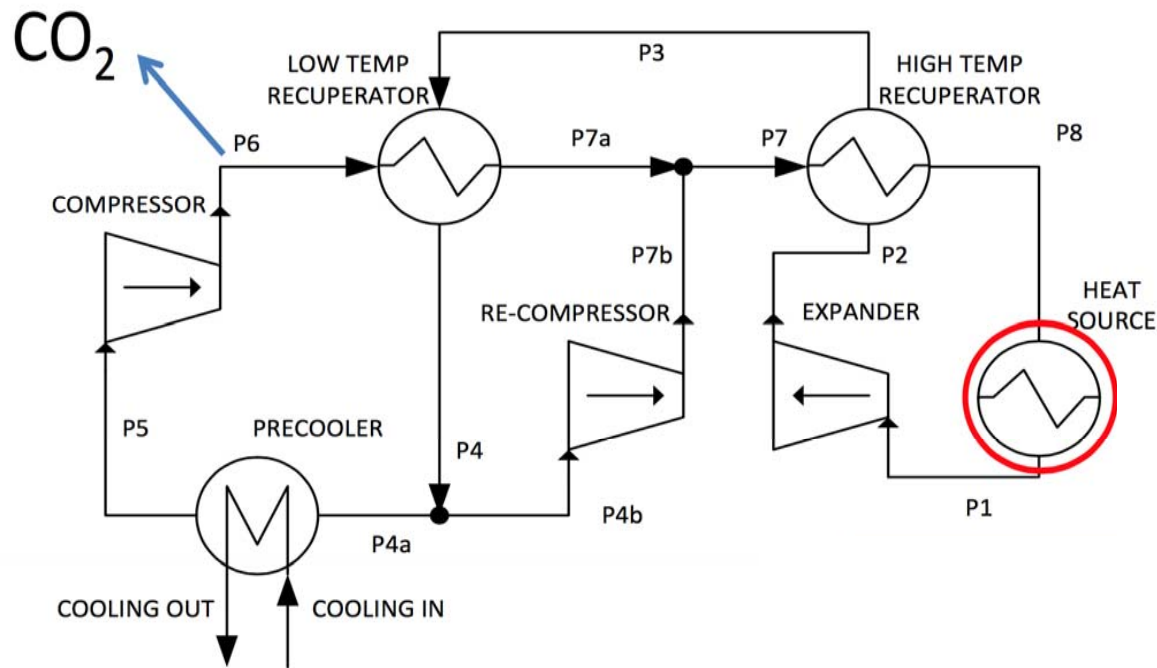


Large eddy simulations of oxy-fuel combustors for direct-fired supercritical CO₂ power cycles

Daniel T. Banuti, Lee Shunn, Sanjeeb Bose, Dokyun Kim



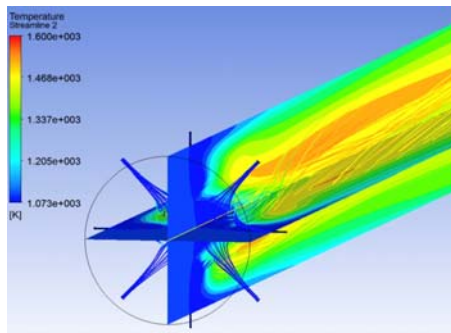
Direct-fired sCO₂ cycle - Allam cycle



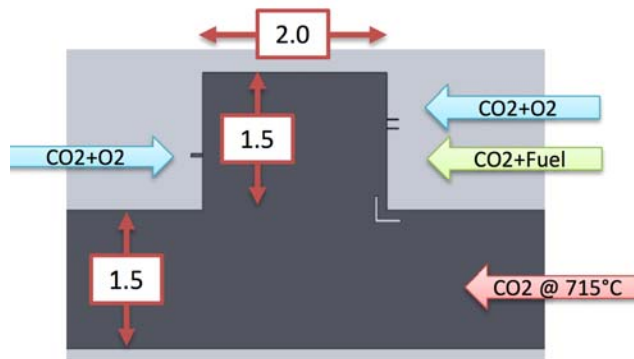
Delimont 2017

- Closed sCO₂ loop
- Increased efficiency
- Small footprint
- Heat added by direct combustion (e.g. CH₄+O₂)
- Ideally, products in stoichiometric combustion (H₂O, CO₂) can be easily removed

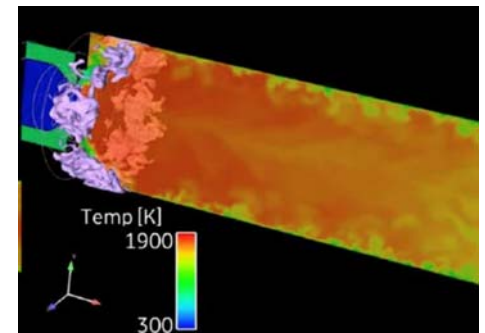
Problem: how *exactly* do we add heat?



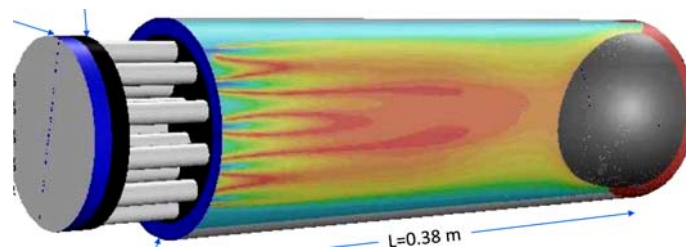
Radial jets in crossflow
(Delimont et al. UTSR 2016)



Trapped vortex chamber
(Delimont et al. UTSR 2017)

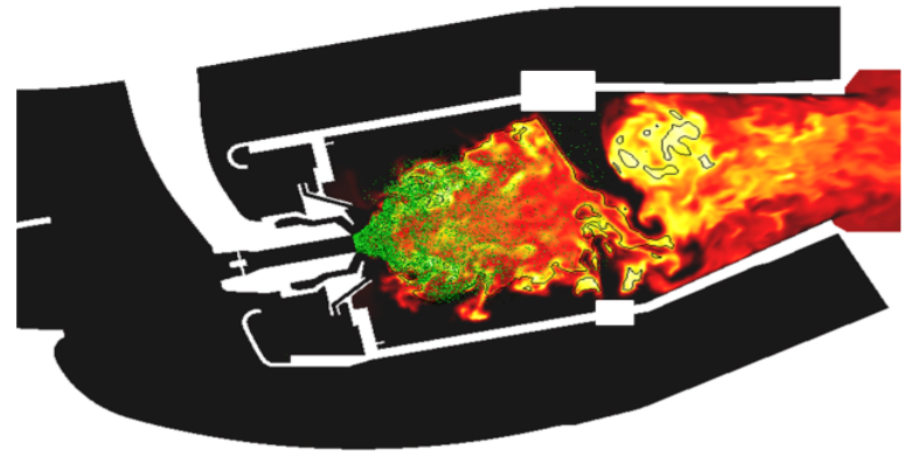
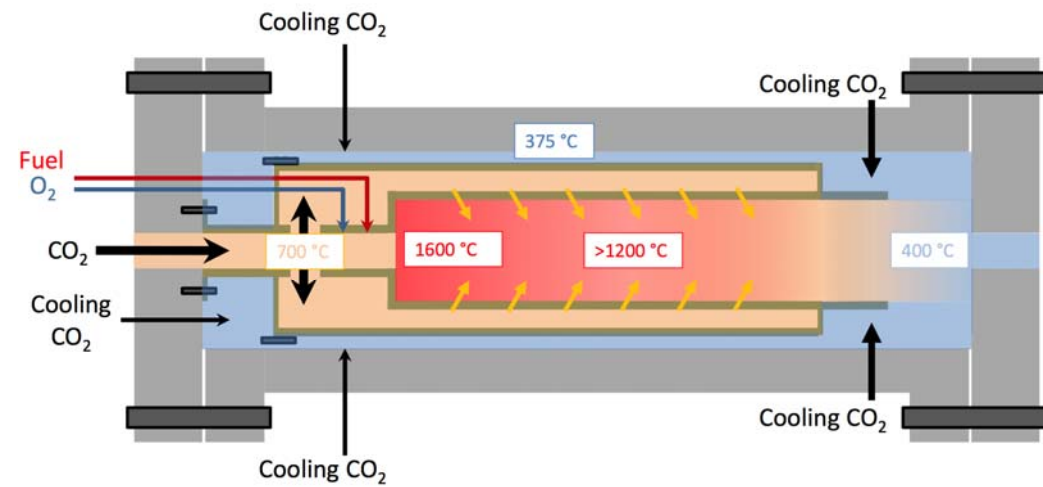


Swirl injector in liner
(Delimont et al. UTSR 2017)



Coaxial injectors
(Strakey UTSR 2017)

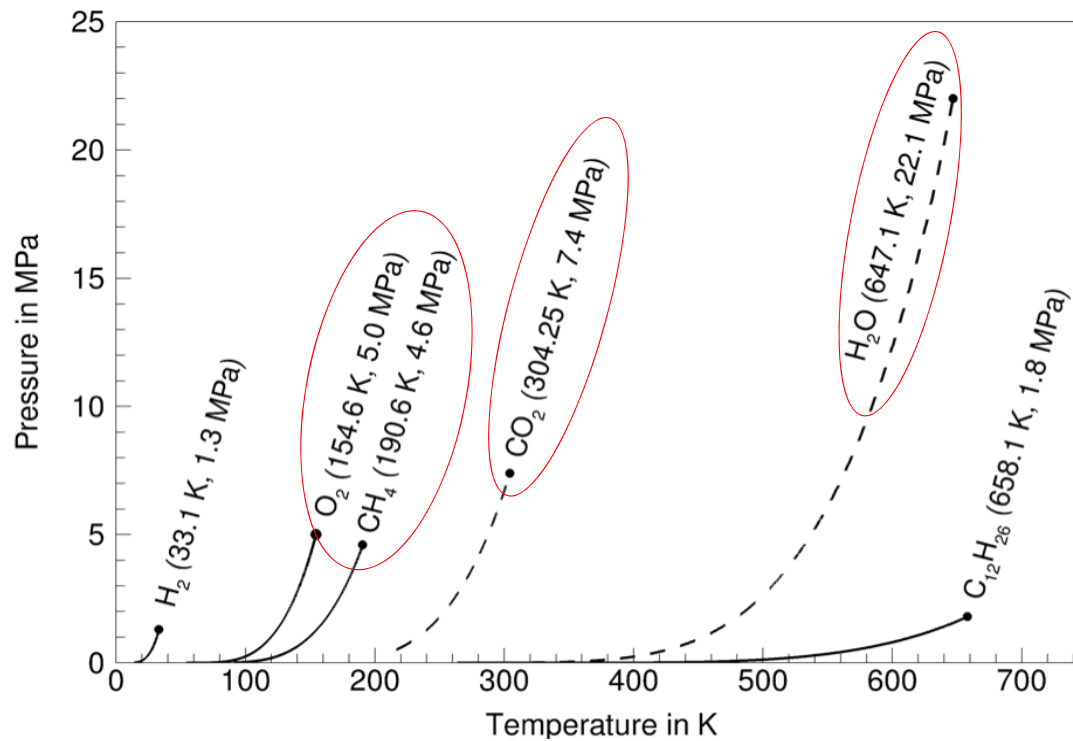
Combustor concept from SwRI



Component	Mass flow in kg/s
CH ₄	0.02
O ₂	0.08
CO ₂ combustor	0.626
CO ₂ bypass	0.899
Total	1.625

$p > 200 \text{ bar}$

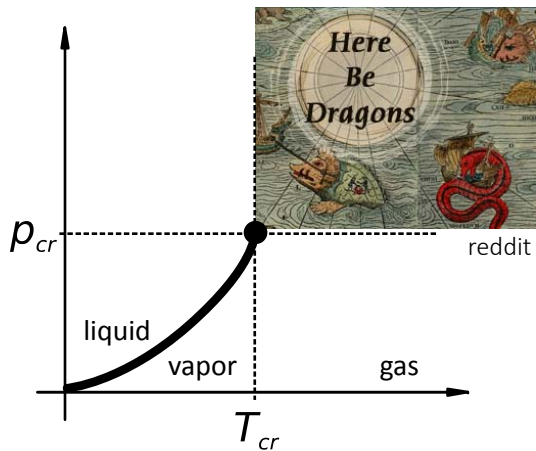
Thermophysical Properties at High Pressures



- Anticipated combustor conditions:
 - $T = 1000\text{-}2000\text{K}$,
 - $p = 200\text{-}300\text{ bar}$
- Mixtures are supercritical with respect to:
 CH_4, O_2, CO_2, H_2O

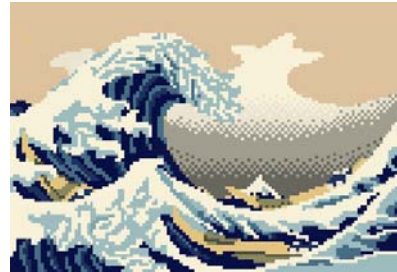
Objectives

What is 'supercritical' anyway?



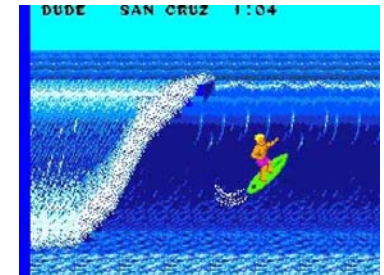
reddit

Identify and analyze model



reddit

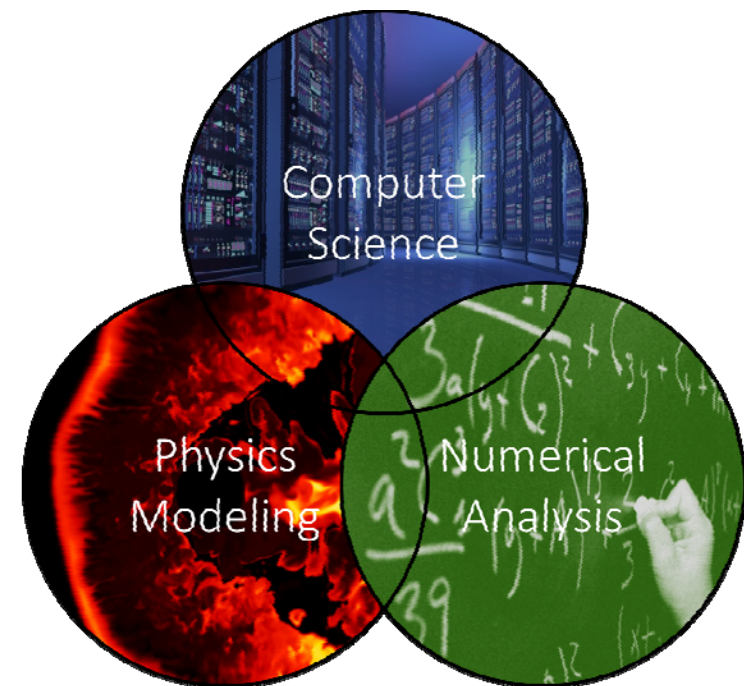
Perform simulations



california games

Cascade Background

- Founded in 1997 to support technology transfer from Stanford University's Center for Turbulence Research to industry
- Located in Palo Alto, CA
- Since 2007, Cascade has developed and licensed [multi-physics Large Eddy Simulation \(LES\) tools](#) tailored for high-performance and extreme scalability
- Cascade's LES software is developed and supported by a growing team of full-time professionals with expertise in [physics modeling](#), [computer science](#), and [numerical analysis](#)

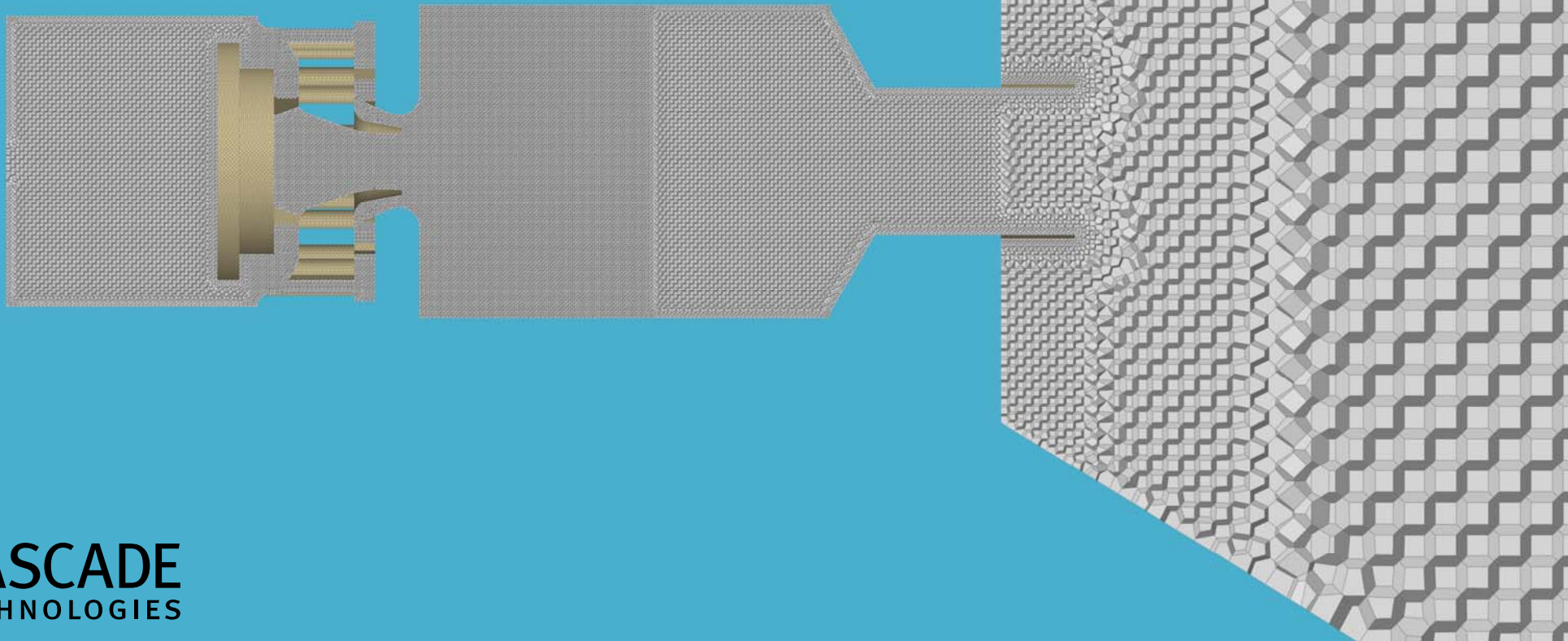


CHARLES™ suite of LES tools

Developed and licensed by Cascade Technologies

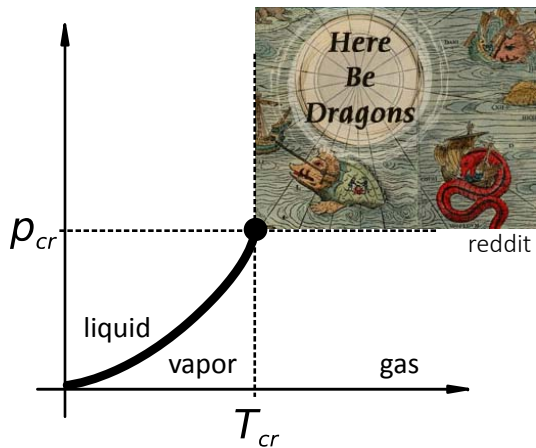
- Compressible FV Navier-Stokes formulation
- Flamelet/progress-variable combustion models
- Massively-parallel communication and I/O
- Numerical method
 - 2nd-order low-dissipation gradient operators
 - 3rd-order explicit time advancement
 - ‘KEEP’ entropy-stable flux discretization

High-quality unstructured meshes with boundary-aligned cells



Objectives

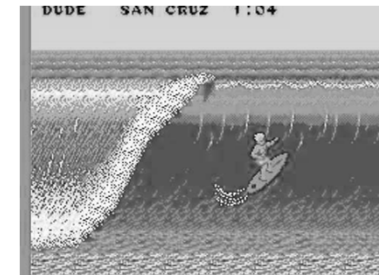
What is 'supercritical' anyway?



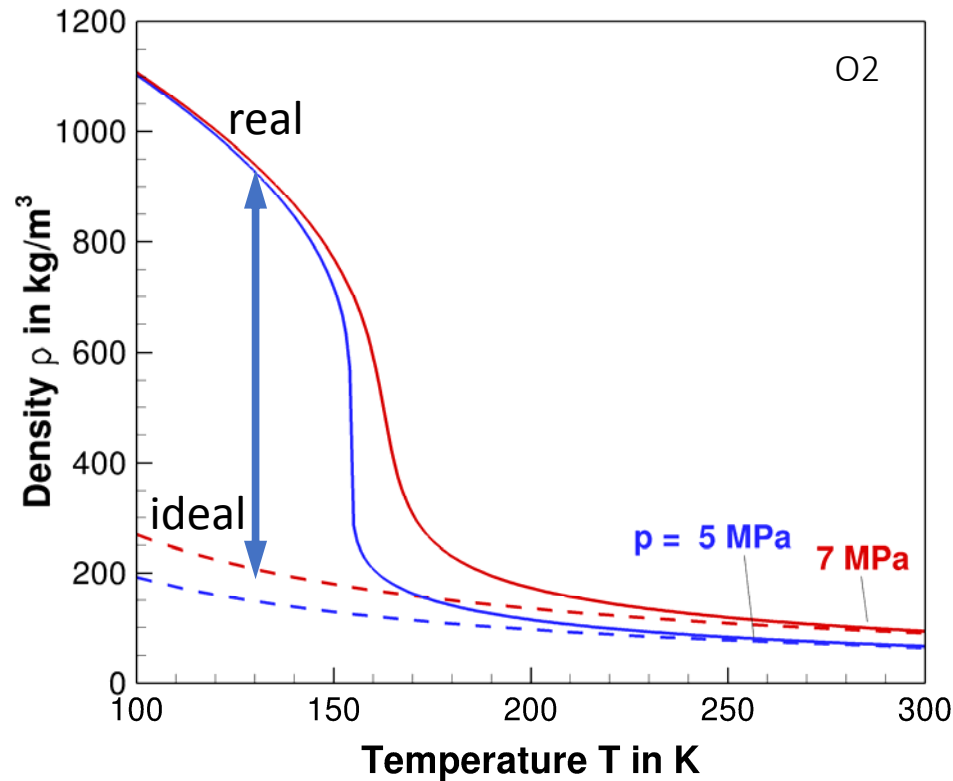
Identify and analyze model



Perform simulations



What is the difference between real and ideal gases?

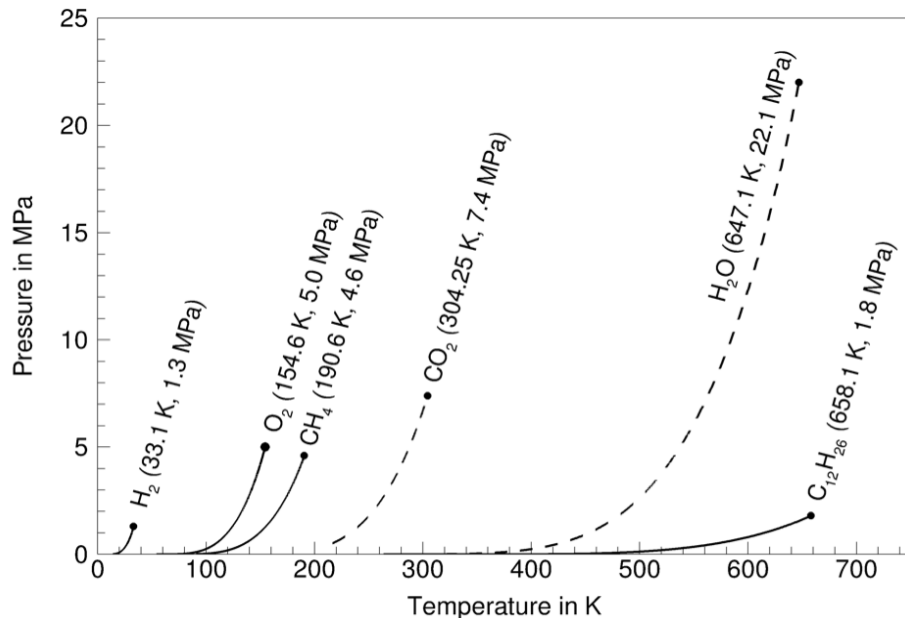


$$p = \frac{RT}{v - b} - \frac{a}{v^2}$$

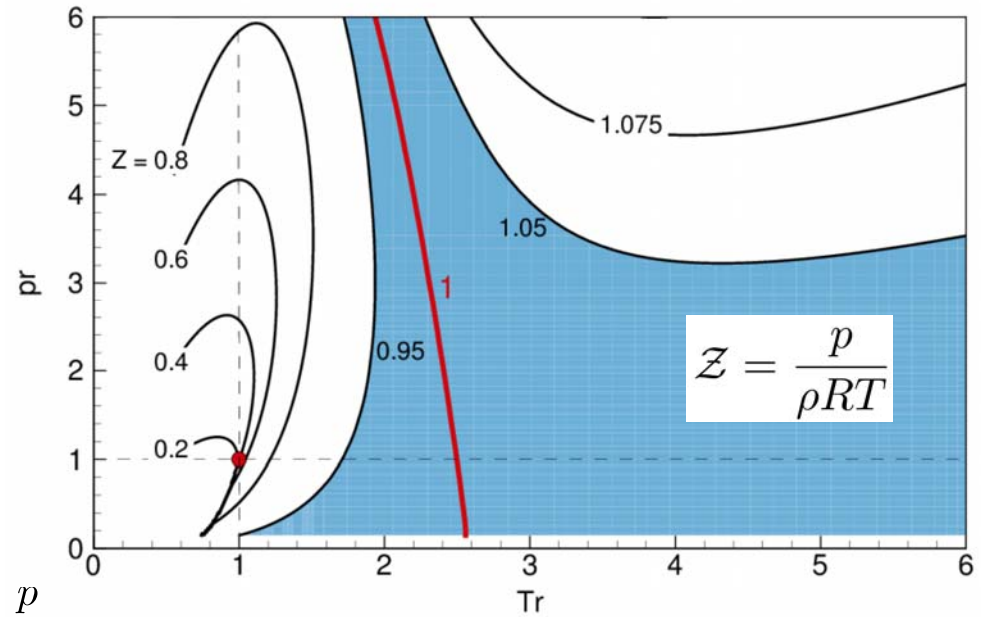
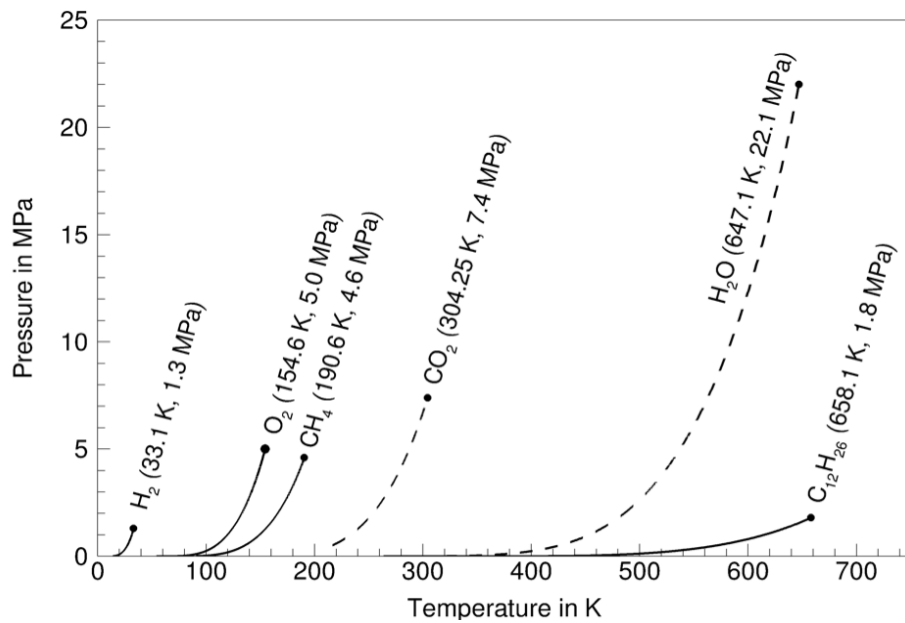
Annotations for the equation:

- Arrows point from the text "molecular volume" to the term $v - b$.
- Arrows point from the text "intermolecular attraction" to the term $\frac{a}{v^2}$.

The supercritical state space



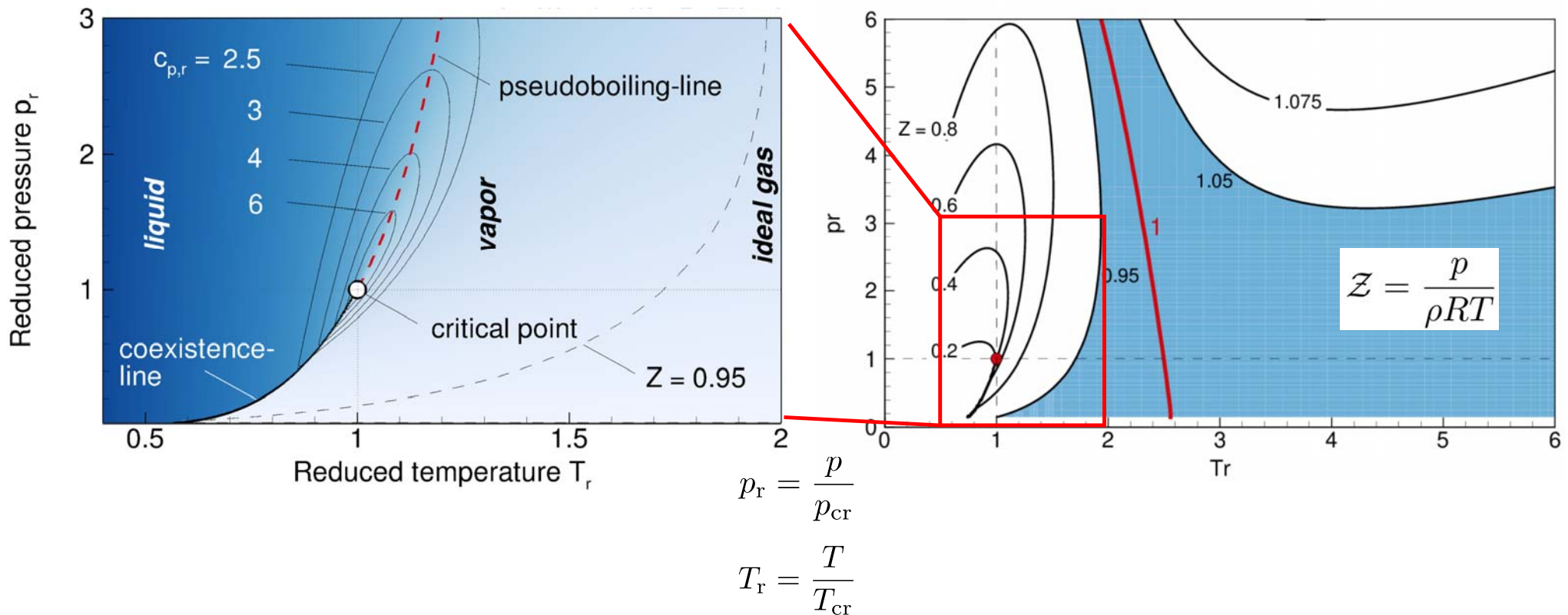
The supercritical state space



$$p_r = \frac{p}{p_{cr}}$$

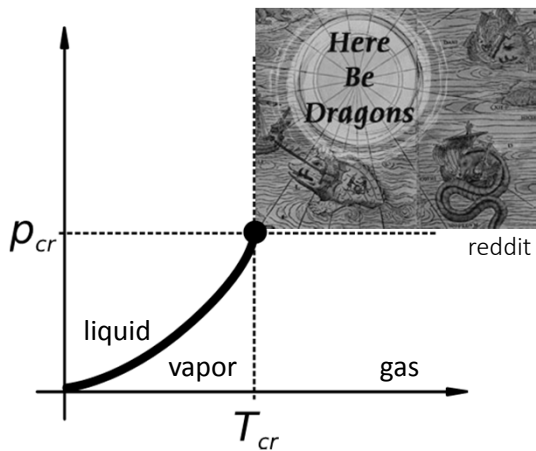
$$T_r = \frac{T}{T_{cr}}$$

The supercritical state space

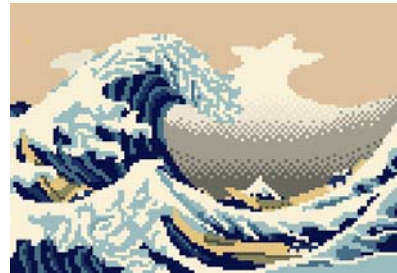


Objectives

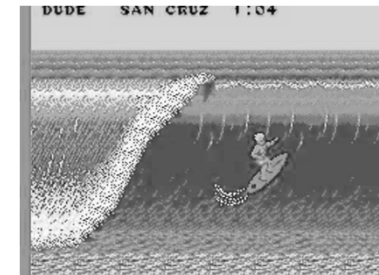
What is 'supercritical' anyway?



Identify and analyze model



Perform simulations



Real fluid thermodynamics for mixtures

Peng-Robinson equation of state:

$$p = \frac{RT}{v - b} - \frac{a}{v^2 + 2bv - b^2}$$

$$a = 0.457236 \frac{(RT_{cr})^2}{p_{cr}} \left[1 + m(1 - \sqrt{T_r}) \right]^2$$

$$m = 0.3746 + 1.54226\omega - 0.26992\omega^2$$

$$b = 0.077796 \frac{RT_{cr}}{p_{cr}}$$

One fluid mixing model

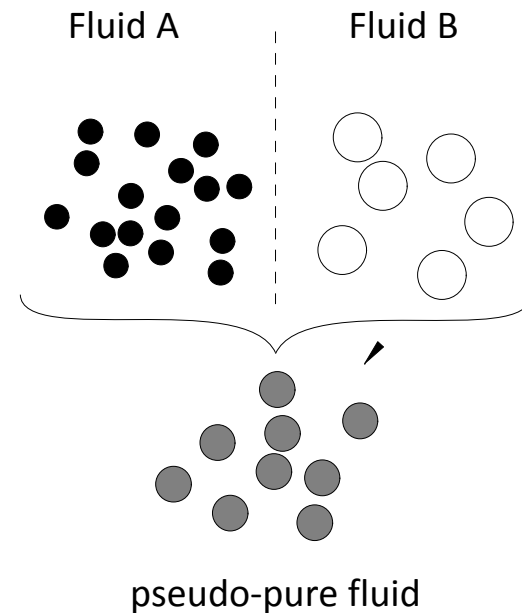
Peng-Robinson equation of state:

$$p = \frac{RT}{v - b} - \frac{a}{v^2 + 2bv - b^2}$$

$$a = 0.457236 \frac{(RT_{cr})^2}{p_{cr}} \left[1 + m(1 - \sqrt{T_r}) \right]^2$$

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$$b = 0.077796 \frac{RT_{cr}}{p_{cr}}$$



Oefelein and Yang (1998)

One fluid mixing model

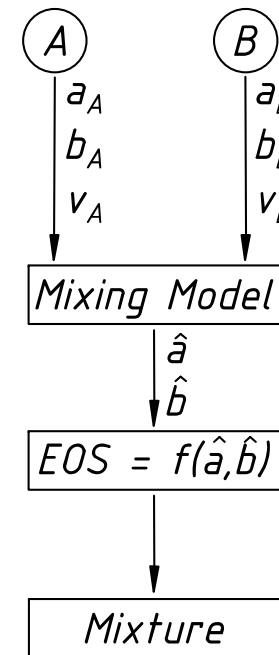
Peng-Robinson equation of state:

$$p = \frac{RT}{v - b} - \frac{a}{v^2 + 2bv - b^2}$$

$$a = 0.457236 \frac{(RT_{cr})^2}{p_{cr}} \left[1 + m(1 - \sqrt{T_r}) \right]^2$$

$$m = 0.3746 + 1.54226\omega - 0.26992\omega^2$$

$$b = 0.077796 \frac{RT_{cr}}{p_{cr}}$$



Oefelein and Yang (1998)

One fluid mixing model - two approaches

Peng-Robinson equation of state:

$$p = \frac{RT}{v - b} - \frac{a}{v^2 + 2bv - b^2}$$

$$a = 0.457236 \frac{(RT_{cr})^2}{p_{cr}} \left[1 + m(1 - \sqrt{T_r}) \right]^2$$

$$m = 0.3746 + 1.54226\omega - 0.26992\omega^2$$

$$b = 0.077796 \frac{RT_{cr}}{p_{cr}}$$

Oefelein and Yang (1998)

Mixing rules

van der Waals

$$a = \sum_{i=1}^N \sum_{j=1}^N y_i y_j \sqrt{a_i a_j} (1 - k_{i,j})$$

$$b = \sum_{i=1}^N y_i b_i$$

$$\omega = \sum_{i=1}^N y_i \omega_i$$

pseudocritical point

$$T_{cr,i,j} = (T_{cr,i} \cdot T_{cr,j})^{1/2},$$

$$v_{cr,i,j} = \left(\frac{1}{2} (v_{cr,i}^{1/3} + v_{cr,j}^{1/3}) \right)^3,$$

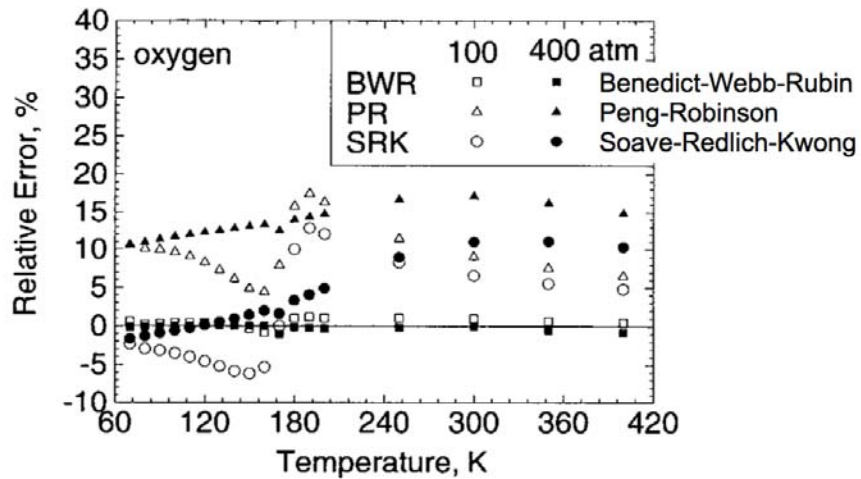
$$Z_{cr,i,j} = \frac{1}{2} (Z_{cr,i} + Z_{cr,j}),$$

$$p_{cr,i,j} = \frac{Z_{cr,i,j} RT_{cr,i,j}}{v_{cr,i,j}},$$

$$\omega_{i,j} = \frac{1}{2} (\omega_i + \omega_j).$$

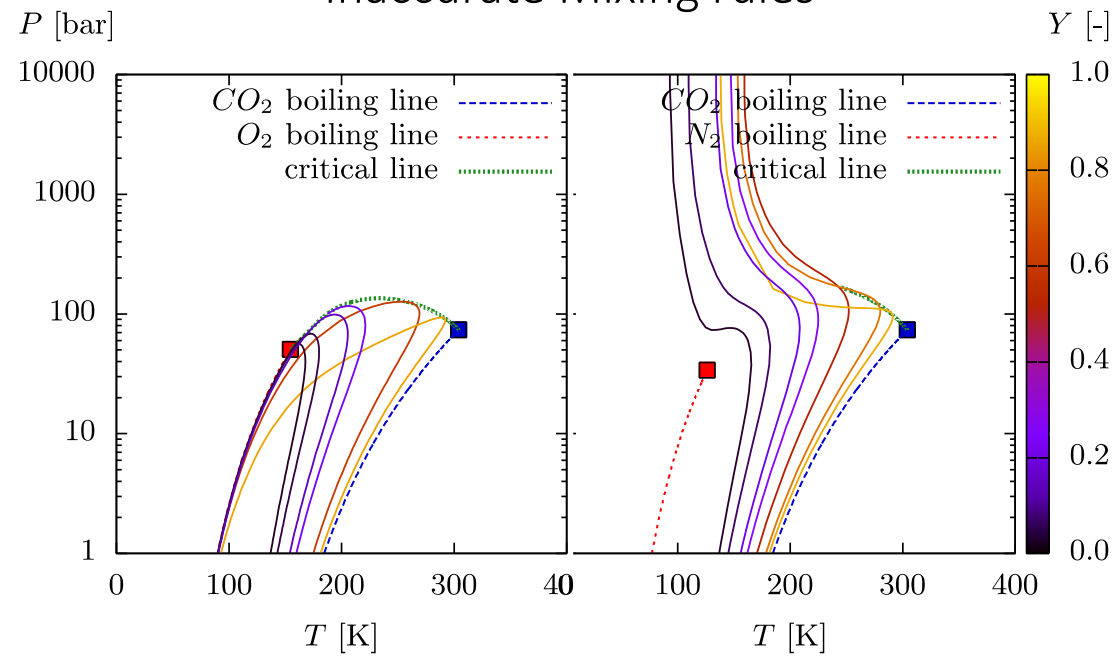
Main Deficiencies

Inaccurate EOS



Yang 2000

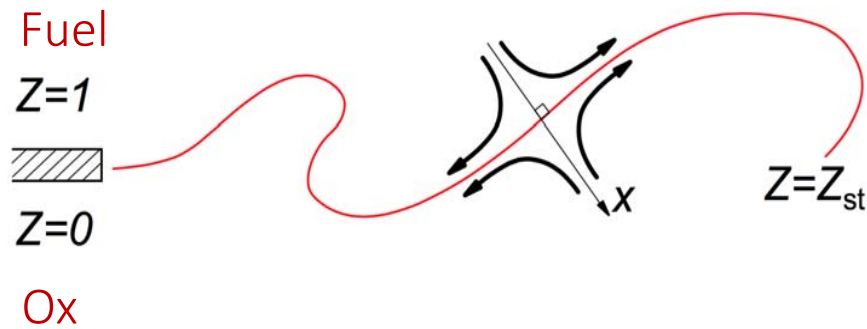
Inaccurate Mixing rules



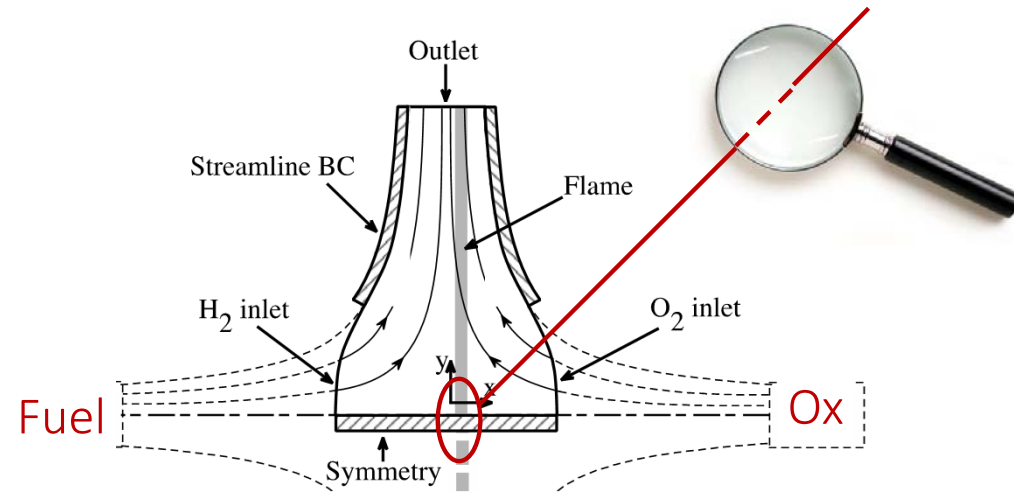
vdW mixing rules always assume Type I mixture

Not applicable for many technical mixtures

1D flame representation - flamelet



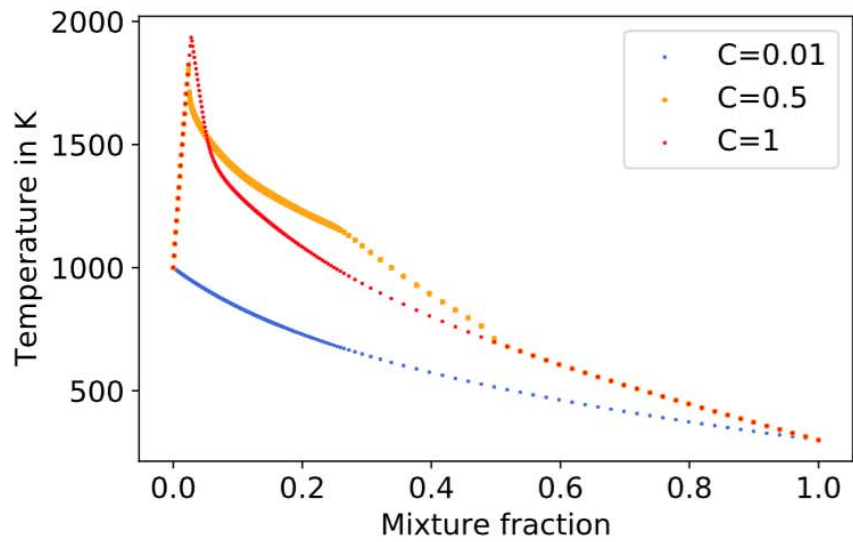
'Mixture fraction' as variable transformation



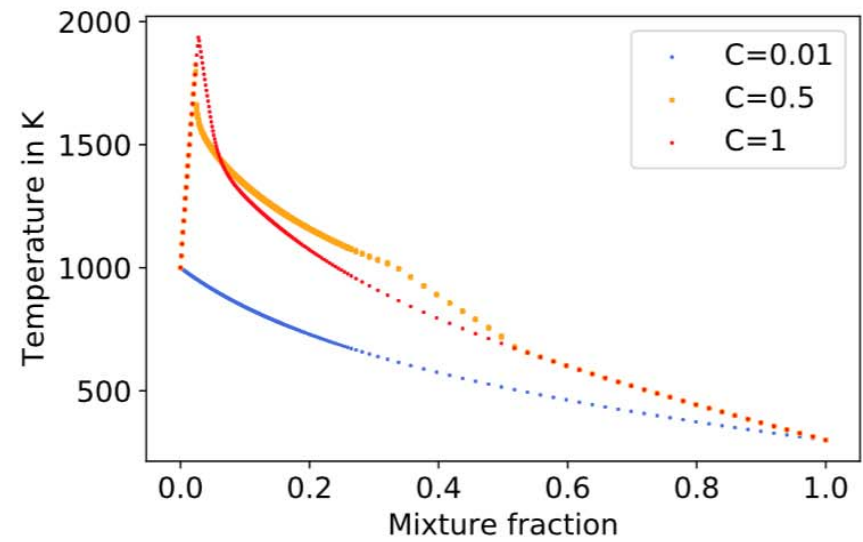
Lacaze & Oefelein CnF 2012

1D flame profiles

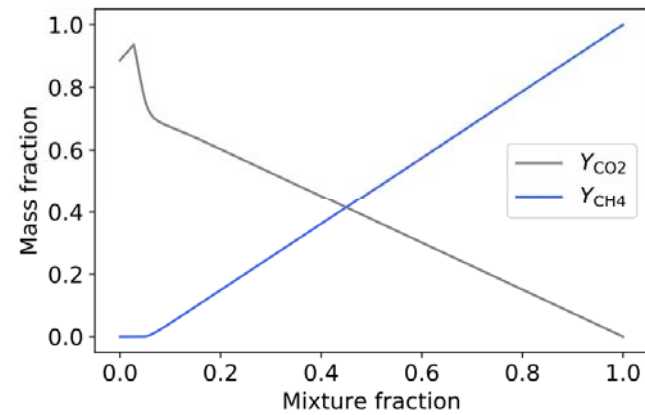
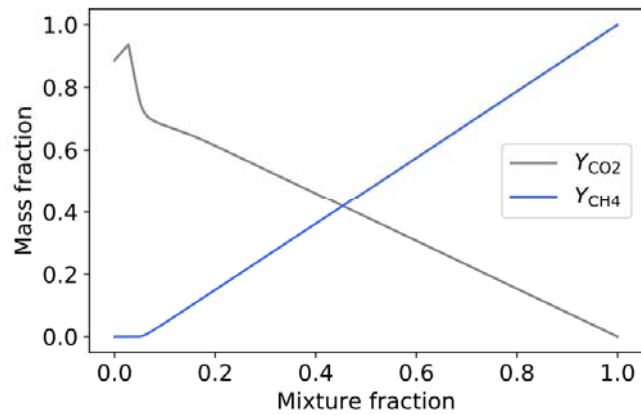
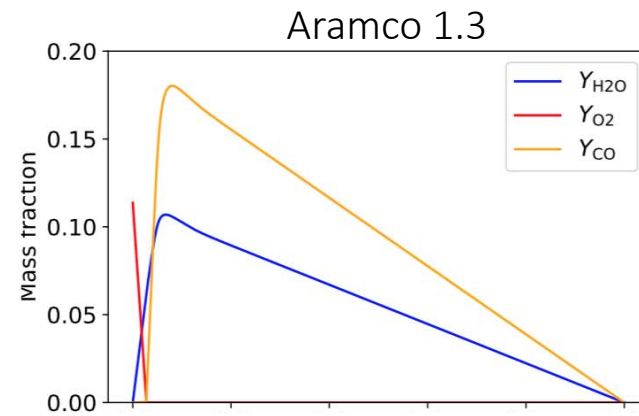
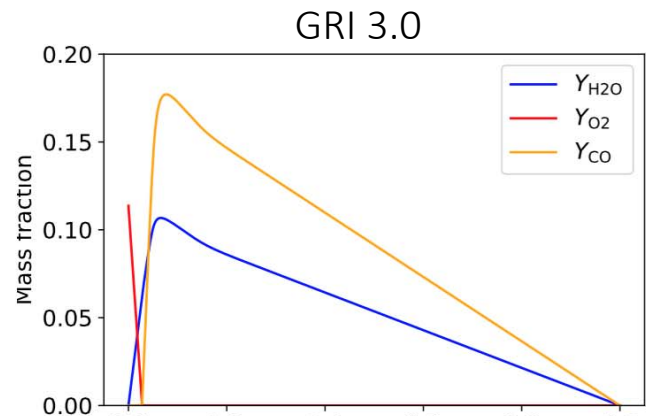
GRI 3.0



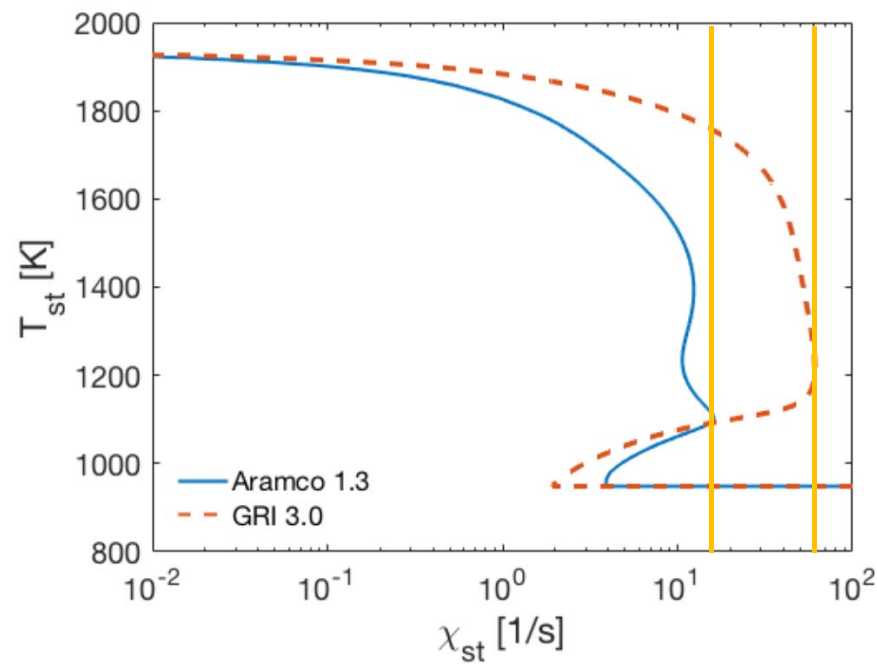
Aramco 1.3



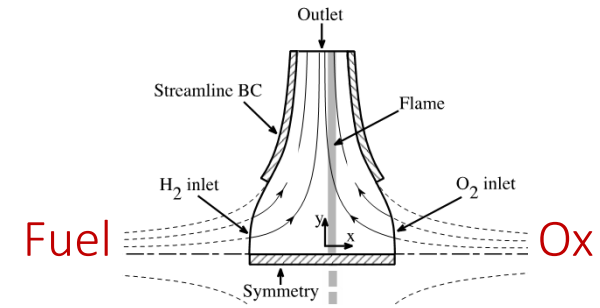
Species distributions



Main differences between mechanisms



Significant discrepancy
in maximum strain rate
introduced uncertainty
for injector studies



Flame thickness

- Decreases with pressure
- Deviation between models for pressures > 10 bar

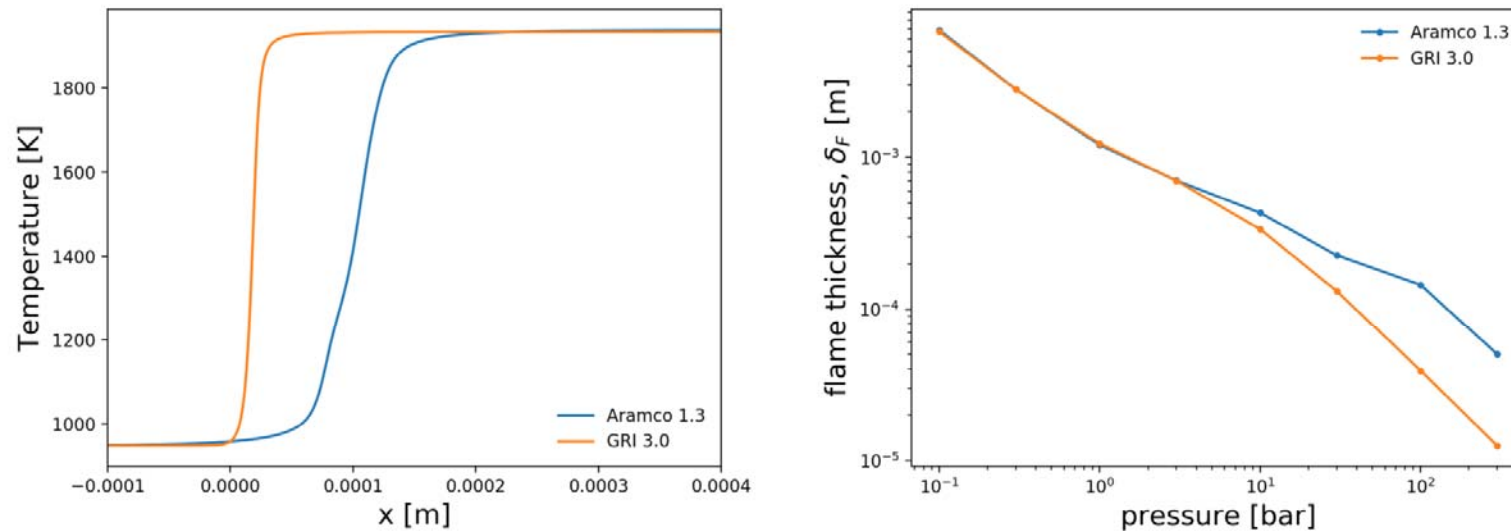
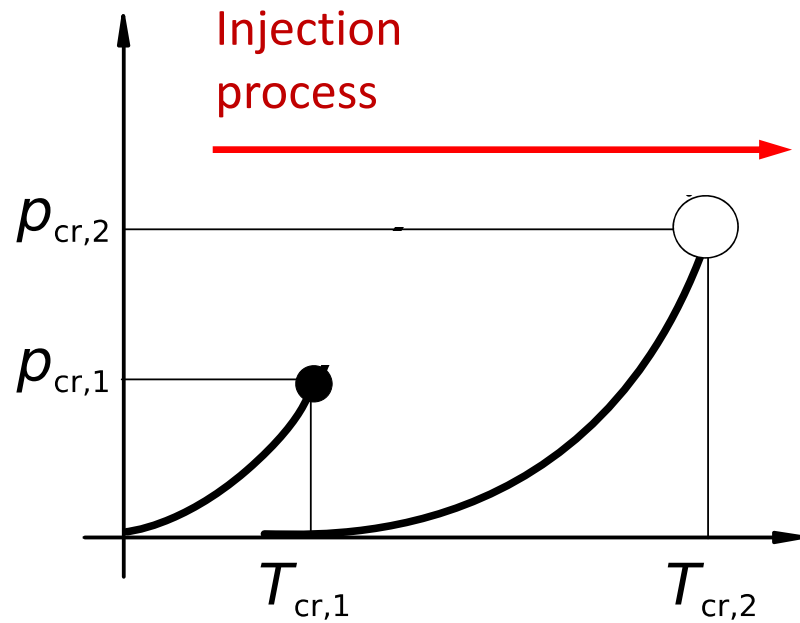


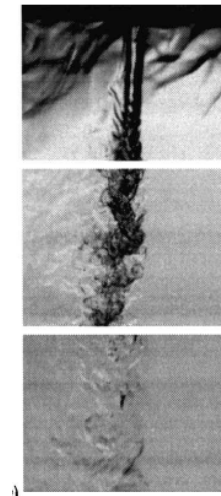
Figure 11: Laminar premixed flames in a stoichiometric mixture of $\text{CH}_4\text{-O}_2\text{-CO}_2$ using two different kinetic mechanisms. (left) Flame structure at 300 bar and (right) laminar flame thickness, δ_F , versus pressure.

Assess relevance of real fluid effects



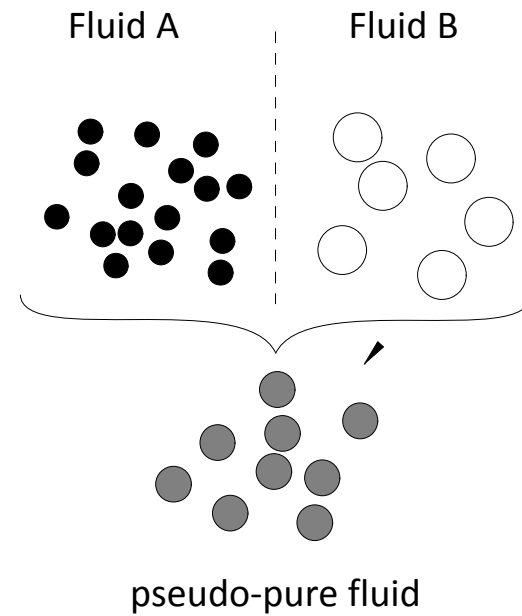
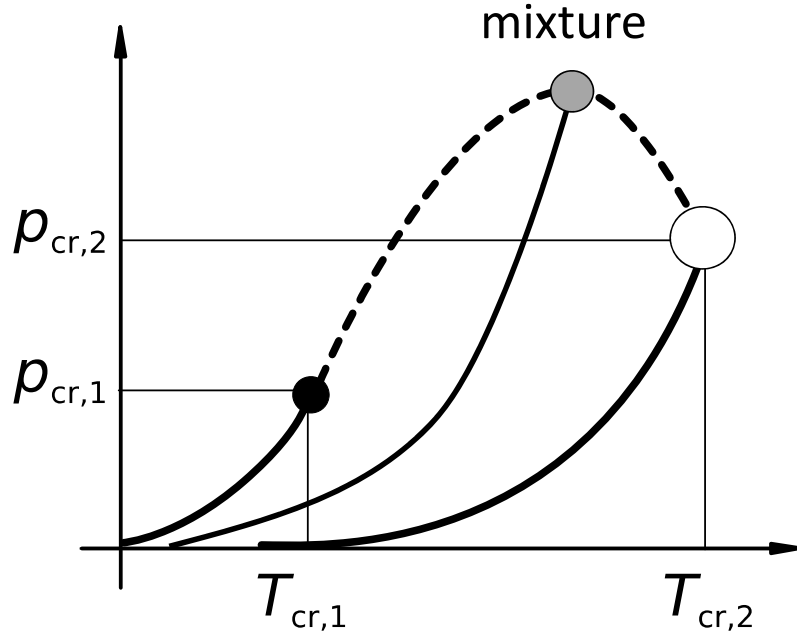
Nitrogen into

N₂

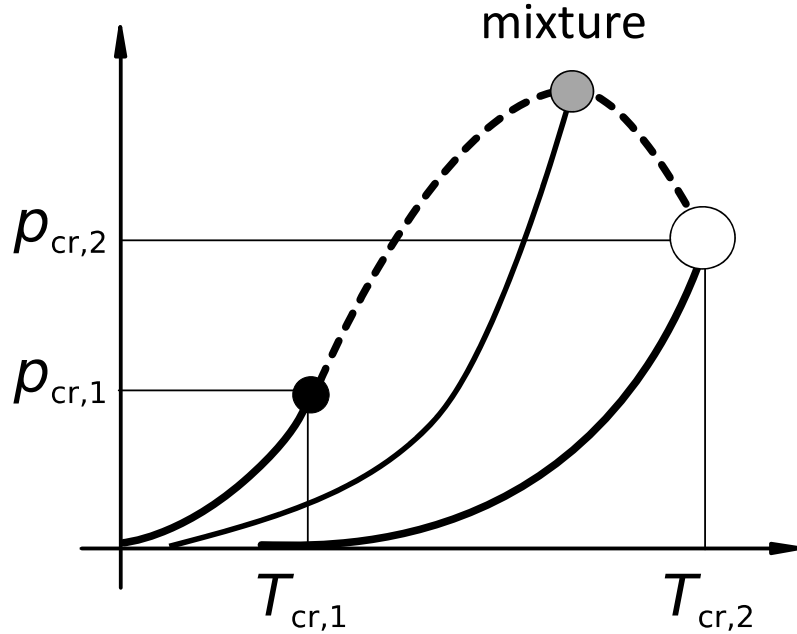


Mayer et al.
(1998)

Assess relevance of real fluid effects



Assess relevance of real fluid effects

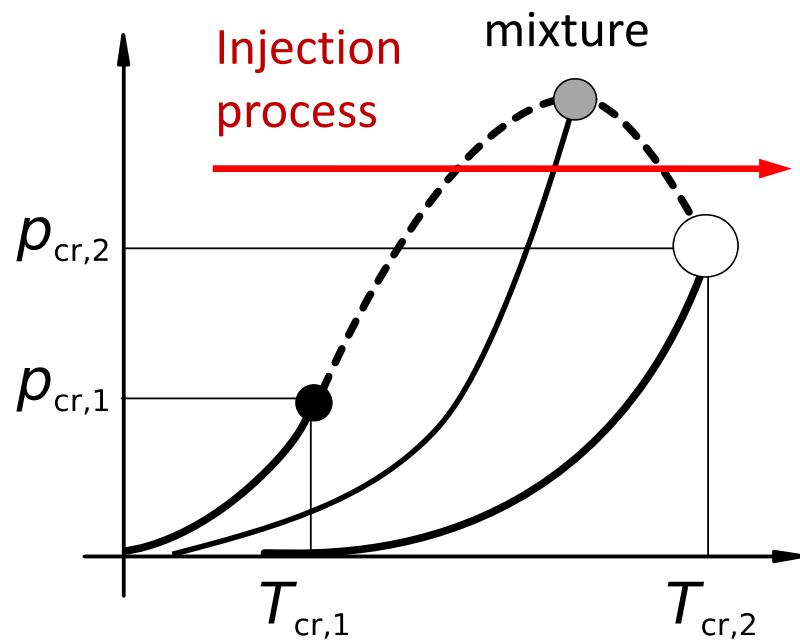


Reid et al. 1987

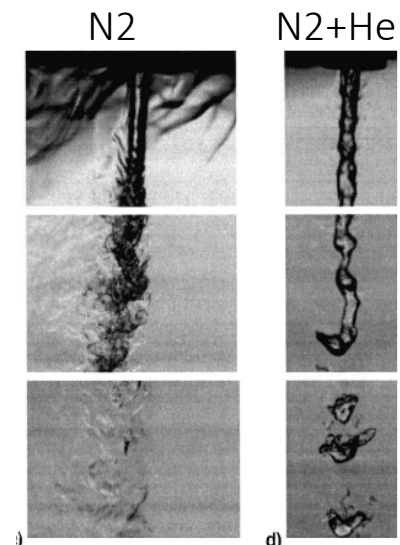
$$T_{\text{mix,cr}} = \sum_{\alpha=1}^{N_S} X_{\alpha} T_{\alpha,\text{cr}},$$

$$p_{\text{mix,cr}} = \frac{RT_{\text{mix,cr}} \sum_{\alpha=1}^{N_S} X_{\alpha} Z_{\alpha,\text{cr}}}{\sum_{\alpha=1}^{N_S} X_{\alpha} v_{\alpha,\text{cr}}}.$$

Assess relevance of real fluid effects

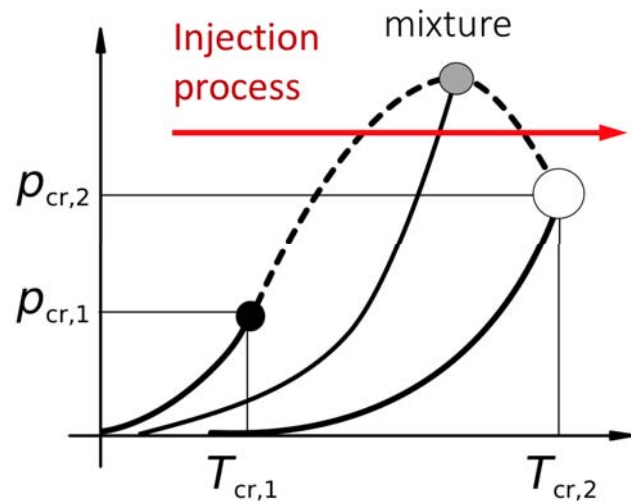


Nitrogen into

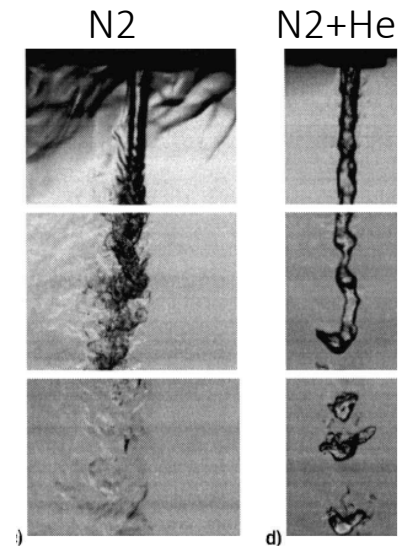


Mayer et al.
(1998)

Assess relevance of real fluid effects

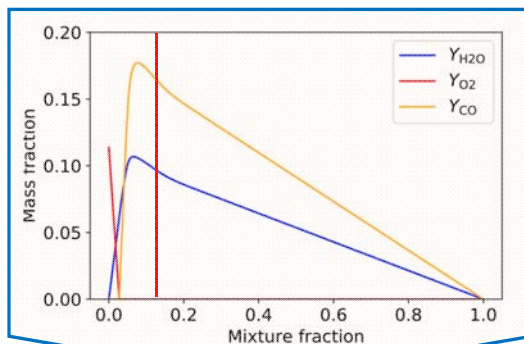


Nitrogen into



Mayer et al.
(1998)

Thermodynamic flame trajectory

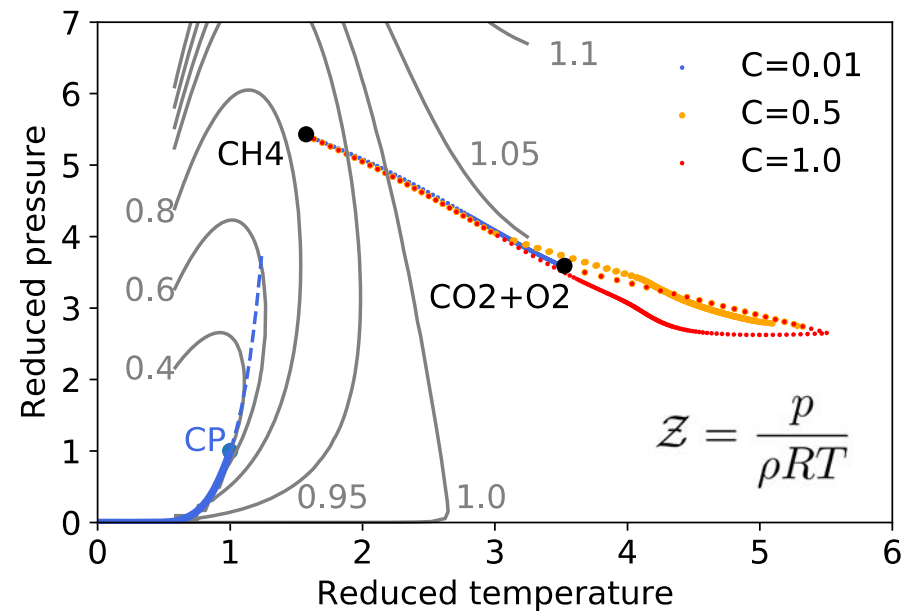


$$T_{\text{mix,cr}} = \sum_{\alpha=1}^{N_S} X_{\alpha} T_{\alpha,\text{cr}},$$

$$p_{\text{mix,cr}} = \frac{RT_{\text{mix,cr}} \sum_{\alpha=1}^{N_S} X_{\alpha} Z_{\alpha,\text{cr}}}{\sum_{\alpha=1}^{N_S} X_{\alpha} v_{\alpha,\text{cr}}},$$

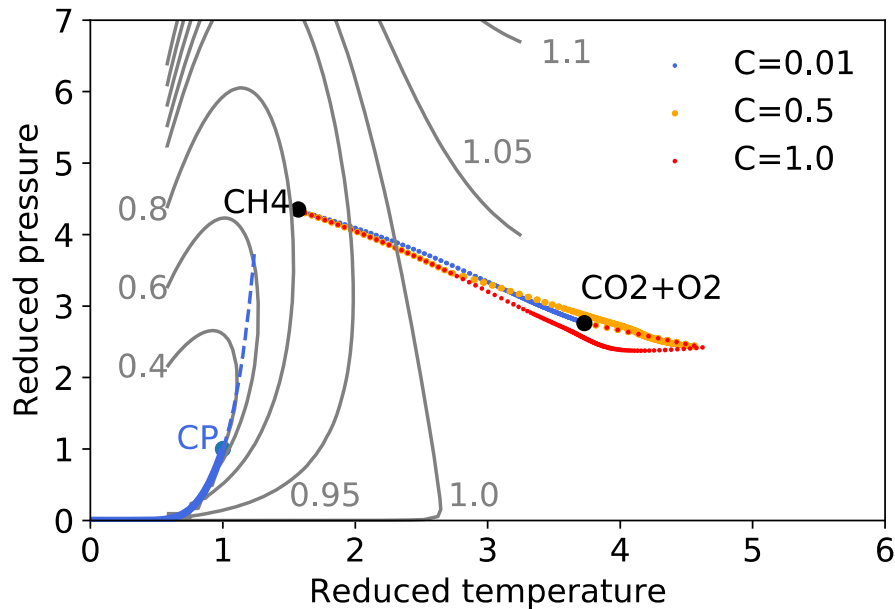
$$p_r = \frac{p}{p_{\text{cr}}} \quad T_r = \frac{T}{T_{\text{cr}}}$$

Banuti et al. AIAA 2016-4789



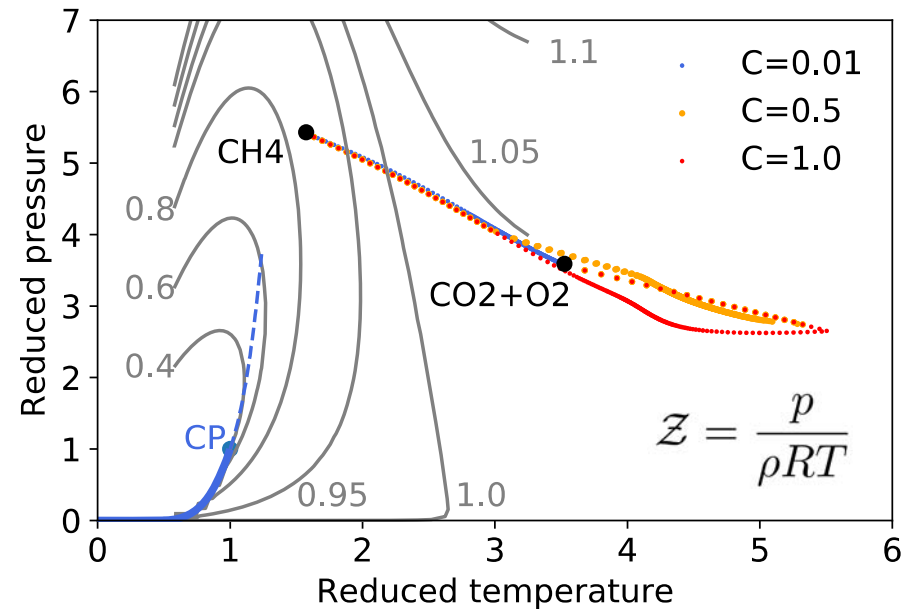
Parameters	CH ₄	O ₂	H ₂ O	CO ₂	CO
T_{cr} [K]	190.6	154.58	647.10	304.2	132.9
p_{cr} [MPa]	4.604	5.043	22.064	7.382	3.499
Z_{cr} [-]	0.288	0.288	0.233	0.274	0.295
v_{cr} [cm ³ /mol]	98.62	73.37	55.95	94.12	92.165

Impact of operating conditions



$p = 20 \text{ MPa}$
 $T_{Fu} = 300\text{K}$
 $T_{Ox} = 1100\text{K}$
 $Y_{O_2} = 0.05$
 $Y_{CO_2} = 0.95$

Chong et al.
 AIAA 2017-0141

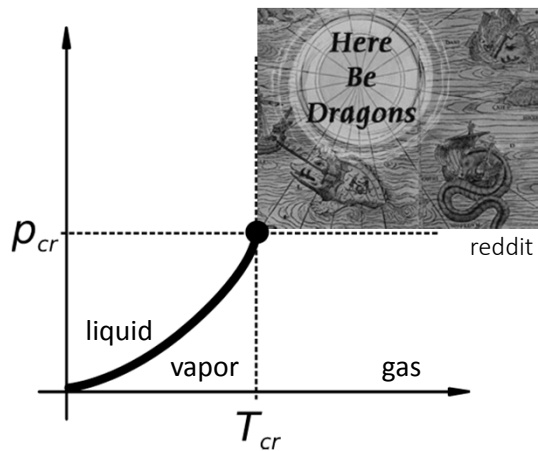


$p = 25 \text{ MPa}$
 $T_{Fu} = 300\text{K}$
 $T_{Ox} = 1000\text{K}$
 $X_{O_2} = 0.15$
 $X_{CO_2} = 0.85$

~Delimont UTSR 2017

Objectives

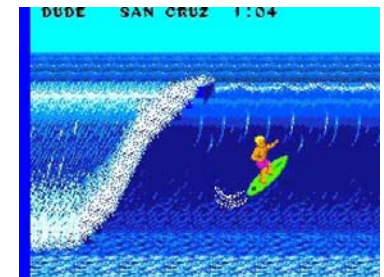
What is 'supercritical' anyway?



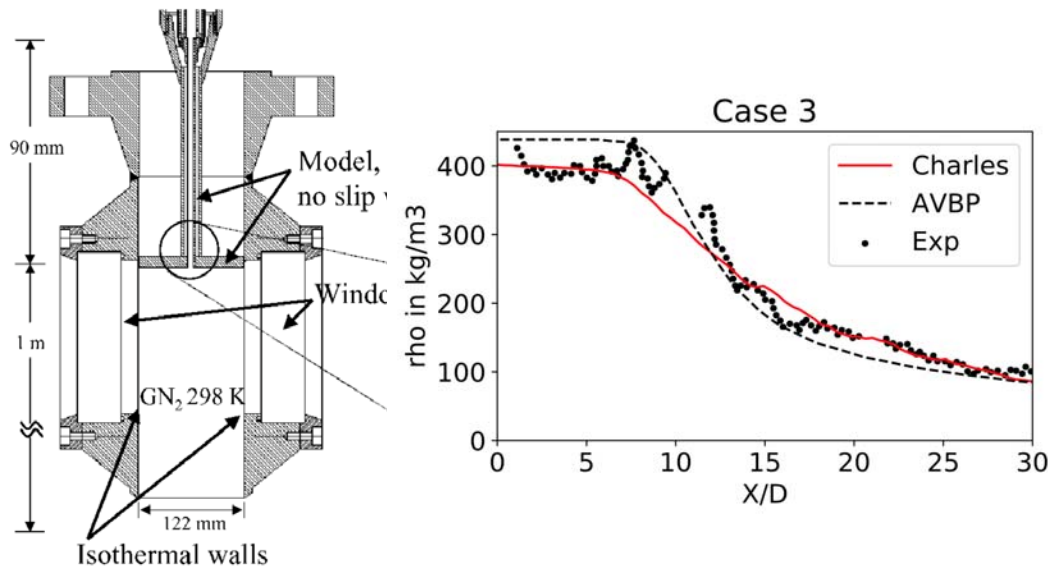
Identify and analyze model



Perform simulations!

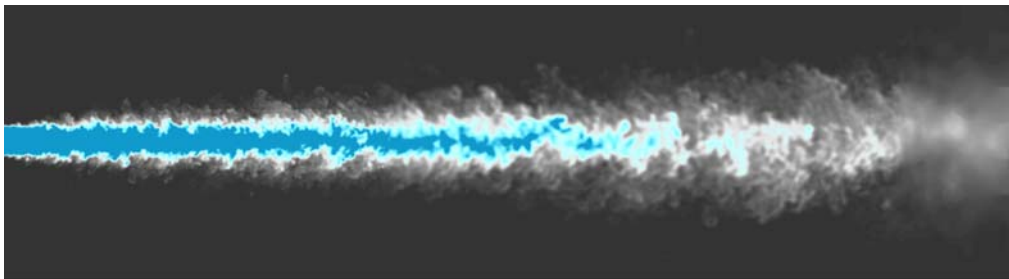


Transcritical nitrogen injection

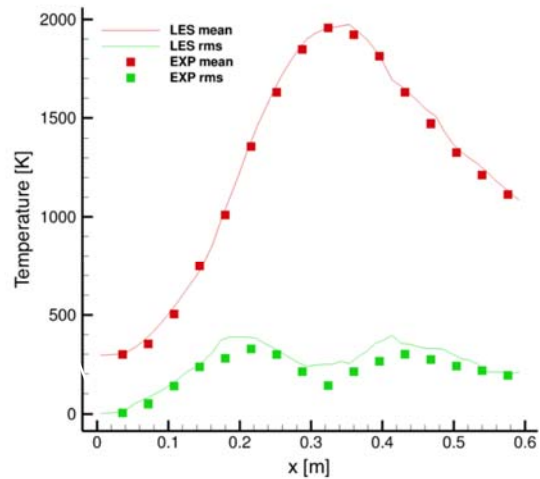


Pure real fluid injection

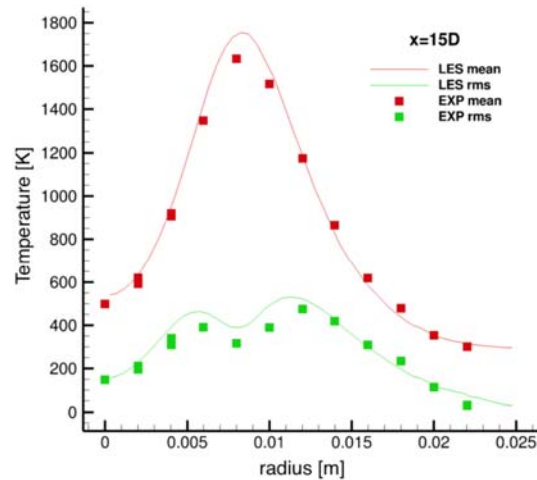
- Mayer & Branam 2003
- Test EOS implementation
- Test real fluid dynamics & numerics
- No mixture models
- Agreement very good



Sandia Flame D



(a) centerline temperature



(b) radial temperature at $x/D = 15$



Reactive mixture

- Barlow et al. 2005
- Multispecies transport
- Partially premixed
- Flamelet progress variable approach
- Agreement very good

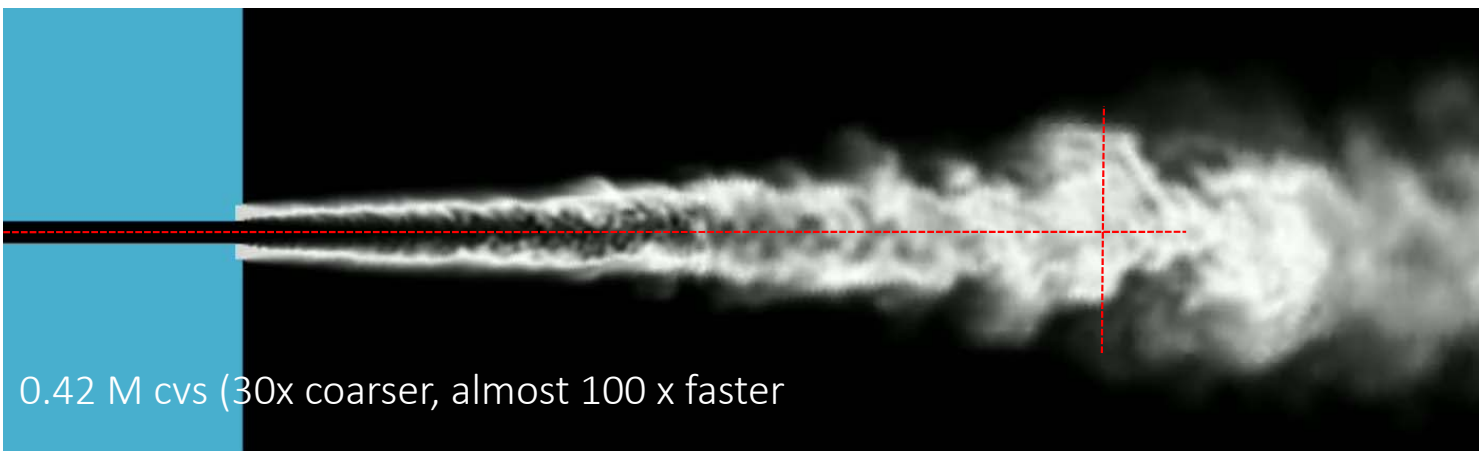
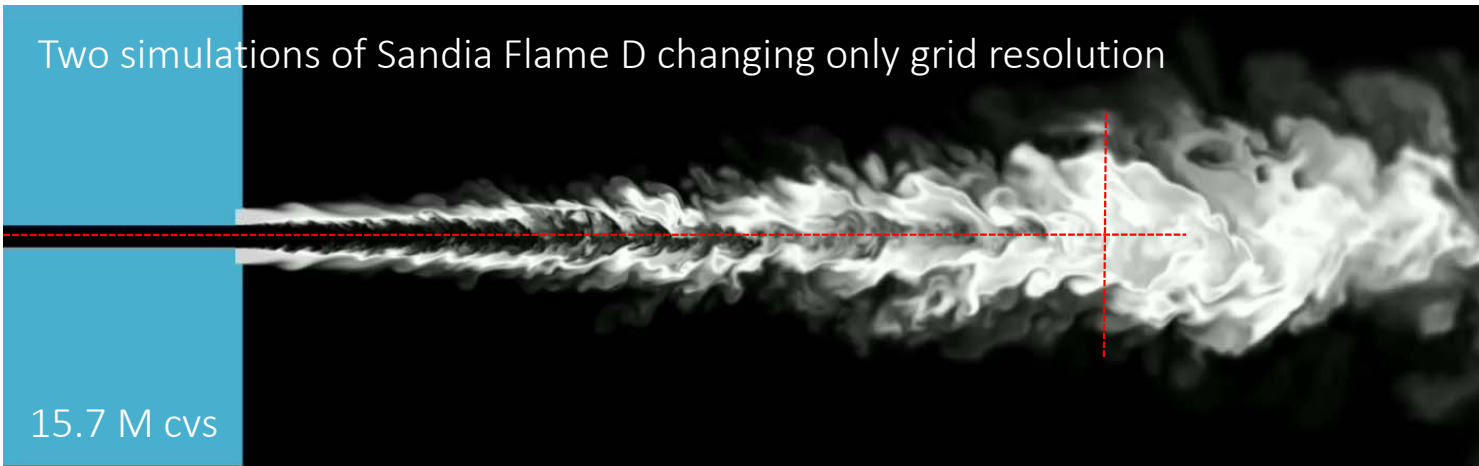
Jet: CH₄/Air

Co-flow: C₂H₂, H₂, air, CO, and N₂

Quantitative impact of entropy-preserving schemes (I)

Application to Sandia Flame D

Two simulations of Sandia Flame D changing only grid resolution

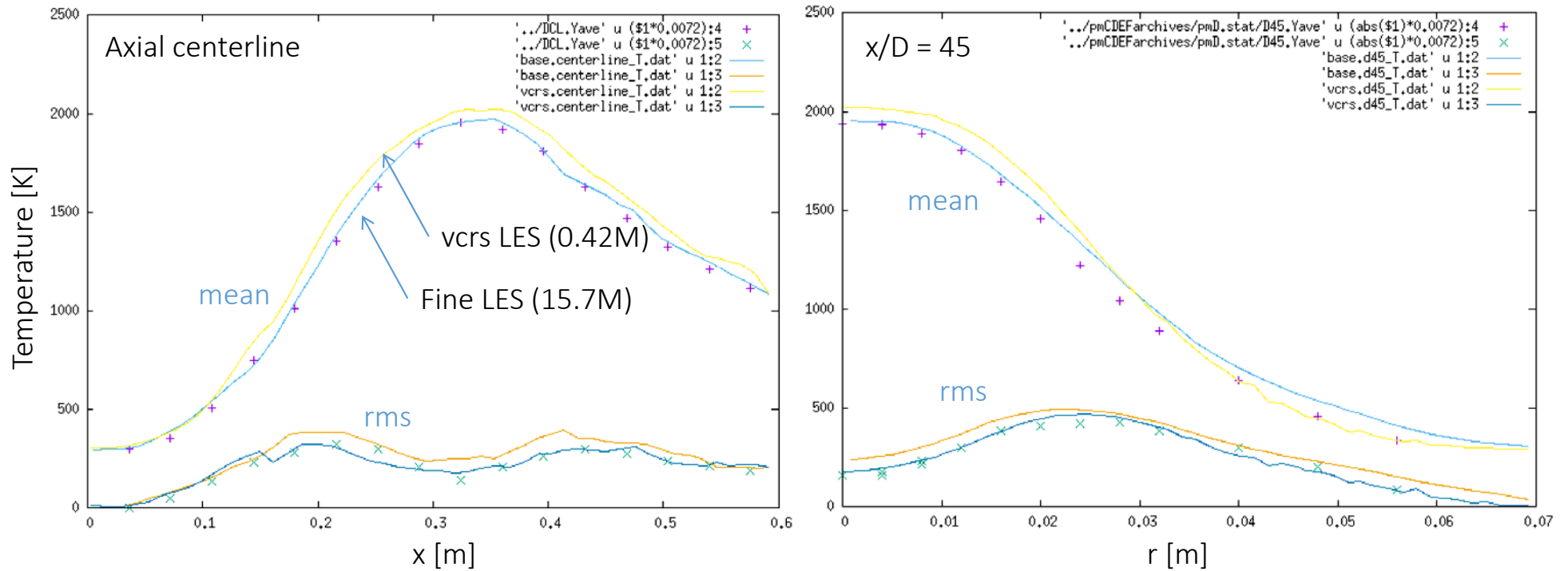


Compare temperature profiles for axial centerline and radial profiles where the centerline temperature peaks

Both locations are sensitive to the addition of numerical dissipation – either from spurious diffusion of hot products or spurious entrainment of the surrounding air

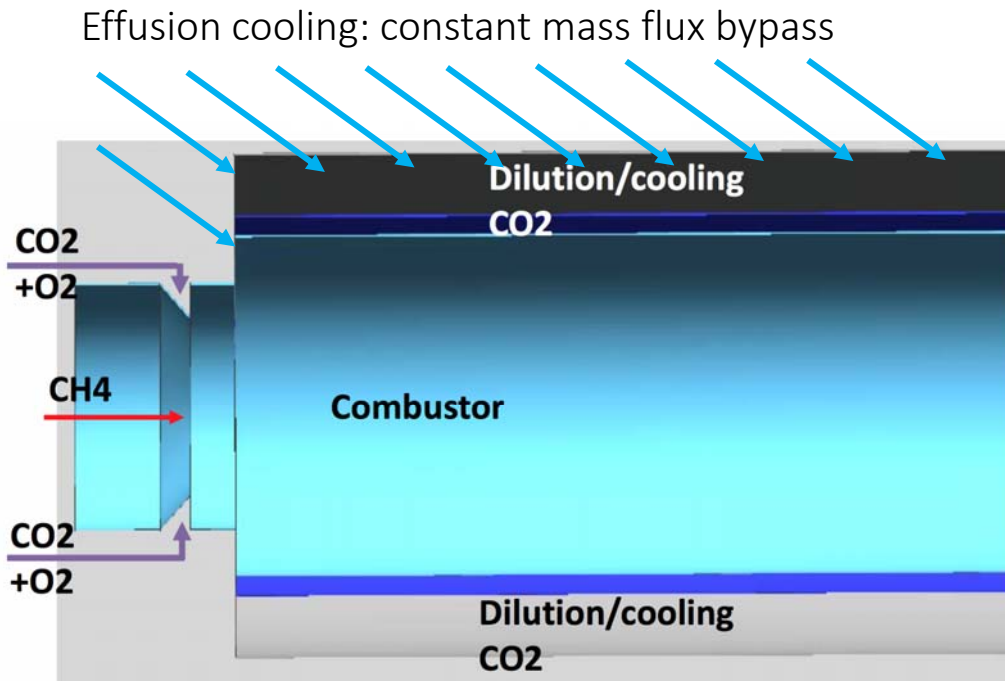
Quantitative impact of entropy-preserving schemes (II)

Application to Sandia Flame D



LES statistics compare remarkably well with experiment from both “fine” and very “coarse” LES

SwRI sCO₂ Swirl Combustor



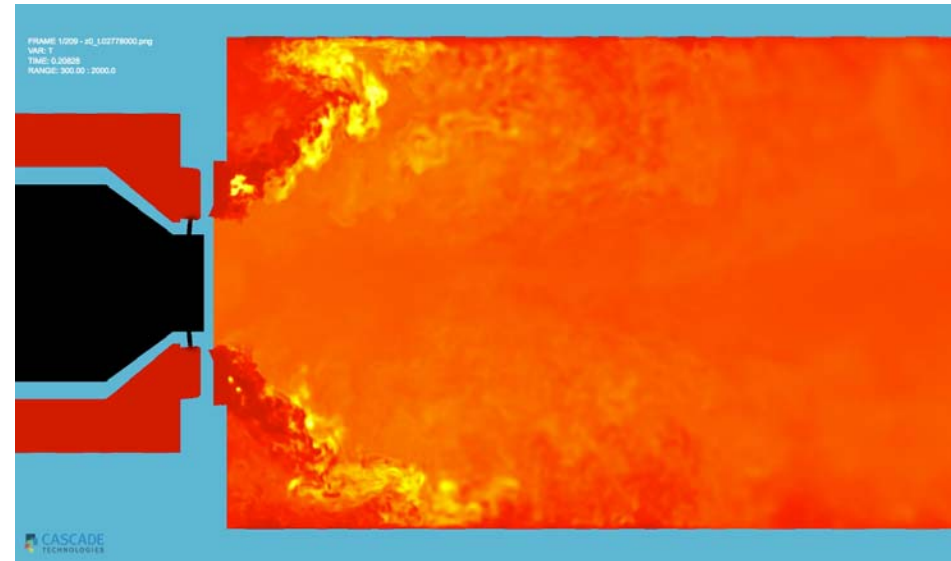
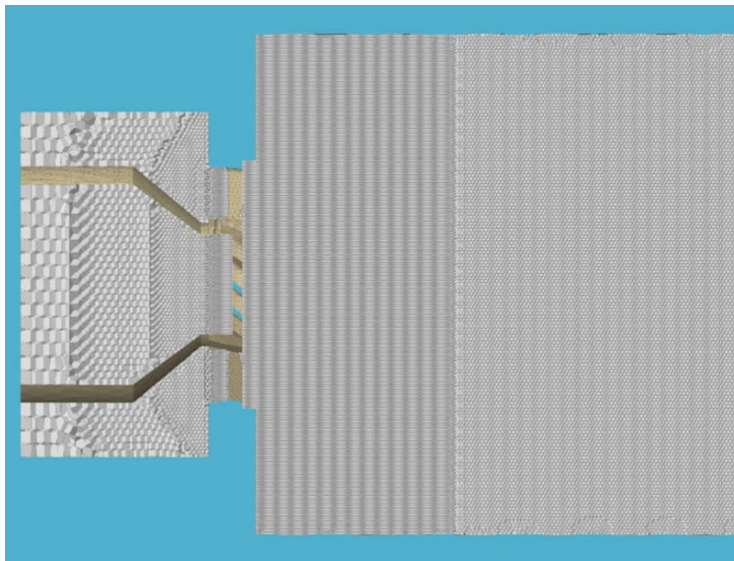
Component	Mass flow in kg/s
CH ₄	0.02
O ₂	0.08
CO ₂ combustor	0.626
CO ₂ bypass	0.899
Total	1.625

Delimont UTSR 2017

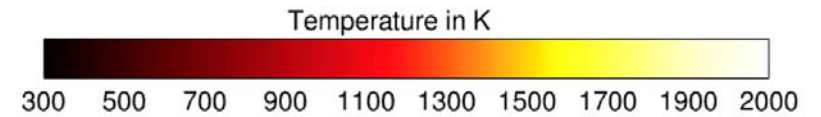
SwRI sCO₂ Swirl Combustor



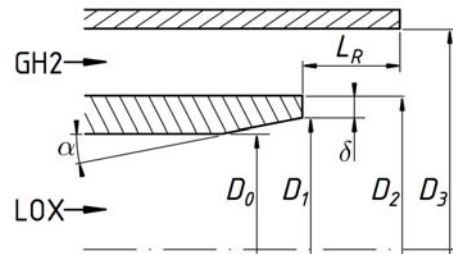
Delimont 2017



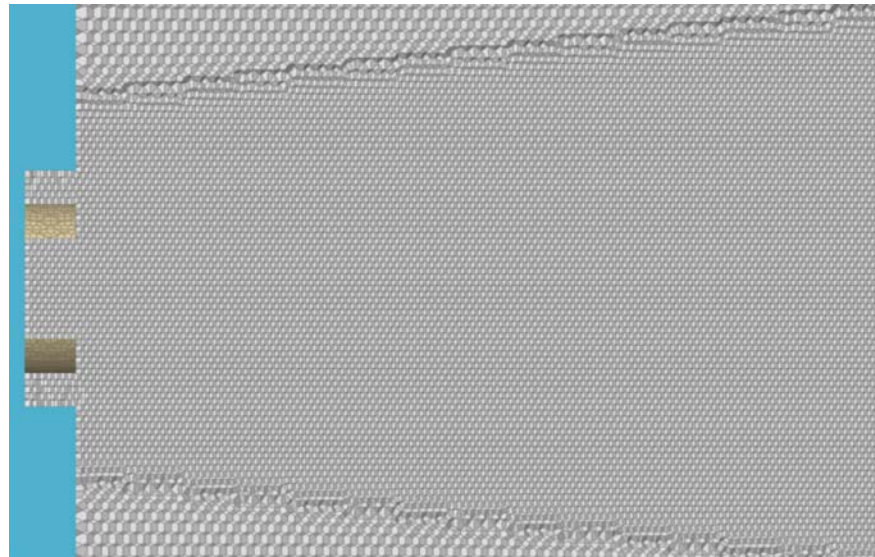
Component	\dot{m} in kg/s	T_{in} in K	ρ_{in} in kg/m ³	X_i	Position
CH ₄	0.02	300	186.3	1.0	center
O ₂	0.08	1000	90.23	0.15	annulus
CO ₂	0.626	1000	125.0	0.85	annulus



Coaxial injector – reduce wall heat loads

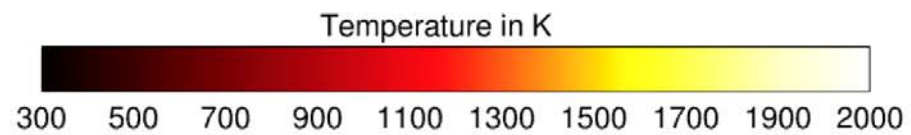
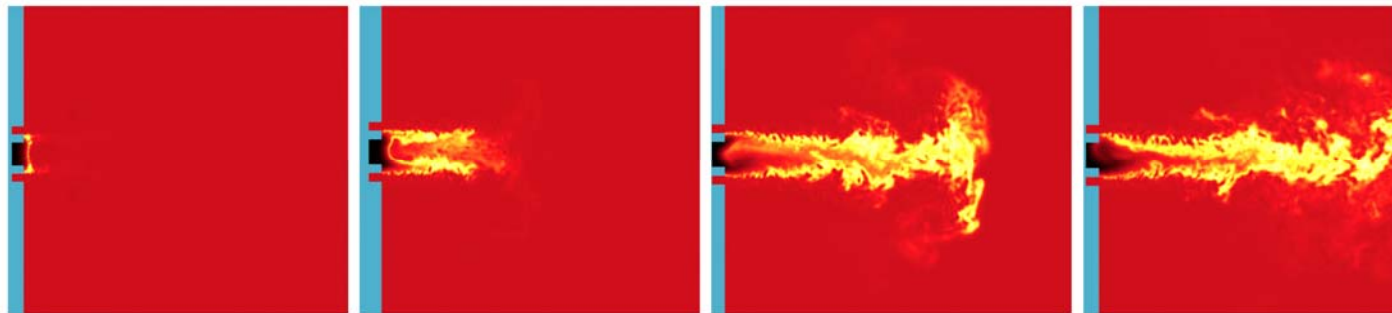


D_0	D_2	D_3	α	L_R	D
0.003	0.005	0.007	0	0	0.0508



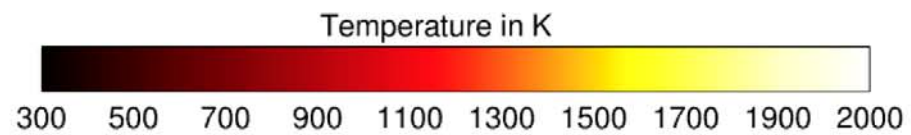
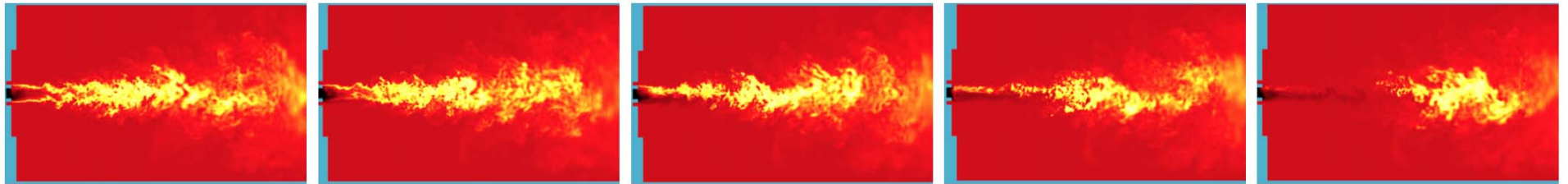
Component	\dot{m} in kg/s	T_{in} in K	ρ_{in} in kg/m ³	X_i	Position
CH ₄	0.02	300	186.3	1.0	center
O ₂	0.08	1000	90.23	0.15	annulus
CO ₂	0.626	1000	125.0	0.85	annulus

Transients – start up



time

Transients – blow out



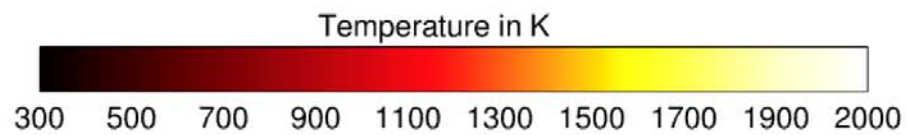
time

Different mixing regimes

Essentially laminar CH₄ jet,
insufficient mixing

Flame anchored in
Recirculation zone

Flame blowout due to
too high shear



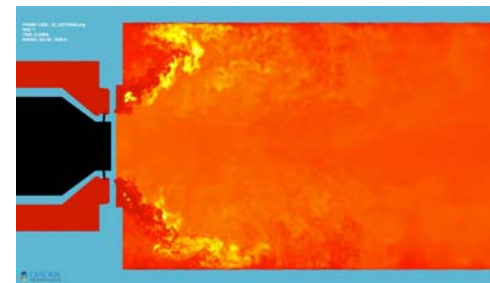
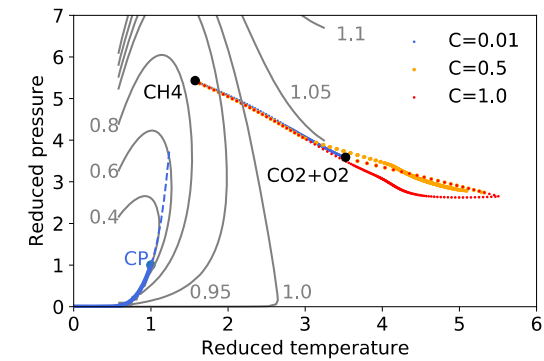
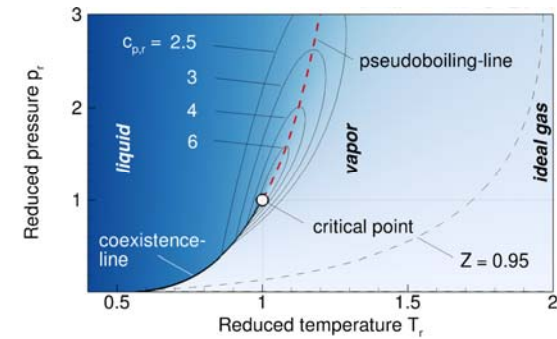
Increasing co-flow mass flow

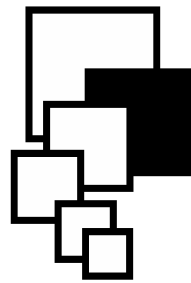
Conclusions

- Goal: develop HPC CFD for sCO₂ combustion
- Supercritical fluids can be ideal gases, subcritical gases can be real fluids
- In sCO₂ combustion, even hot reaction gases may exhibit real fluid properties
- Solver validated for pure real fluids and combustion
- Preliminary ideal gas sCO₂ results promising
- Next step: reactive real fluids

- Q: Why not burn pure CH₄+O₂, and dilute later?

dbanuti@cascadetechnologies.com



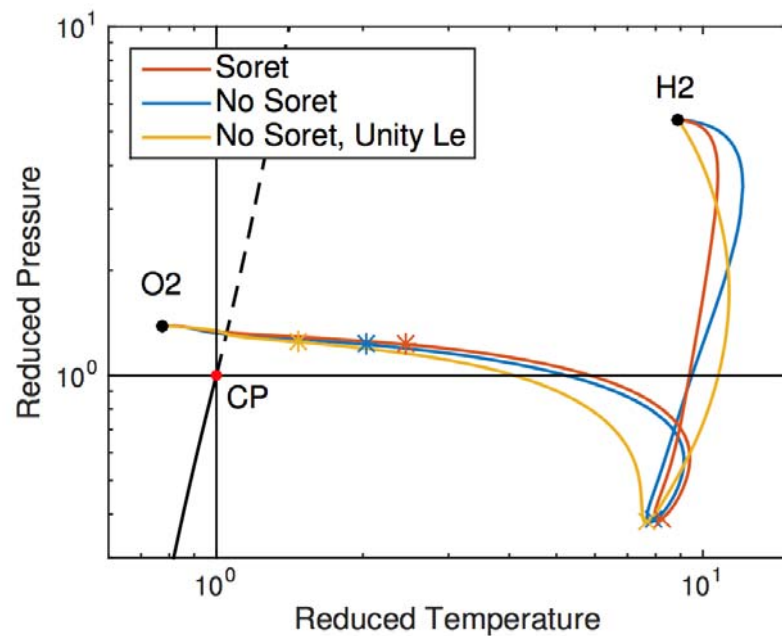


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TECHNOLOGIES

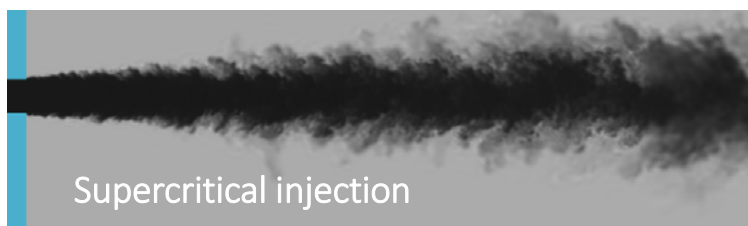
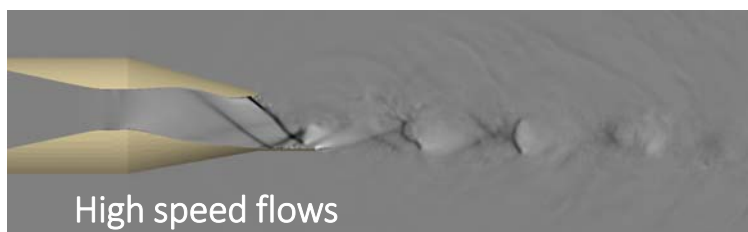
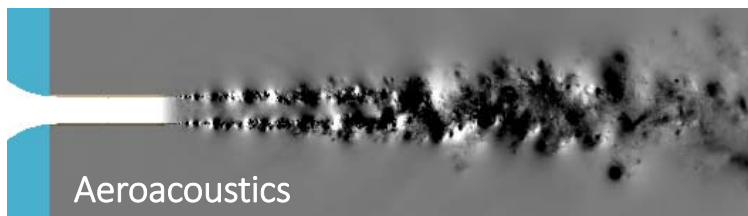
Discovery through simulation

LOX/GH2 flame trajectory - transport



- End points and flame not affected
- Reduced diffusion in real fluid makes trajectory more horizontal

Stability using physics, not dissipation!



Kinetic energy, entropy preserving (KEEP) schemes

- Discrete entropy framework used to develop low dissipation fluxes has been generalized to treat a variety of flow regimes (e.g., high speed flows, reacting flows, real gas effects)
- Leads to a stable, homogenous flux discretization without complex sensors, upwinding hybridization, or tuning of coefficients for stability

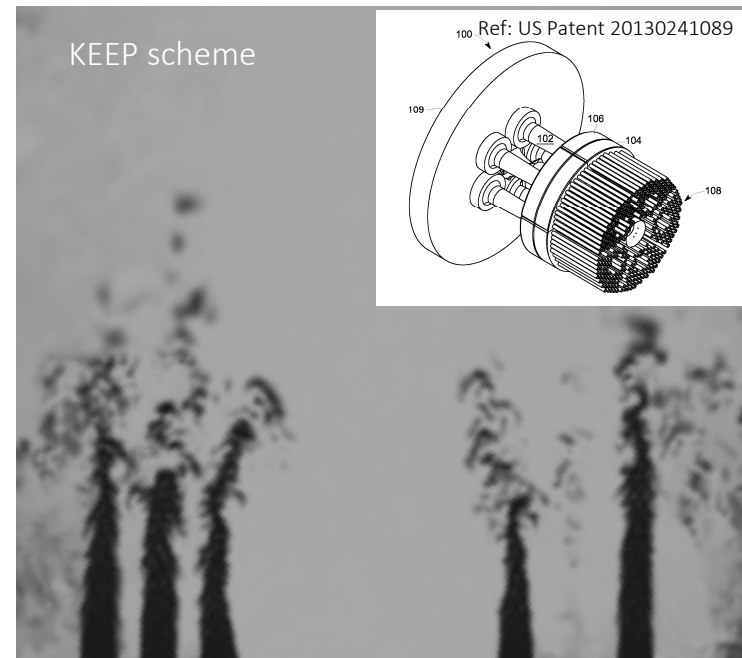
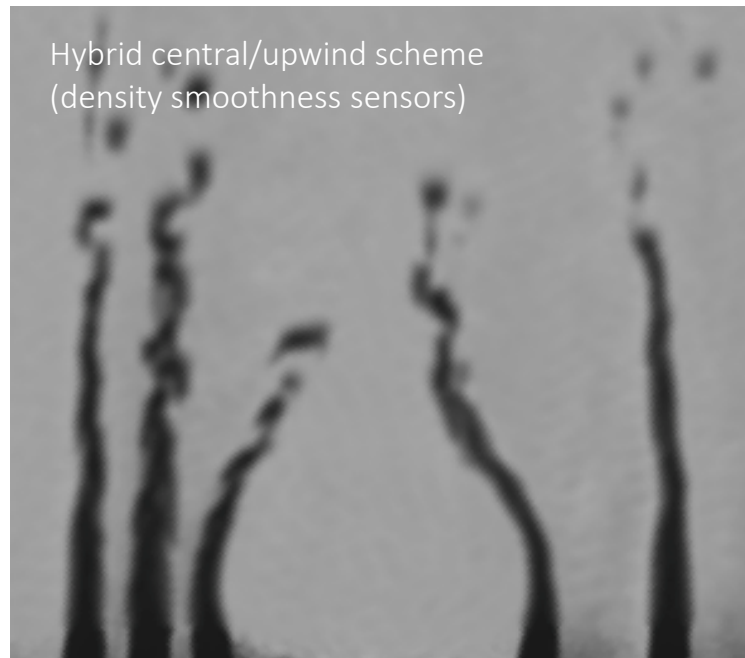
Stability conditions based on discrete satisfaction of Gibbs-Duhem condition (2nd law of thermodynamics)

$$d(\rho s) = \frac{1}{T} d(\rho E) - \frac{u}{T} d(\rho u) + \left(s + \frac{u^2}{2T} - \frac{h}{T} \right) d\rho$$

$$\Delta w_i f_i + \Delta(\rho u) = 0; w_i = \nabla_\phi(\rho s)$$

KEEP schemes drastically improve solution quality and numerical stability

Example: Premixed combustion in industrial multi-element combustor



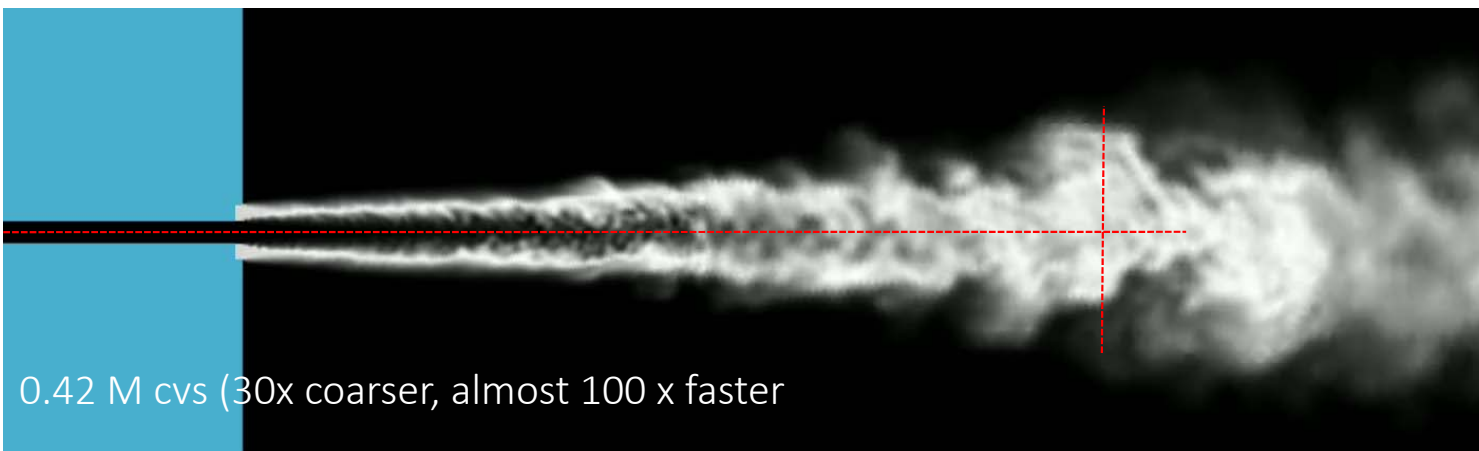
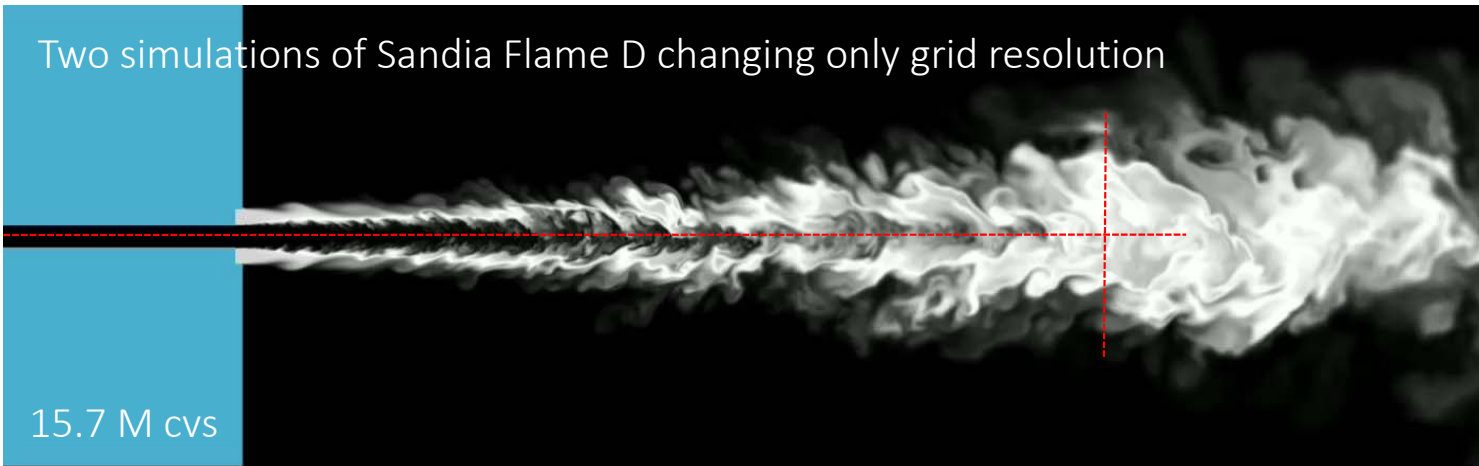
System level LES calculations necessarily result in coarsely resolved structures

- KEEP schemes improve accuracy (e.g., flame length consistent with experiments)
- Simulations are more robust and less sensitive to mesh resolution and transitions

Quantitative impact of entropy-preserving schemes (I)

Application to Sandia Flame D

Two simulations of Sandia Flame D changing only grid resolution

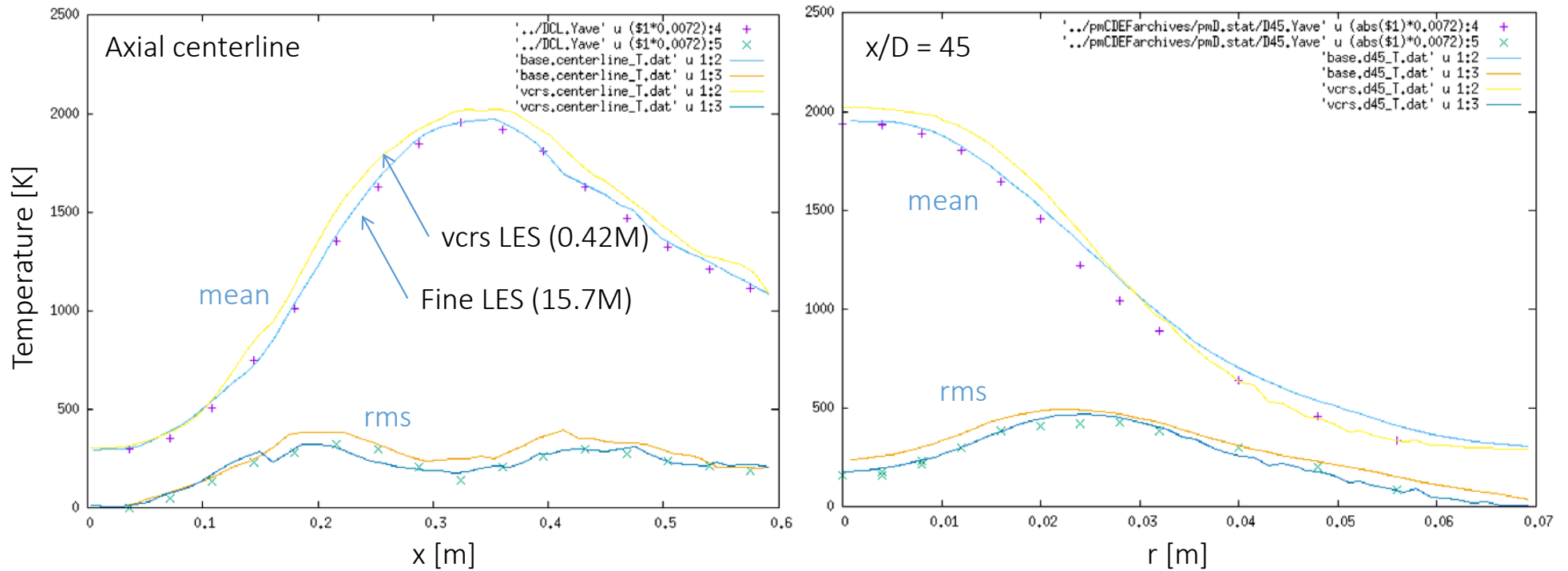


Compare temperature profiles for axial centerline and radial profiles where the centerline temperature peaks

Both locations are sensitive to the addition of numerical dissipation – either from spurious diffusion of hot products or spurious entrainment of the surrounding air

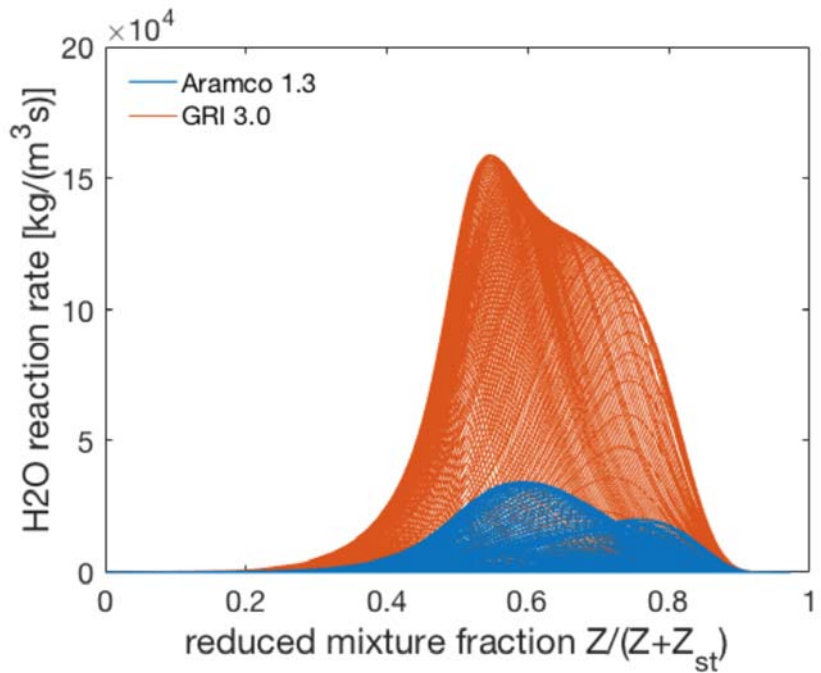
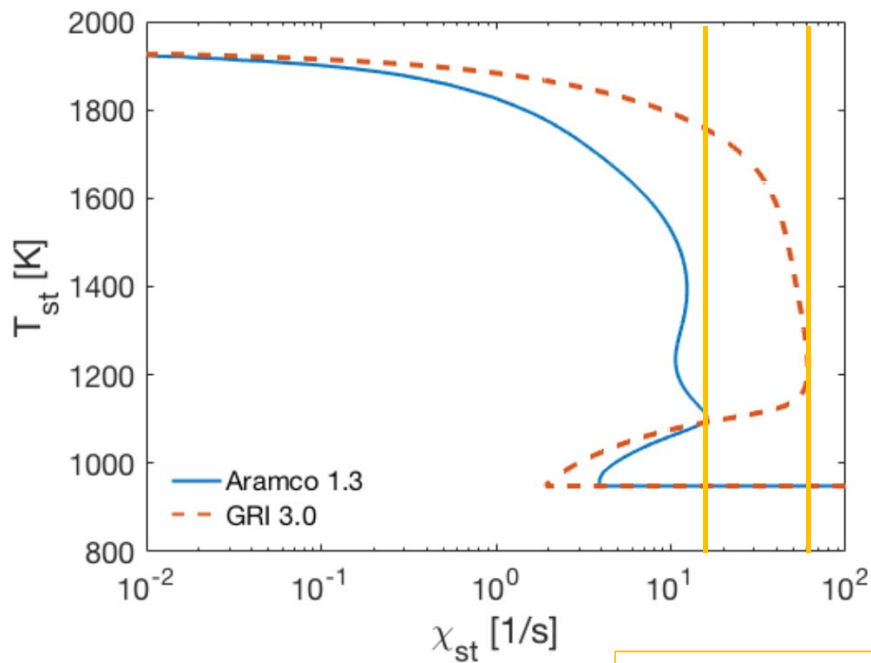
Quantitative impact of entropy-preserving schemes (II)

Application to Sandia Flame D



LES statistics compare remarkably well with experiment from both “fine” and very “coarse” LES

Main differences between mechanisms



Significant discrepancy
in maximum strain rate
introduced uncertainty
for injector studies

Literature review

Source	Name	Type	Turbulence	Spray	EOS	Mixing	Combustion
[48, 13]	'CFD-ACE'	incomp	k-ε	SEE	n/a	x	x
[56]	Oefelein	compr	LES	SEE, SEL	BWR/SRK	ECS	FR9S24R
[54]	Oefelein	compr	DNS/LES	SEE	PR	ECS	FR nS
[55]	Oefelein	compr	DNS/LES	SEE	PR	ECS	FR9S19R
[82, 83, 84]	Yang	n/a	LES	SEE, SEL	BWR/SRK	ECS	x
[28, 18]	'FDNS-RFV'	FD incomp	k-ε	SEE/SEL	HBMS	additive volume	FR6S10R
[57, 58, 59]	Bellan	pressure	DNS	SEE	mPR	vdW	x
[67]	'MSD+DLS'	struct FV	k-ε	SEL/IATE	iG	iG	EQU,PDF
[10]	'TEACH'	incomp	k-ε	SEE	iG/Z eq	iG	x
[81]	'ROCFLAM'	FV compr	k-ε	SEL	iG	iG	FR
[32]	'CryoROC'	FV compr	k-ε	SEL	iG	iG	FR5S1R ED
[40]	'Rocflam II'	FV compr	k-ε	SEL*	iG	iG	EQU,PDF, FR ED
[22, 23]	Cutrone	compr	k-ε	SEE	PR, iG	vdW	Flamelet, FPV
[65, 66, 38]	'CFX'	pressure	k-ε	SEE	RK, PR	vdW, ECS	ED1S, Flamelet
[36]	'CRUNCH'	FV compr	RANS/LES	SEE	SRK, HBMS	x	x
[72, 73, 71]	'AVBP'	compr	LES	SEE	PR	vdW	FR4S2R
[47]	Menon	FV compr	LES	SEE	PR	vdW	EBU, EQU, FR2S
[39]	Kim	FV incomp	k-ε	SEE	mSRK, PR	vdW	Flamelet
[35, 44, 45, 9]	'CharLES ^x '	FV compr	LES	SEE	PR	vdW / VLE	FPV
[52, 53]	'INCA'	FV compr	LES	SEE	PR	vdW	x
[77]	'Ansys Fluent'	n/a	k-ε	SEE	iG	iG	FR6S2R
[25, 24]	'Ansys CFX'	n/a	k-ε	SEE	n/a	n/a	FR6S2R
[19]	Raman	FV incomp	DNS	SEE	PR	vdW	FR5S2R
[4]	'TAU'	FV compr	SA	SEE	MBWR	MFM	FR8S17R
[68]	'KIVA 3V'	FV	SA	SEL	PR	VLE	x
[29]	Giovangigli	FD	DNS	SEE	SRK	DI	FR

+40 papers from
+20 groups

standard

sCO2

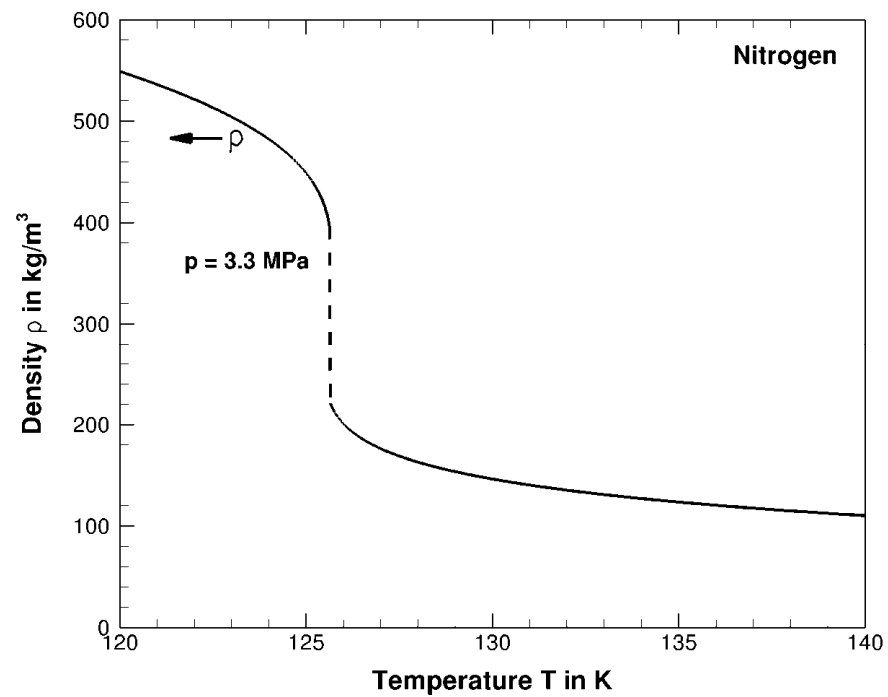
alternative
mixing

Table 2: Overview of CFD codes for real gas injection. Abbreviations: n/a: not given, x: not used, incomp: incompressible, compr: compressible, FV: finite volume, pressure: pressure based, FD: finite difference, struct: structured, k-ε: RANS, SEL*: statistical Eulerian-Lagrangian where particles are converted to continuum immediately after injection, BWR (t): BWR EOS used for transport coefficients, HBMS: Hirschfelder-Buehler-McGee-Sutton EOS, mPR: modified PR EOS, Z eq: mixture fraction transport equation, mSRK: modified SRK EOS, iG: ideal-gas EOS or mixing rules, FRnSmR: finite-rate chemistry with n species and m reactions, EQU: equilibrium, PDF: flame turbulence interaction based on probability density function, ED: eddy dissipation, FPV: flamelet progress variable, ED1S: eddy dissipation one species, EBU: eddy break-up, DI: diffuse interface, MFM: multi-fluid mixing, VLE: vapor liquid equilibrium.

What happens at the supercritical transition?

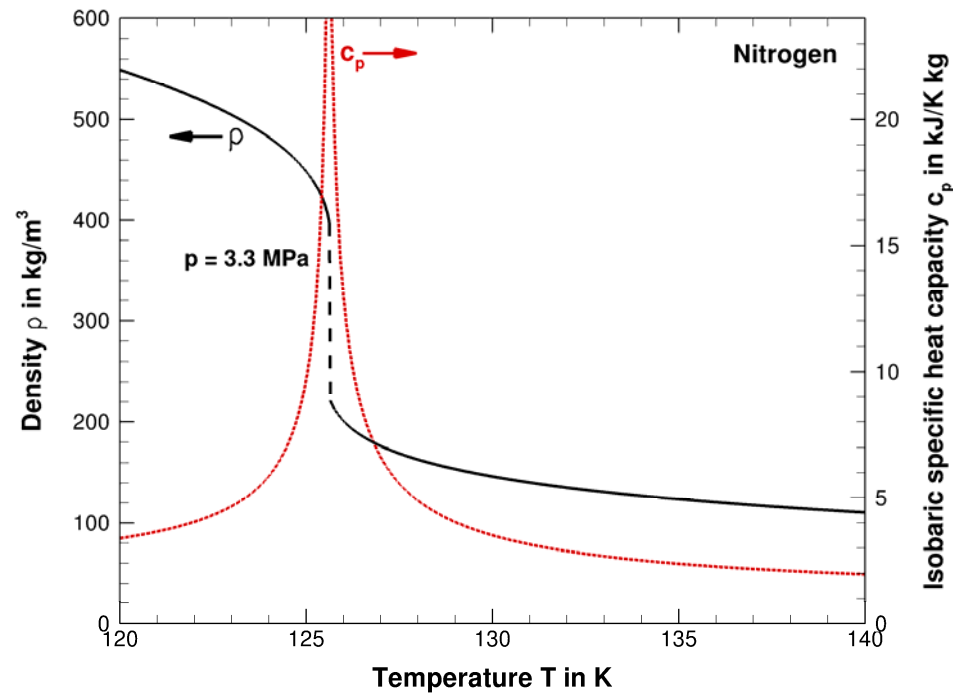
Are supercritical fluids insensitive to dp , dT ?

Sub- and supercritical phase transitions



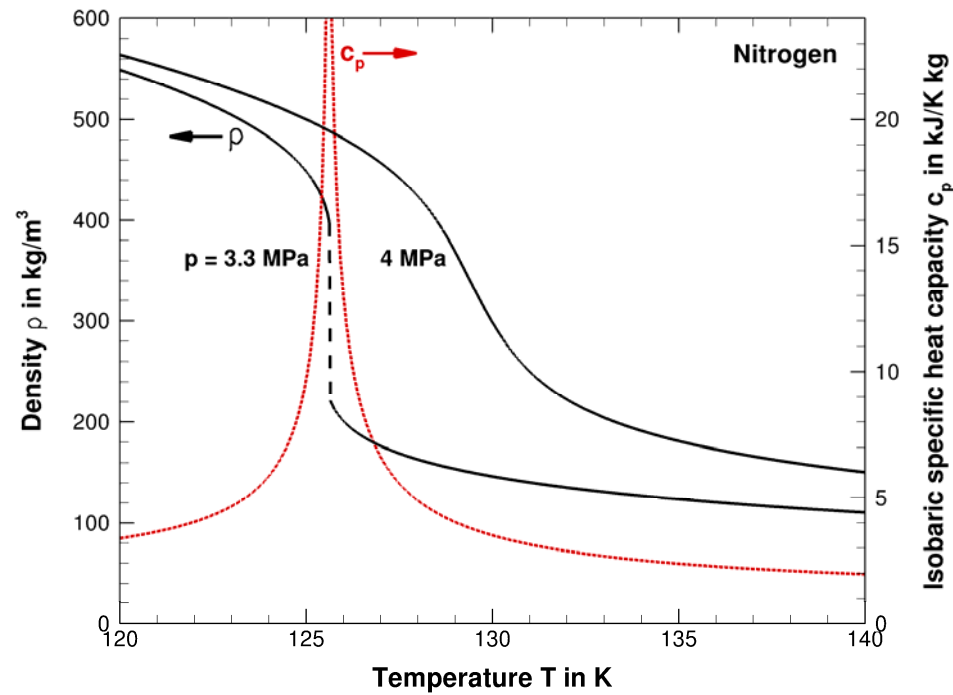
Banuti and Hannemann PoF 2016

Sub- and supercritical phase transitions

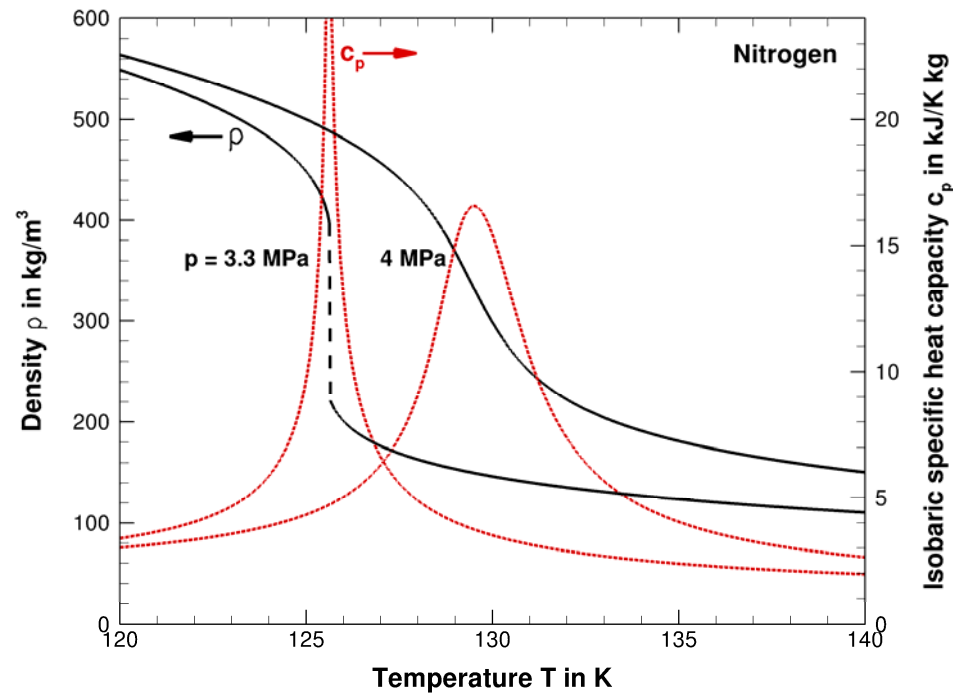


Banuti and Hannemann PoF 2016

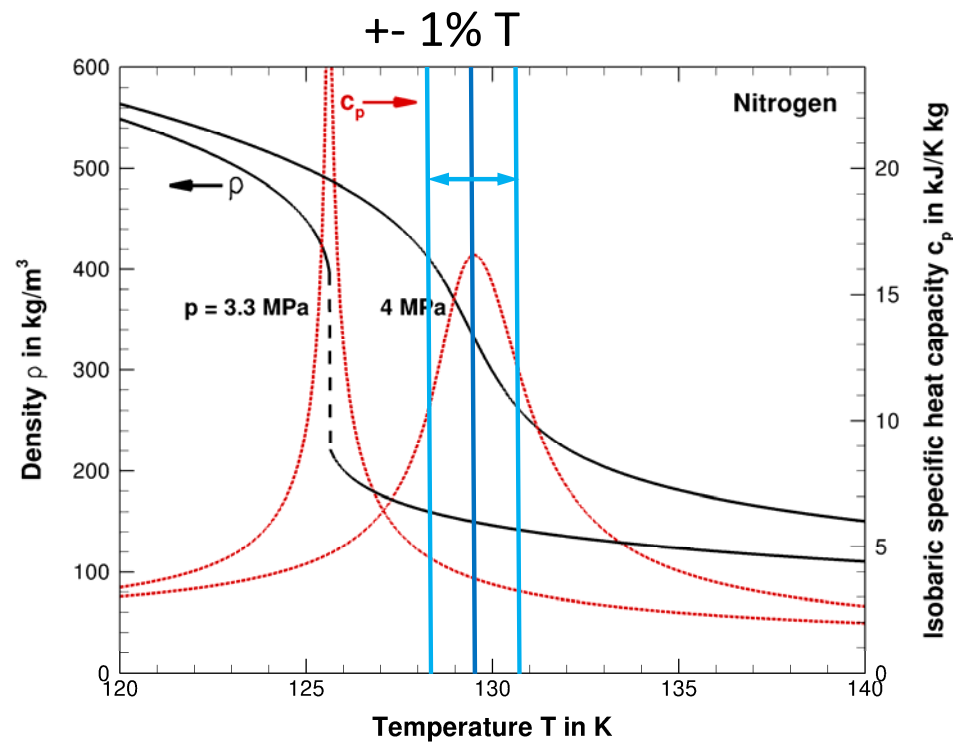
Sub- and supercritical phase transitions



Sub- and supercritical phase transitions: pseudoboiling



Sub- and supercritical phase transitions: pseudoboiling



Sub- and supercritical phase transitions: pseudoboiling

