



**UCLA**

# Off-design Performance of the Recompression sCO<sub>2</sub> Cycle for CSP Applications

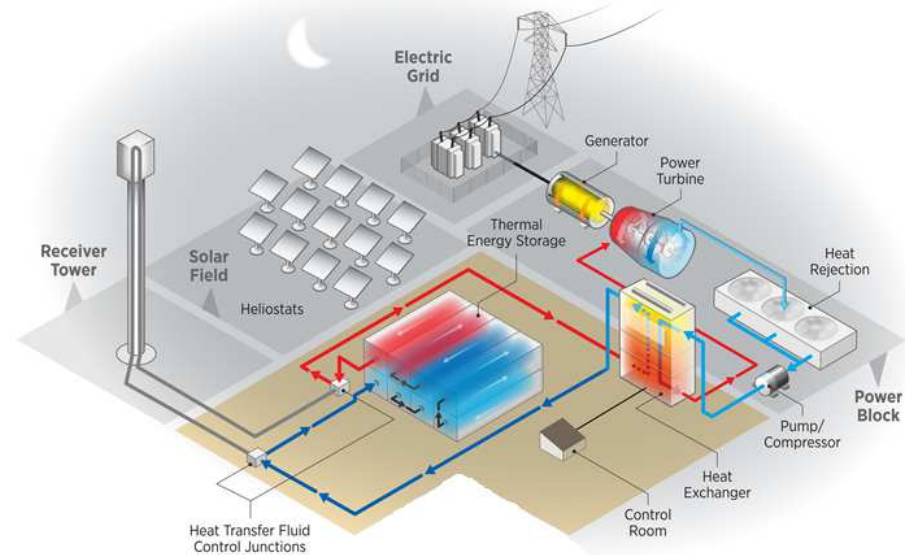
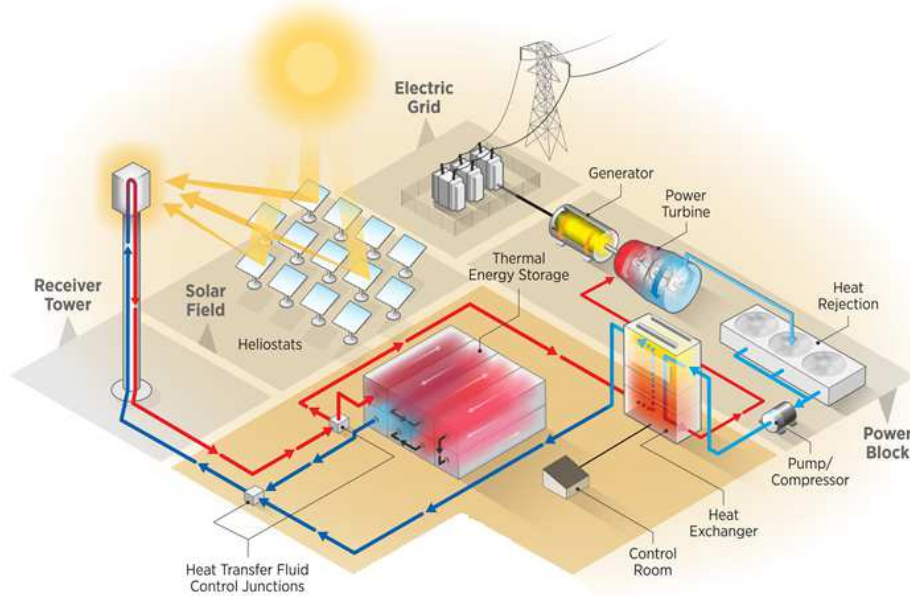
**5<sup>th</sup> International Supercritical CO<sub>2</sub>  
Power Cycles Symposium**

**Ty Neises - NREL**

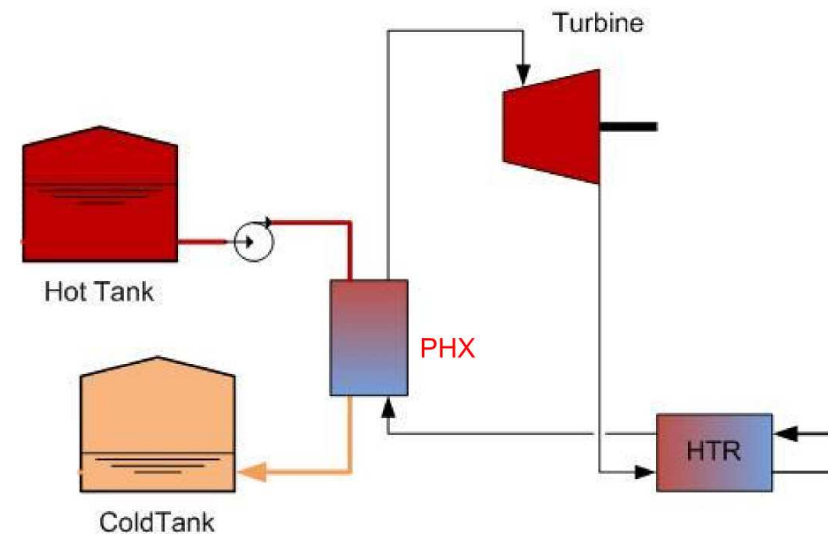
**Louis Tse - UCLA**

**March 30, 2016**

# Concentrating Solar Power Overview



- Concentrated sunlight heats a fluid (e.g. molten salt) that delivers thermal power to cycle
- Hot fluid is stored and dispatched to cycle to maximize revenue
- Storage decouples electricity generation from sunlight; CSP acts as dispatchable generator



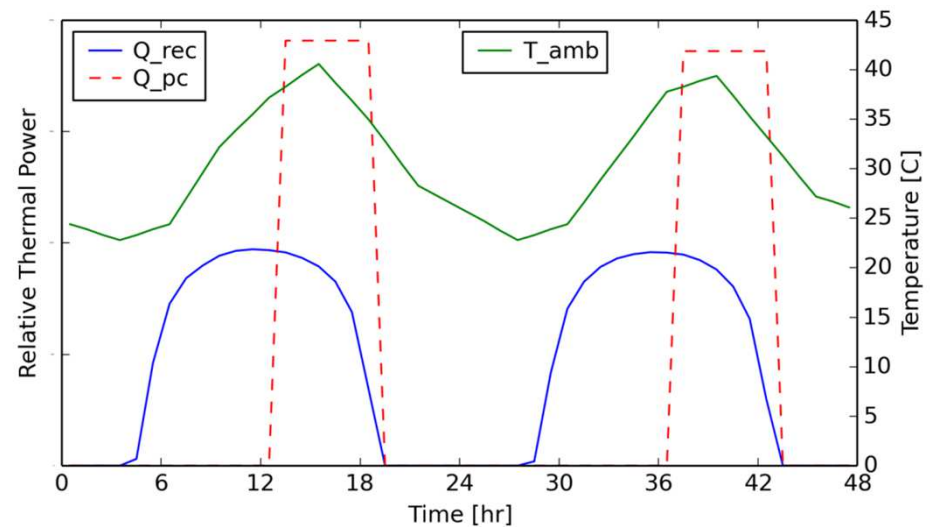
# sCO<sub>2</sub> Cycle Attributes and Areas of Focus

## Attributes

- Efficiency at CSP temps (550 – 750 C)
- Performance at smaller capacity (10-50 MWe)
  - Enables smaller, cheaper, more efficient CSP systems
  - Potentially allows for more favorable financing options

## CSP Areas of Focus

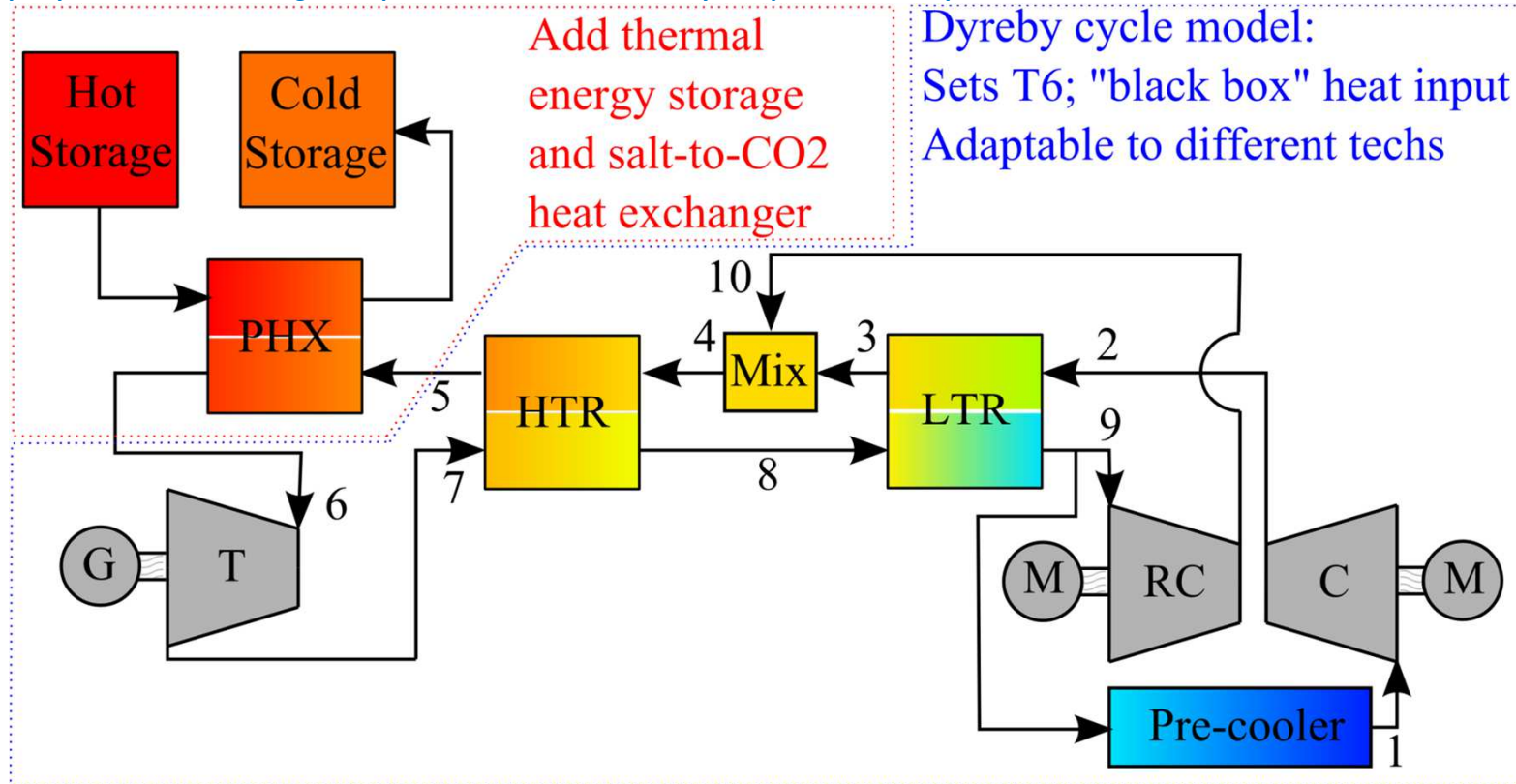
- Performance & control of dry-cooled cycles in desert climates
  - Cycle operation over varying (hot) compressor inlet temps
- $\Delta T$  over primary heat input & thermal storage: storage cost
  - Off-design & part-load operation impact on storage capacity
- Dispatchable generation
  - Part-load operation, ramping, and standby



# Modeling Overview

## Approach: Extend and analyze Dyreby's cycle models for CSP applications

Dyreby, J. J., 2014, "Modeling the Supercritical Carbon Dioxide Brayton Cycle with Recompression," THE UNIVERSITY OF WISCONSIN-MADISON



### Component Models:

- Counterflow HX
- Compressor
- Turbine

### Simplifications:

- Pre-cooler can achieve constant 15°C difference between comp inlet and ambient temperatures
  - Fan parasitics ignored
- Generator/motor efficiencies included in turbomachinery isentropic efficiencies

# Compressor Design

Characterize performance using dimensionless parameters and performance curves fitted from SNL radial compressor data:

Ideal Head Coefficient:  $\psi_i = \frac{\Delta h_i}{U_c^2}$

Flow Coefficient:  $\phi = \frac{\dot{m}}{\rho U_c D_c^2}$

$\Delta h_i$  ideal (isentropic) enthalpy change

$U_c$  rotor tip speed

$\dot{m}$  mass flow rate

$\rho$  density

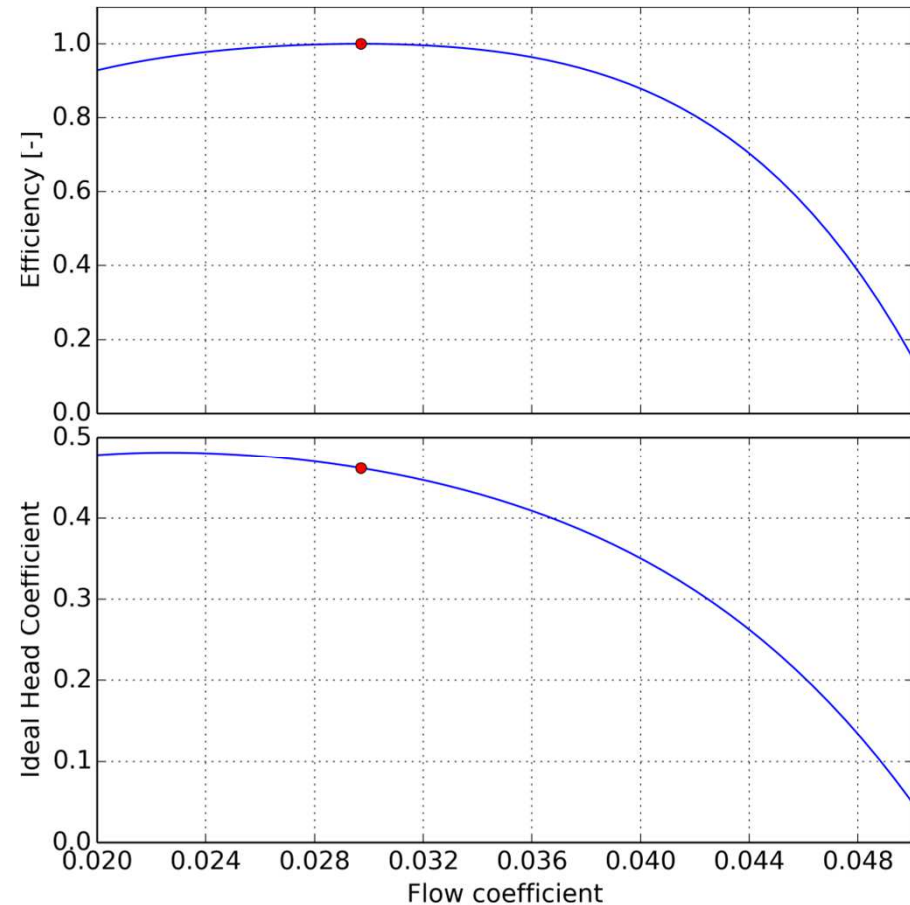
$D_c$  rotor diameter

## Design

○ Know:  $T_{in}, P_{in}, T_{out}, P_{out}, \dot{m}, \eta_{isen}$

○ Design:  $\phi_{opt}, \psi_{i,opt}$

○ Calculate:  $D_c, U_c, N_c$



# Compressor Off-Design Performance

Characterize performance using dimensionless parameters and performance curves fitted from SNL radial compressor data:

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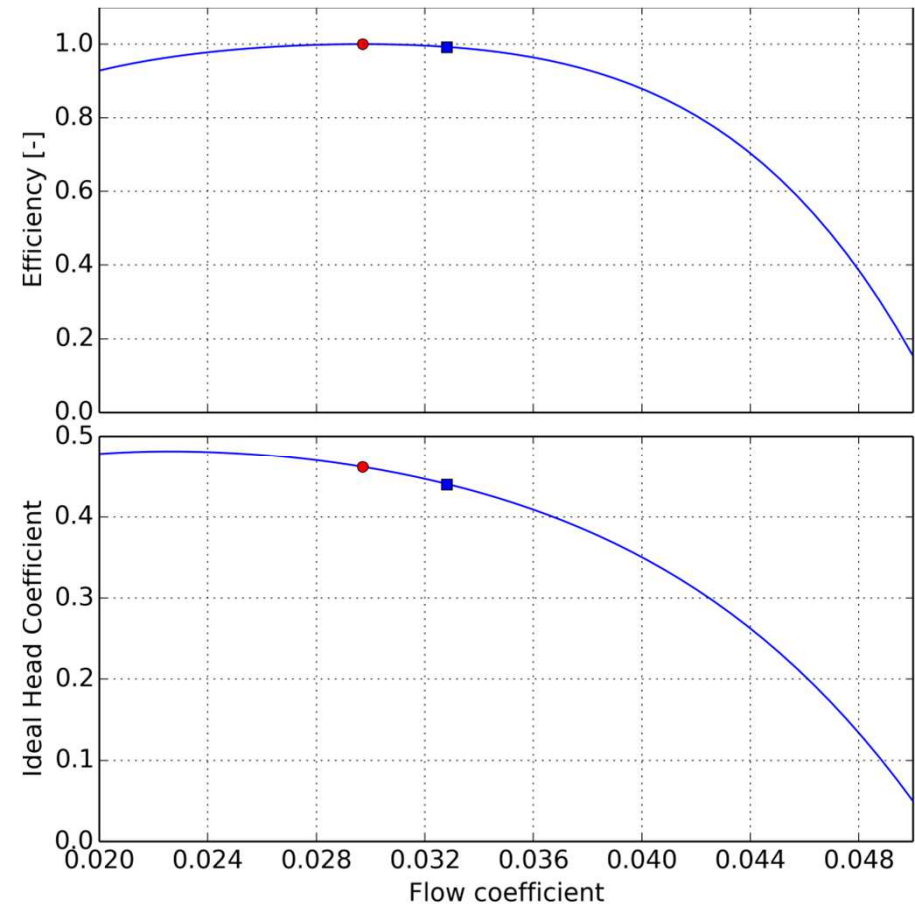
$\dot{m}$  mass flow rate

$\rho$  density

$D_c$  rotor diameter

## Off-Design Performance

- Design:  $D_c, \eta_{isen}$
- Set:  $P_{in}, T_{in}, N_c, \dot{m}$
- Calculate:  $\phi, \psi, P_{out}, \eta_{adj}$



# Turbine Modeling

Characterize performance using dimensionless parameters and modeled efficiency curves (Wright et al. 2011):

$$\dot{m} = C_s A_{nozzle} \rho$$

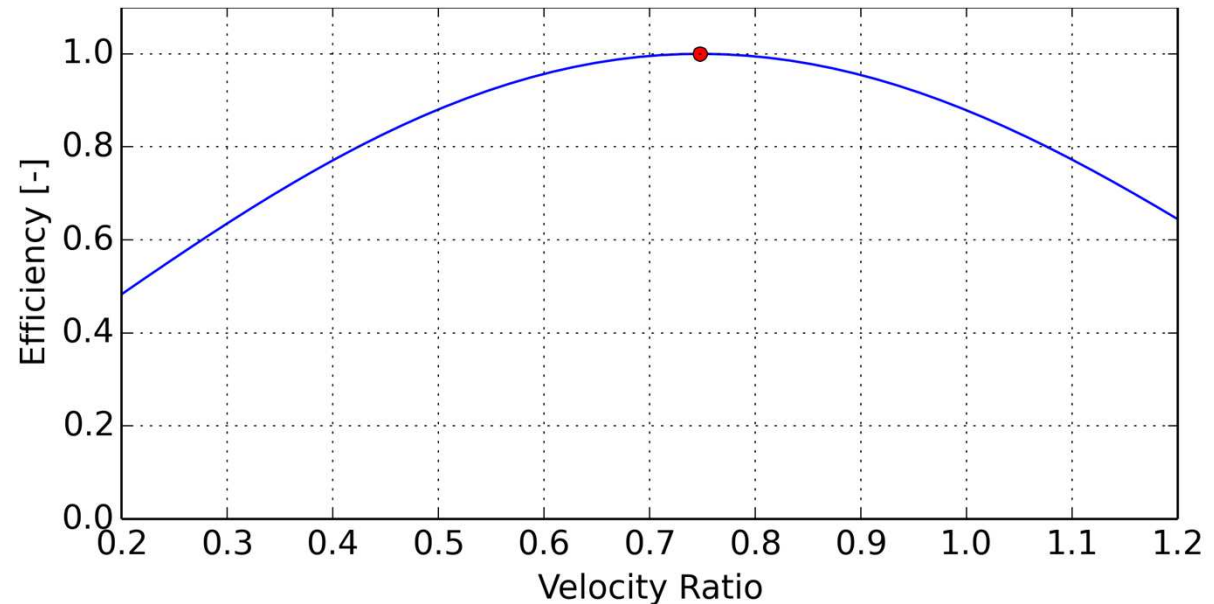
$$C_s = \sqrt{2\Delta h_i}$$

$$v = \frac{U}{C_s}$$

$A_{nozzle}$  Effective nozzle area

$C_s$  Spouting velocity

$v$  Velocity ratio



## Design

- Know:  $T_{in}, P_{in}, T_{out}, P_{out}, \dot{m}, \eta_{isen}, N$
- Design:  $v_{opt}$
- Calculate:  $A_{nozzle}, D, U$

## Off-Design Performance

- Design:  $A_{nozzle}, D, \eta_{isen}$
- Set:  $P_{in}, T_{in}, N, P_{out}$
- Calculate:  $v, \dot{m}, \eta_{adj}$

# Counterflow Heat Exchanger Modeling

## Design

- Know design performance:
  - inlet and outlet states
  - mass flow rates
- Solve for required UA
- Example: PHX, CR = 1

$$\dot{q}_{max} = (\dot{m}c_p)_{CO_2,des} \cdot (T_{HTF,hot} - T_{CO_2,PHX,in})$$

$$\epsilon = \frac{\dot{q}_{actual}}{\dot{q}_{max}}$$

$$UA_{des} = \frac{\epsilon}{1 - \epsilon} (\dot{m}c_p)_{CO_2,des}$$

## Off-Design

- Know hot and cold inlet conditions
- Scale conductance for off-design mass flow rate
- Solve for outlet conditions

$$U = U_{des} \left( \frac{1}{2} \left( \frac{\dot{m}_{CO_2}}{\dot{m}_{CO_2,des}} + \frac{\dot{m}_{HTF}}{\dot{m}_{HTF,des}} \right) \right)^{0.8}$$

$$C_R = \frac{\dot{C}_{min}}{\dot{C}_{max}} = \frac{\min \left( [(\dot{m}c_p)_{CO_2}], [(\dot{m}c_p)_{HTF}] \right)}{\max \left( [(\dot{m}c_p)_{CO_2}], [(\dot{m}c_p)_{HTF}] \right)}$$

$$NTU = \frac{UA_{des}}{\dot{C}_{min}}$$



# Design Model

- 1) Find smallest total recuperator conductance resulting in design point efficiency
  - Optimize compressor inlet pressure, pressure ratio, and recompression fraction

Design Point Parameters		Optimized Design Point Parameters	
Net Power Output	10 MW	Comp. Inlet Pressure	9.00 MPa
Thermal Efficiency (no cooling)	0.48 -	Comp. Pressure Ratio	2.74 -
Turb. Inlet Temp	690 °C	Recompression Fraction	0.18 -
Turb. Isentropic Efficiency	0.93 -	<b>Design Point Solution Results</b>	
Turb. Shaft Speed (fixed)	3600 rpm	Recuperator Conductance	1375 kW/K
Main Comp. Inlet Temp	45 °C	Main Comp. Shaft Speed	33294 rpm
Comp. Isentropic Efficiency	0.89 -	Turb. Rotor Diameter	2.32 m
Maximum Pressure	25 MPa	CO2 Mass Flow Rate	82.0 kg/s
Neglecting Pressure Drops		PHX CO2 Inlet Temperature	505 °C

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Maximum Pressure	25 MPa	<b>CO2 Mass Flow Rate</b>	<b>82.0 kg/s</b>
Neglecting Pressure Drops		<b>PHX CO2 Inlet Temperature</b>	<b>505 °C</b>

- 2) Use design cycle solution and PHX parameters to find PHX design

Required Design Point Solution Results	Design Point Parameters		Design Point Solution Results	
<b>PHX CO2 Inlet Temperature</b>	HTF Inlet Temp	700 °C	PHX Conductance	2.9×10 <sup>5</sup> kW/K
<b>Turb. Inlet Temp</b>	Capacitance ratio	1	PHX NTU	9.39
<b>CO2 Mass Flow Rate</b>			HTF Mass Flow Rate	72.4 kg/s

# Off-Design Model

Off-Design Conditions: 1) Ambient Temperature, 2) HTF mass flow rate, 3) HTF Temp

1) Given a turbine inlet temperature, optimize compressor shaft speed, compressor inlet temperature, and recompression fraction to maximize efficiency

Required Design Point Solution Results	Off-Design Parameters	Off-Design Results
Recuperator Conductance	Turb. Inlet Temp 687 °C	Net Power Output 9.30 MW
Turb Isen Efficiency	Comp. Inlet Temp 50 °C	Thermal Efficiency 0.47 -
Turb. Rotor Diameter	<b>Optimized Off-Design Parameters</b>	PHX CO2 Inlet Temp. 510 °C
Comp. Isen Efficiency (2)	Main Compressor Shaft Speed 36523 rpm	Pressure Ratio 2.73 -
Comp. Rotor Diameter (2)	Main Compressor Inlet Pressure 9.0 MPa	CO2 Mass Flow Rate 82.9 kg/s
Maximum Pressure Component Pressure Drops	Recomp. Fraction 0.17 -	

# Off-Design Model

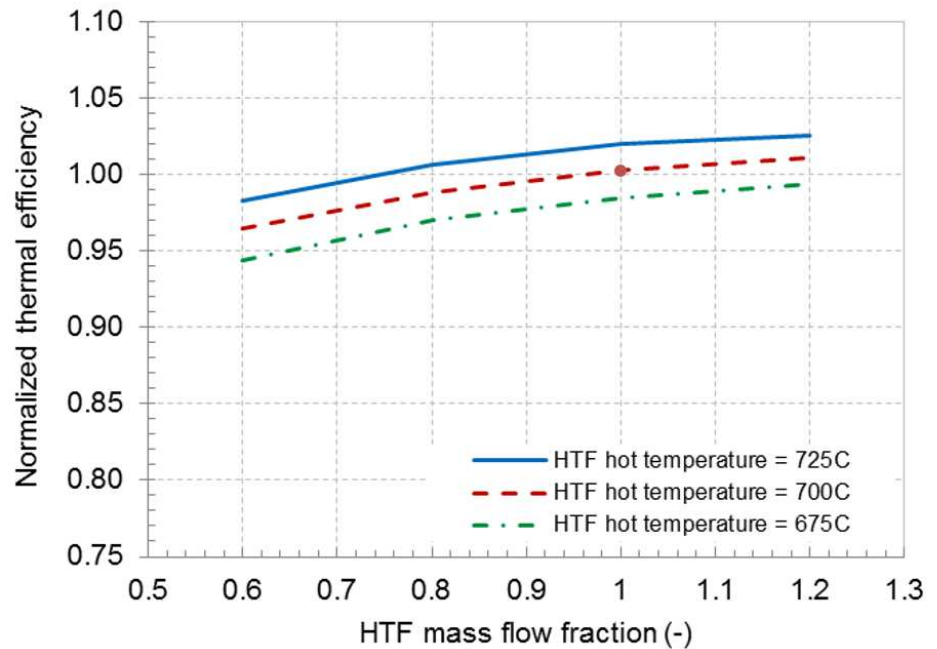
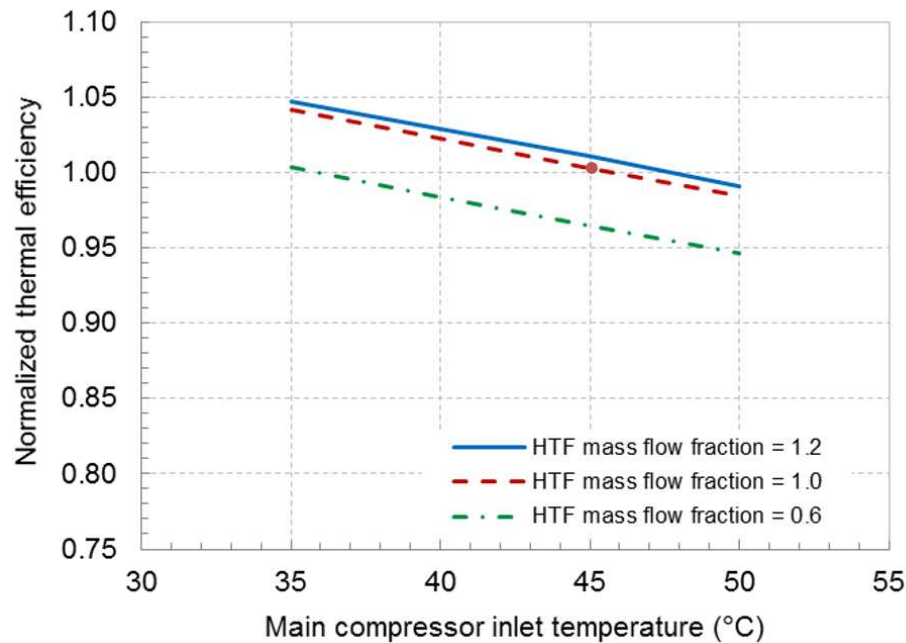
Iterate to find turbine inlet temperature that converged cycle and PHX models

Required Design Point Solution Results	Off-Design Parameters	Off-Design Results
Recuperator Conductance	Turb. Inlet Temp 687 °C	Net Power Output 9.30 MW
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Maximum Pressure Component Pressure Drops	Recomp. Fraction 0.17 -	

Required PHX Design Point Solution Result	Required Cycle Off-Design Solution Results	Off-Design Results
PHX Conductance	PHX CO2 Inlet Temp. 510 °C	Turb. Inlet Temp 687 °C
HTF Mass Flow Rate	CO2 Mass Flow Rate 82.9 kg/s	HTF Return Temp 520 °C
	<b>Off-Design Parameters</b>	
	HTF Inlet Temp 700 °C	

# Off-Design Cycle Efficiency

- Trends compare well against Dyreby's "black box" heat input model
- HTF mass flow > 1 results in turbine temps > design
  - Will add constraint in future analyses
- High efficiencies at part load
  - Inventory control & improved regeneration

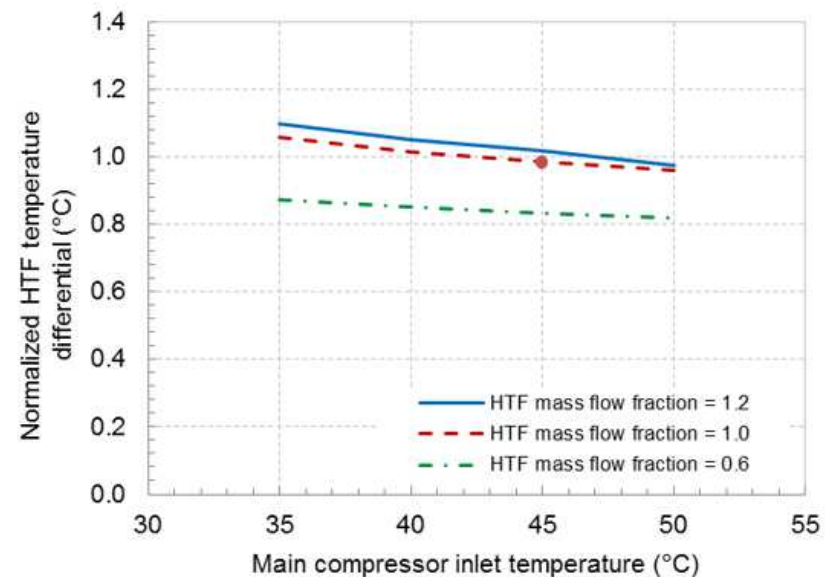
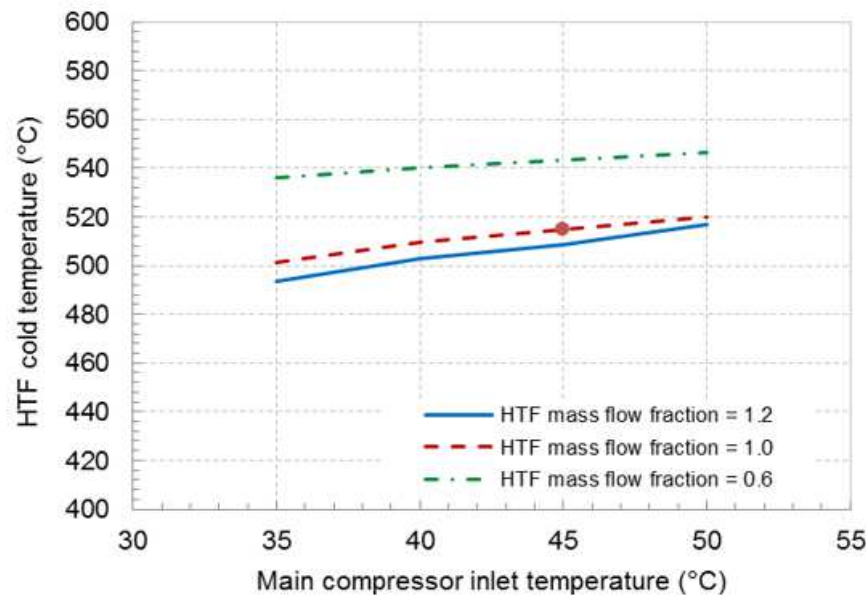


# Off-Design TES Temperature Difference

$$Energy_{TES} = mass * specific\ heat * (T_{hot} - T_{cold})$$

For sensible heat storage:

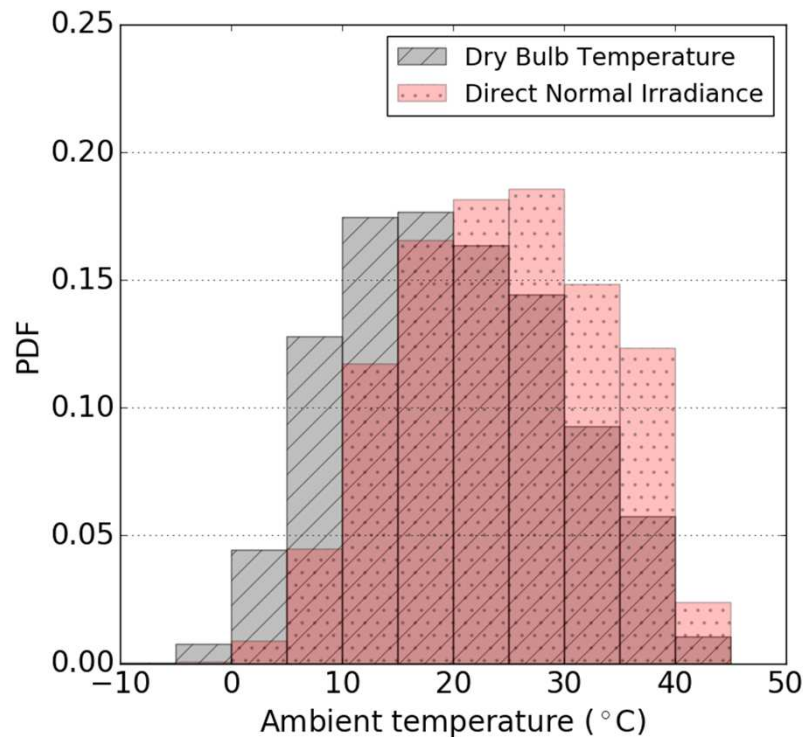
- The required mass of HTF is proportional to the hot and cold tank temperatures.
- All else equal, a cycle with a larger temperature difference is preferred to a cycle with a smaller temperature difference



# Annual Operating Ambient Temperatures

How might the design compressor inlet temperature affect annual performance  
Scenarios

1. Cycle operates every hour of year (baseload)
2. Cycle generates power proportionally to available DNI (CSP w/ small TES)



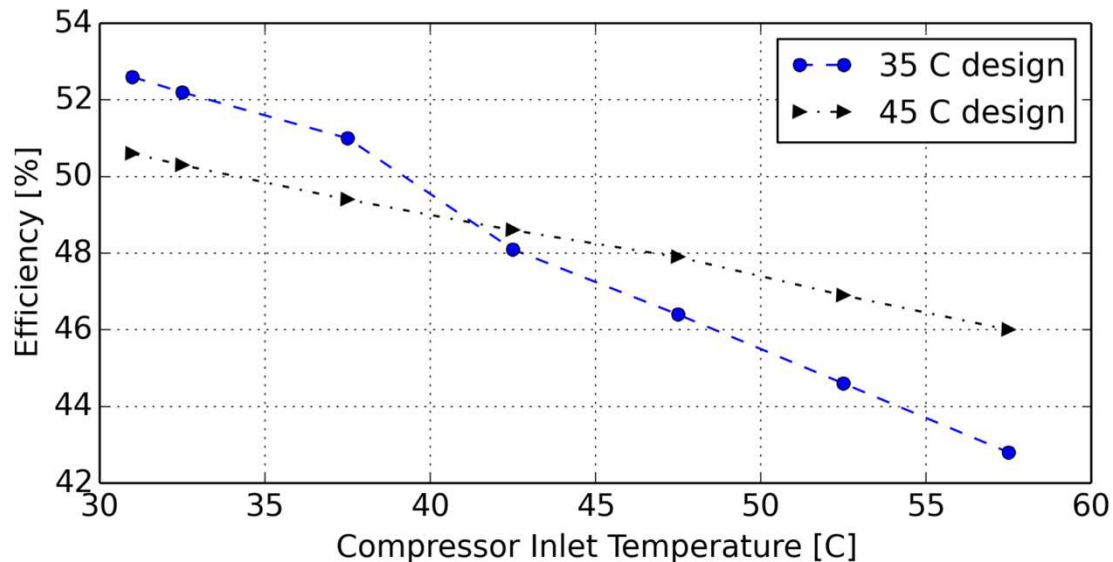
Annual Average Ambient Temperature = 19.5°C

Annual DNI – weighted Ambient Temp

$$= \sum_{i=1}^{8760} T_{amb,i} * \frac{DNI_i}{\sum_{j=1}^{8760} DNI_j} = 24.3^{\circ}\text{C}$$

# Annual Efficiency Estimates

- Design cycles for three compressor inlet temperatures
- Calculate off-design efficiencies at each PDF bin (assuming design point HTF mass flow rate & temperature)
- Don't allow compressor inlet temperatures colder than critical temperature



	Compressor inlet temperature 35°C (51.4%)	Compressor inlet temperature 45°C (48.0%)
Ambient temperature-weighted annual efficiency (-)	50.5%	49.5%
Direct normal irradiance-weighted annual efficiency (-)	49.3%	48.9%



# Conclusions

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- **Off-design cycle performance can affect the performance of the heat source**
  - Reduced thermal energy storage capacity
- **Cycle design should consider likely cycle *operating* conditions, especially ambient temperature *at generation***
  - Electricity peak pricing would drive “average” annual temperature even higher than DNI-weighted
- **Next steps:**
  - Air-cooler design and operation
  - Cost models as function of design
  - Economic analysis
- **Off-design optimization can be difficult**
  - Lot’s of infeasible points, especially at large HTF mass flow rates & hot ambient temps
  - Develop proxy model to screen solution space and generate guess values?

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# Thank You!

# Questions?