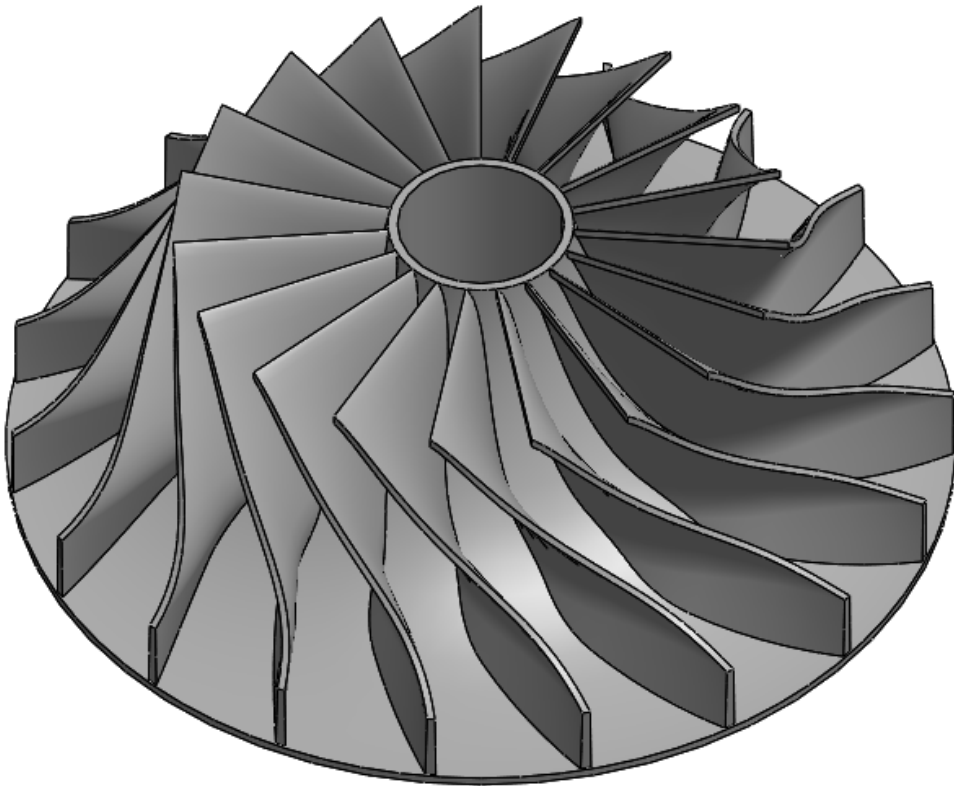
Performance maps



Performance maps

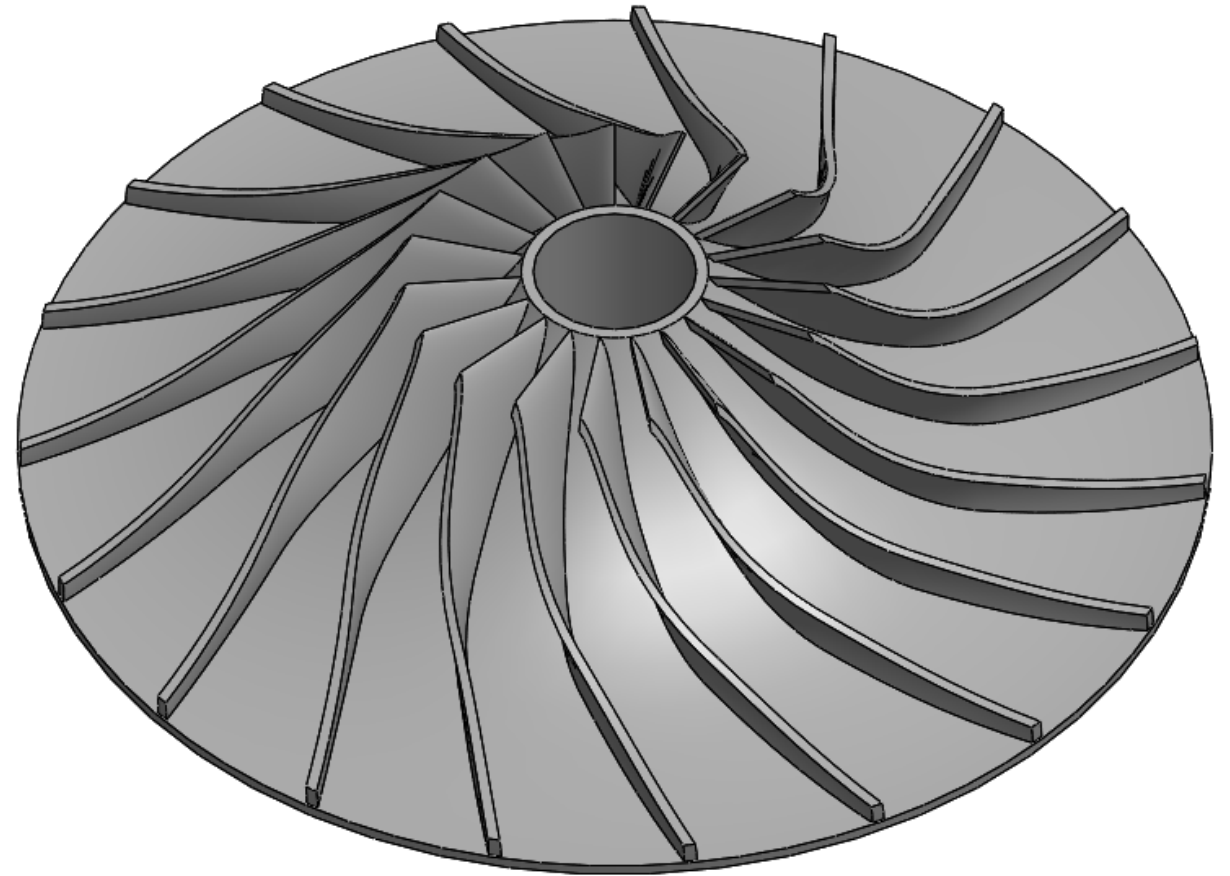


LPC



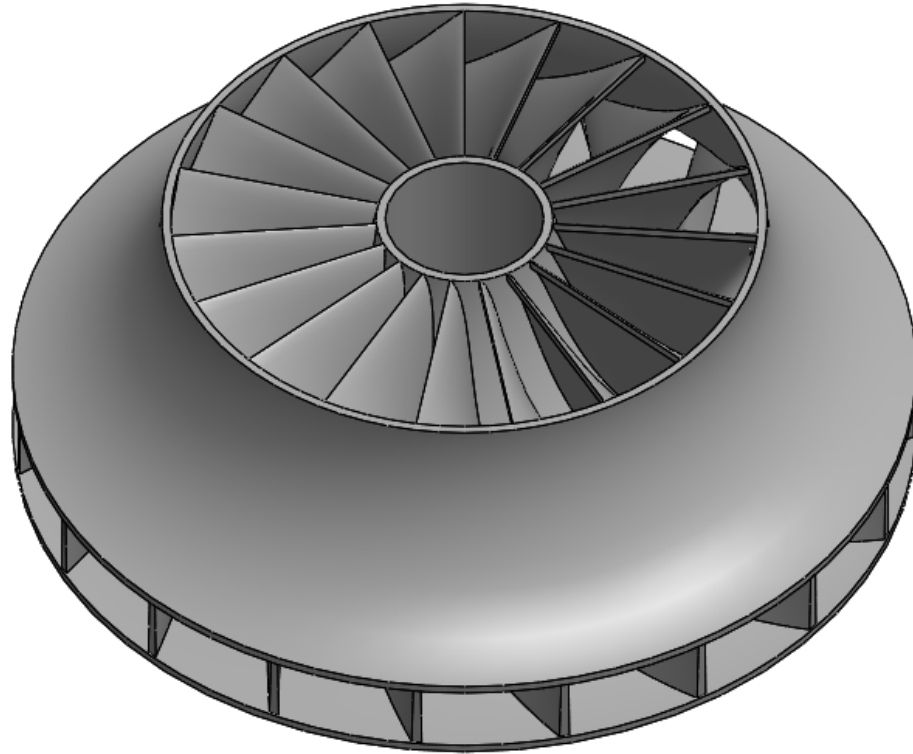
358 x 116

HPC



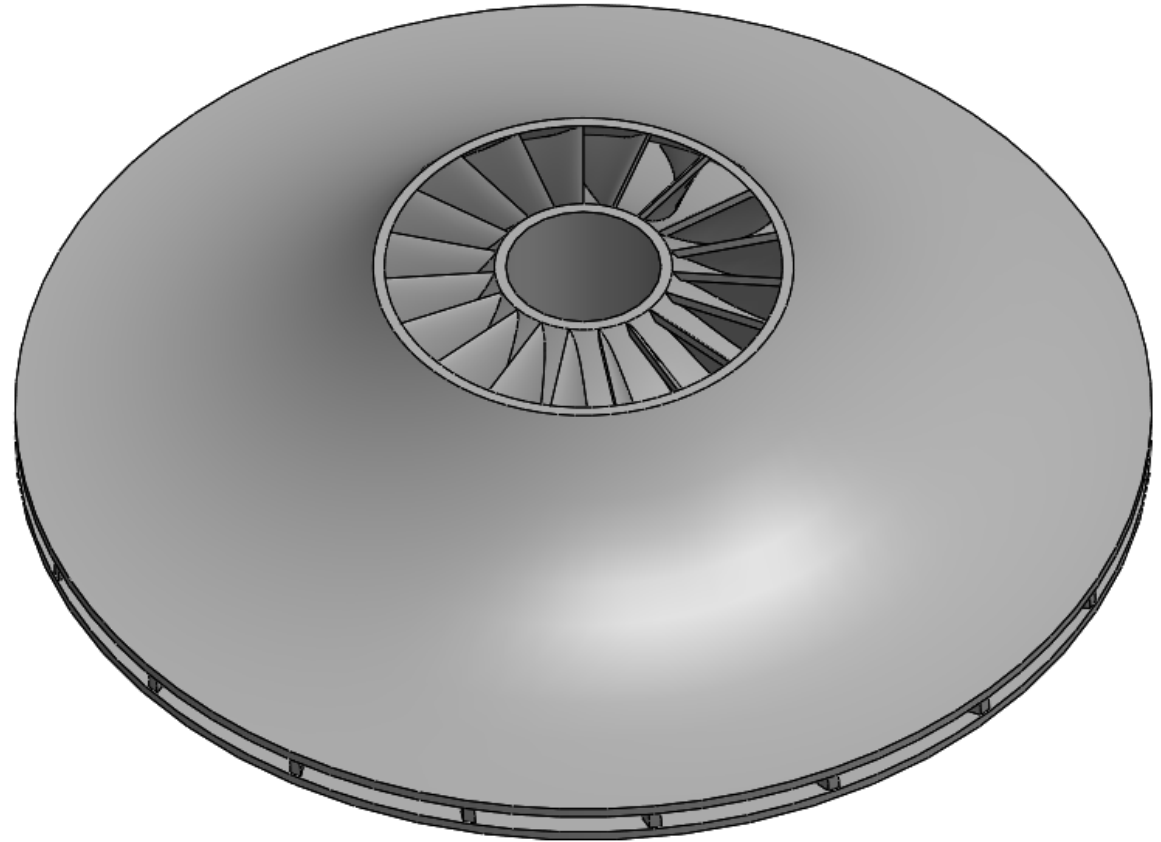
450 x 91

LPC



358 x 116

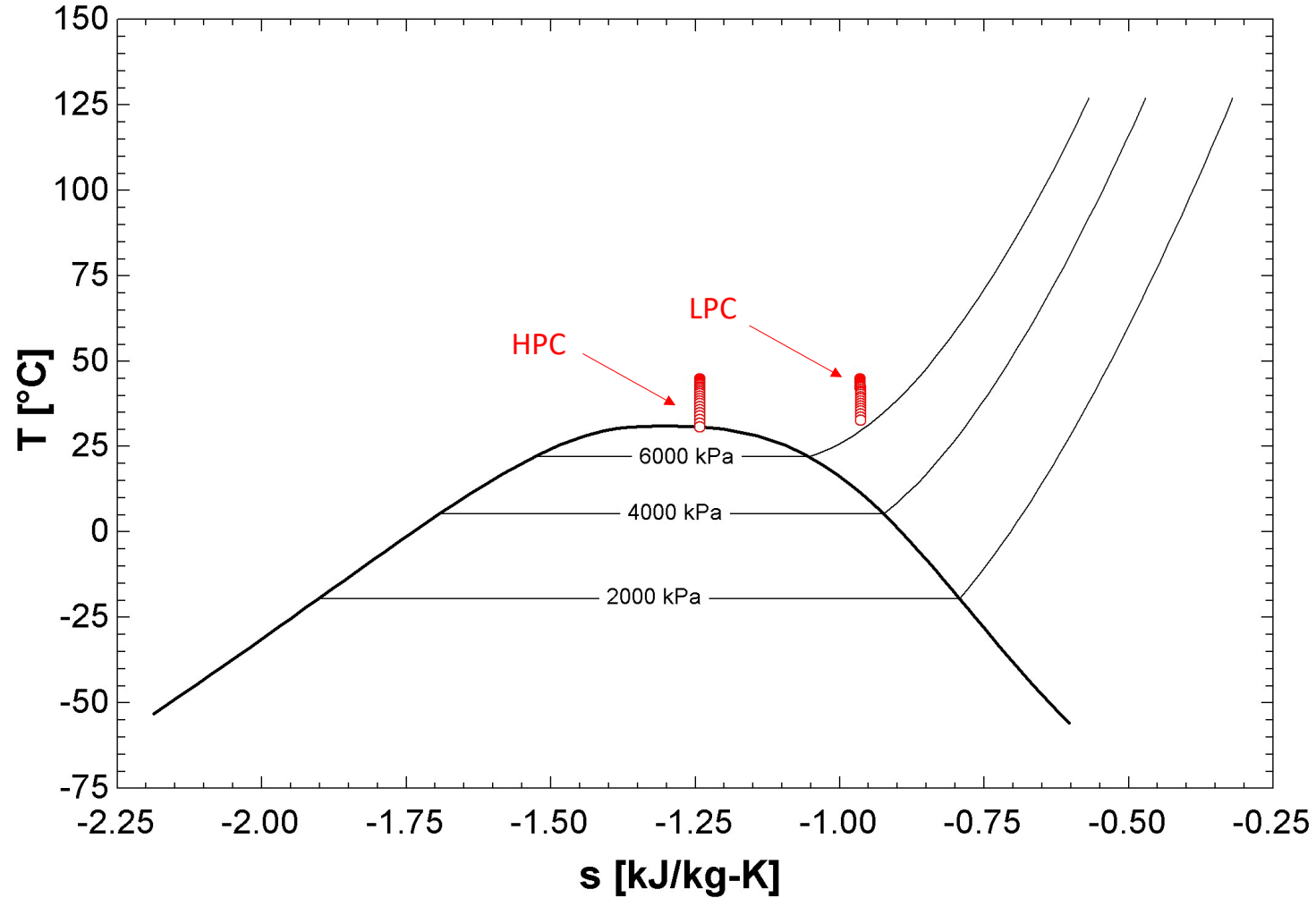
HPC



450 x 91

Minimum static temperatures

For the HPC, when operating at the highest speed and flow rate, a two-phase flow state may be encountered.



Summary and conclusions

- Dynamic compressor models are required for transient simulation studies of sCO₂ cycles.
- Most researchers apply Dyreby's correlations, which is useful, but has shortcomings.
- Except for KAIST-TMD and AlFa CCD, which are not fully documented and leave room for improvement, there are no suitable tools available to size and develop performance maps for sCO₂ radial compressors.

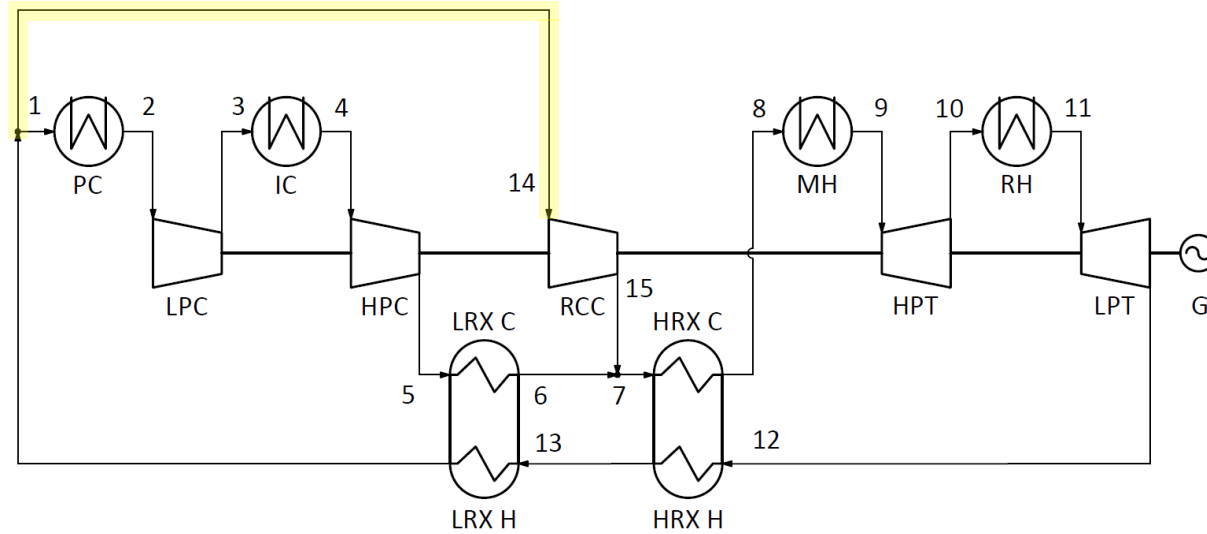
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 - A 1D mean-line code to size centrifugal compressors was developed and verified.
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- In this work:
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 - The code was used to size centrifugal compressors and develop performance maps.
 - 3D models were developed to estimate the inertia of the compressors.
- The maps and inertia values may be used to model compressors in simulation software.
- The methods employed in this work may be used by others to model centrifugal compressors.

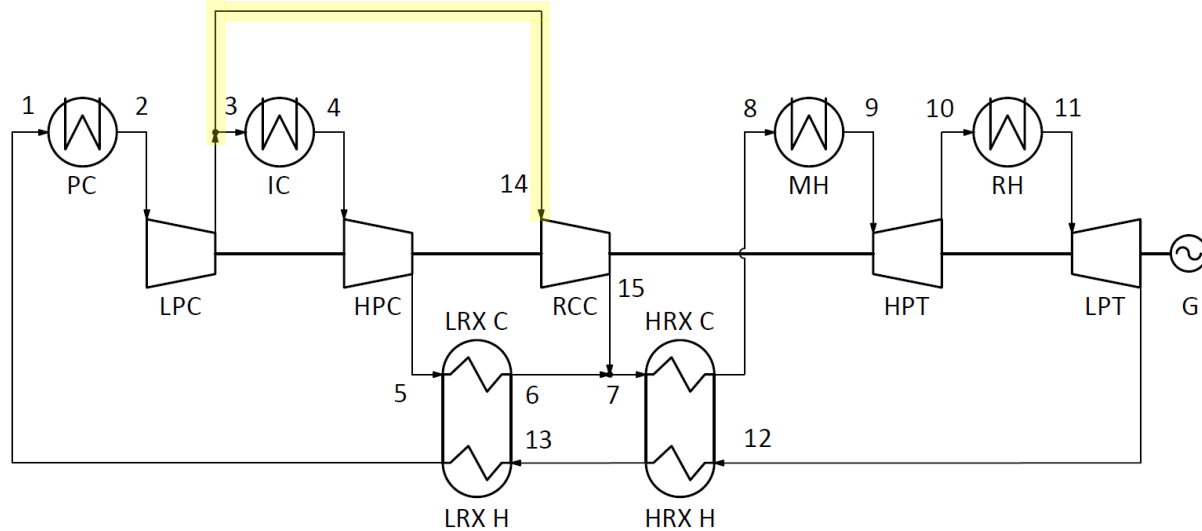
Q&A

Cycles of interest

Partial cooling with reheating cycle



Recompression with intercooling and reheating cycle



PC: Pre-cooler

IC: Intercooler

LPC: Low pressure compressor

HPC: High pressure compressor

RCC: Recompression compressor

MH: Main heater

RH: Reheater

HPT: High pressure turbine

LPT: Low pressure turbine

LRX: Low temperature recuperator

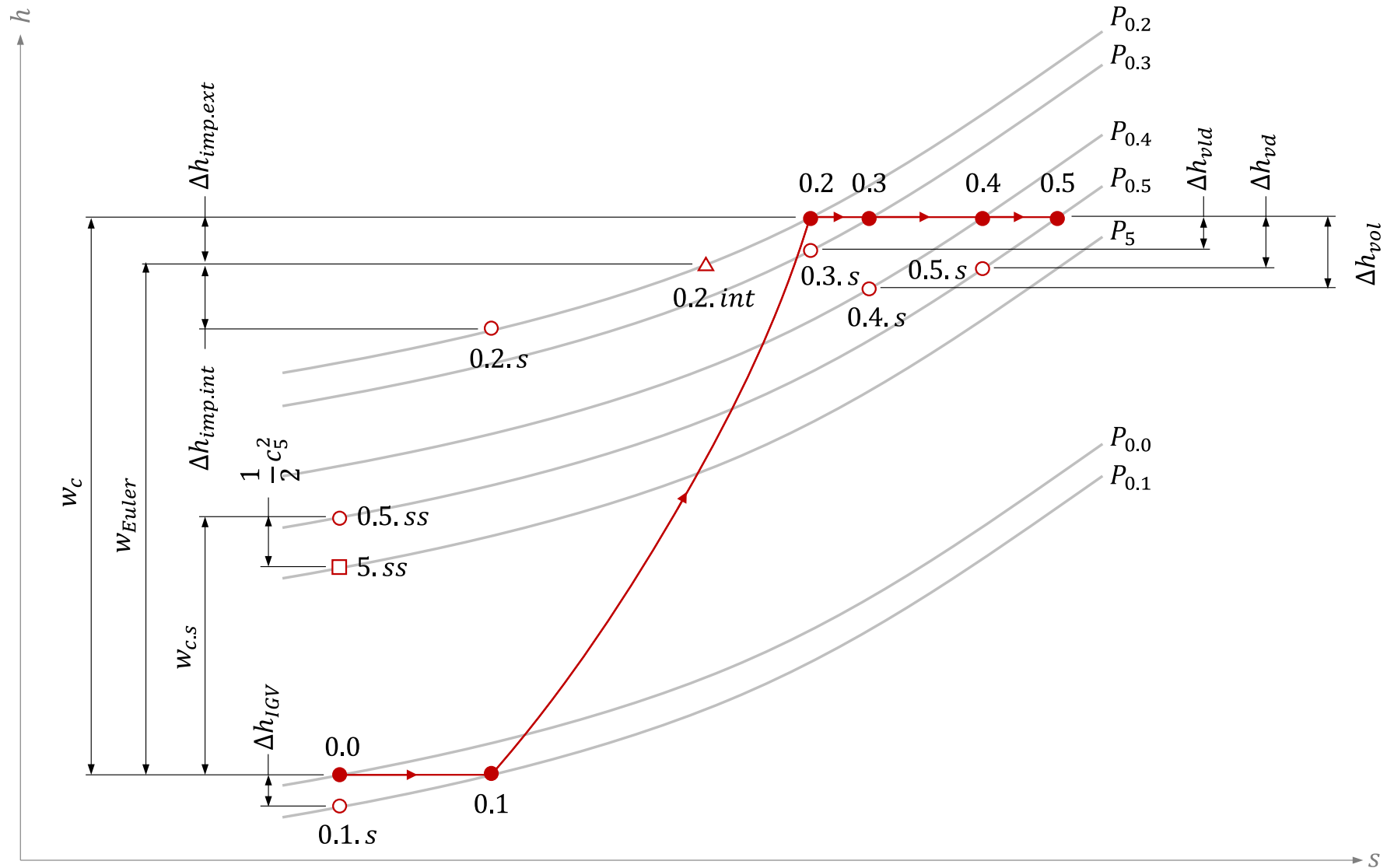
HRX: High temperature recuperator

_C: Cold side

_H: Hot side

G: Generator

Mollier diagram



Mass Balance (all elements)

$$\dot{m} = \rho A c$$

Energy Balance (impeller)

$$h_{0.out.s} = h_{0.in} - w_{Euler} - \Delta h_{imp.int}$$

$$h_{0.out} = h_{0.in} - w_{Euler} + \Delta h_{imp.ext}$$

Energy Balance (other elements)

$$h_{0.out.s} = h_{0.in} - \Delta h_{element}$$

$$h_{0.out} = h_{0.in}$$

Entropy Balance (all elements)

$$s_{in} = f(P_{in}, T_{in})$$

$$s_{out.s} = s_{in}$$

$$P_{0.out} = f(h_{0.out.s}, s_{out.s})$$

$$T_{0.out} = f(h_{0.out}, P_{0.out})$$

Real gas fluid property relationships

$$h_0 = h + \frac{1}{2}c^2$$

$$h, \rho, \nu, ss = f(P, T)$$

Work and efficiency definitions

$$w_{c.s} = h_{0.0} - h_{0.5.ss}$$

$$w_c = h_{0.0} - h_{0.5}$$

$$\eta_{TS} = \frac{h_{0.0} - h_{5.ss}}{w_c}$$

$$\eta_{TT} = \frac{w_{c.s}}{w_c}$$

| | Loss/ Model | Source |
|-----------------|--|---|
| | Inlet guide vanes | (Galvas, 1973) |
| Internal losses | Skin friction | Jansen (as cited by Ameli et al., 2018; Harrison, 2020) |
| | Impeller blade loading | (Aungier, 1995) |
| | Hub to shroud (for shrouded impellers) | (Aungier, 1995) |
| | Mixing | (Aungier, 1995) |
| | Clearance (for unshrouded impellers) | Jansen (as cited by Zhang et al., 2019) |
| | Incidence | (Aungier, 2000) |
| | Entrance diffusion | (Aungier, 1995) |
| | Choke | (Aungier, 1995) |
| | Shock | (Aungier, 1995) |
| External losses | Disk friction | Daily & Nece (as cited by Zhang et al., 2019) |
| | Recirculation | Coppage & Dallenbach (as cited by Zhang et al., 2019) |
| | Leakage (for unshrouded impellers) | (Aungier, 1995) |
| | Vaneless space (friction) | Based on Jansen (as cited by Ameli et al., 2018) |
| | Vaned diffuser (incidence) | Aungier (as cited by Zhang et al., 2019) |
| | Vaned diffuser (friction) | Based on Jansen (as cited by Ameli et al., 2018) |
| | Volute pressure recovery | Japikse & Baines (1997) |
| | Slip factor | Wiesner (1967) |



- Steady state cycle study:
 - du Sart, C.F., Rousseau, P. & Laubscher, R. 2024. Comparing the partial cooling and recompression cycles for a 50 MWe sCO₂ CSP plant using detailed recuperator models. Renewable Energy. DOI: 10.1016/j.renene.2024.119980.
- Solar field and receiver studies:
 - Heydenrych, J.M., Rousseau, P.G. & du Sart, C.F. 2022. Reduced-order modelling of central solar tower receivers using an equivalent thermal resistance network. In Proceedings of the 16th international conference on heat transfer, fluid mechanics and thermodynamics (HEFAT-16). Virtual: HEFAT. 911–916. Available: <https://www.researchgate.net/publication/363173202>.
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- Heat rejection system study:
 - Abrahams, L., du Sart, C. & Laubscher, R. 2022. Design of an air-cooled heat rejection system for a sCO₂ concentrated solar power plant. In 16th international conference on heat transfer, fluid mechanics and thermodynamics (HEFAT-16). Virtual: HEFAT. 288–293. Available: <https://www.researchgate.net/publication/363173234>.
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