

Exceptional service in the national interest



The SEARCH Software Suite Code Capabilities and Experimental Comparison

The 5th International Symposium - Supercritical CO₂ Power Cycles

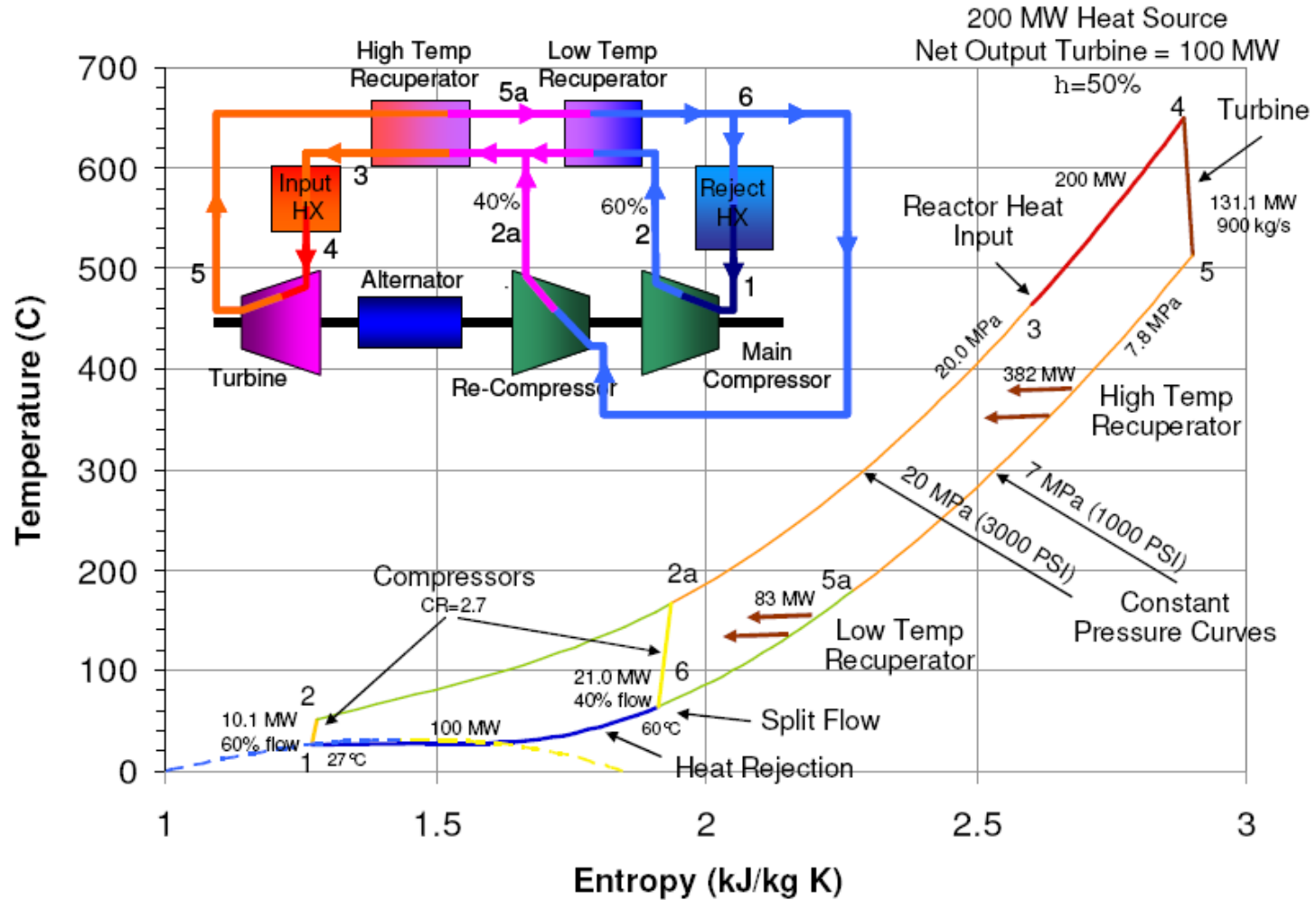
March 28-31, 2016, San Antonio, Texas, USA

*Carlson, M. D, Bell, C., Schalansky, C., Fleming, D. F., Rochau, G.



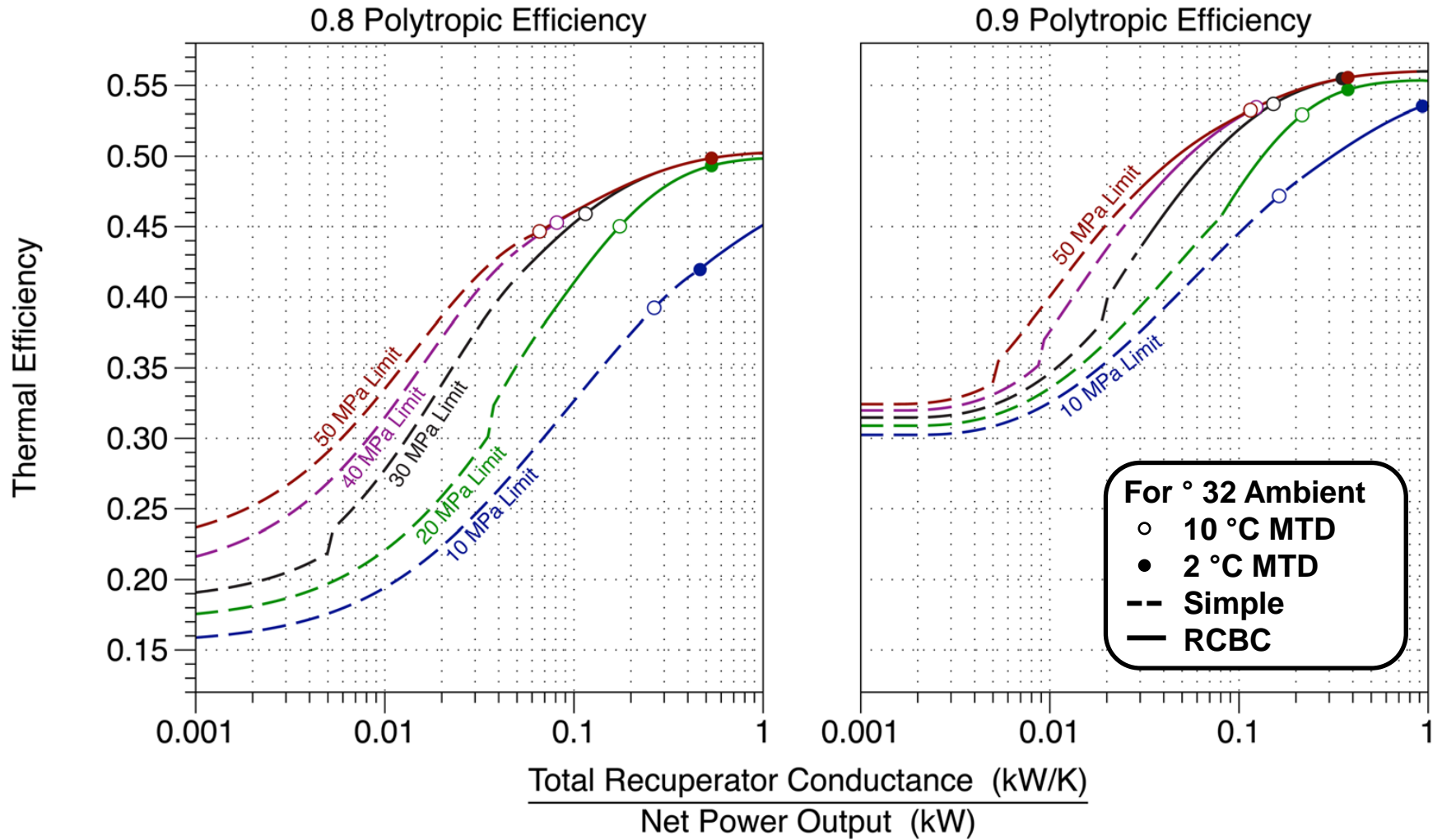
BACKGROUND

Supercritical CO₂ Brayton Cycle



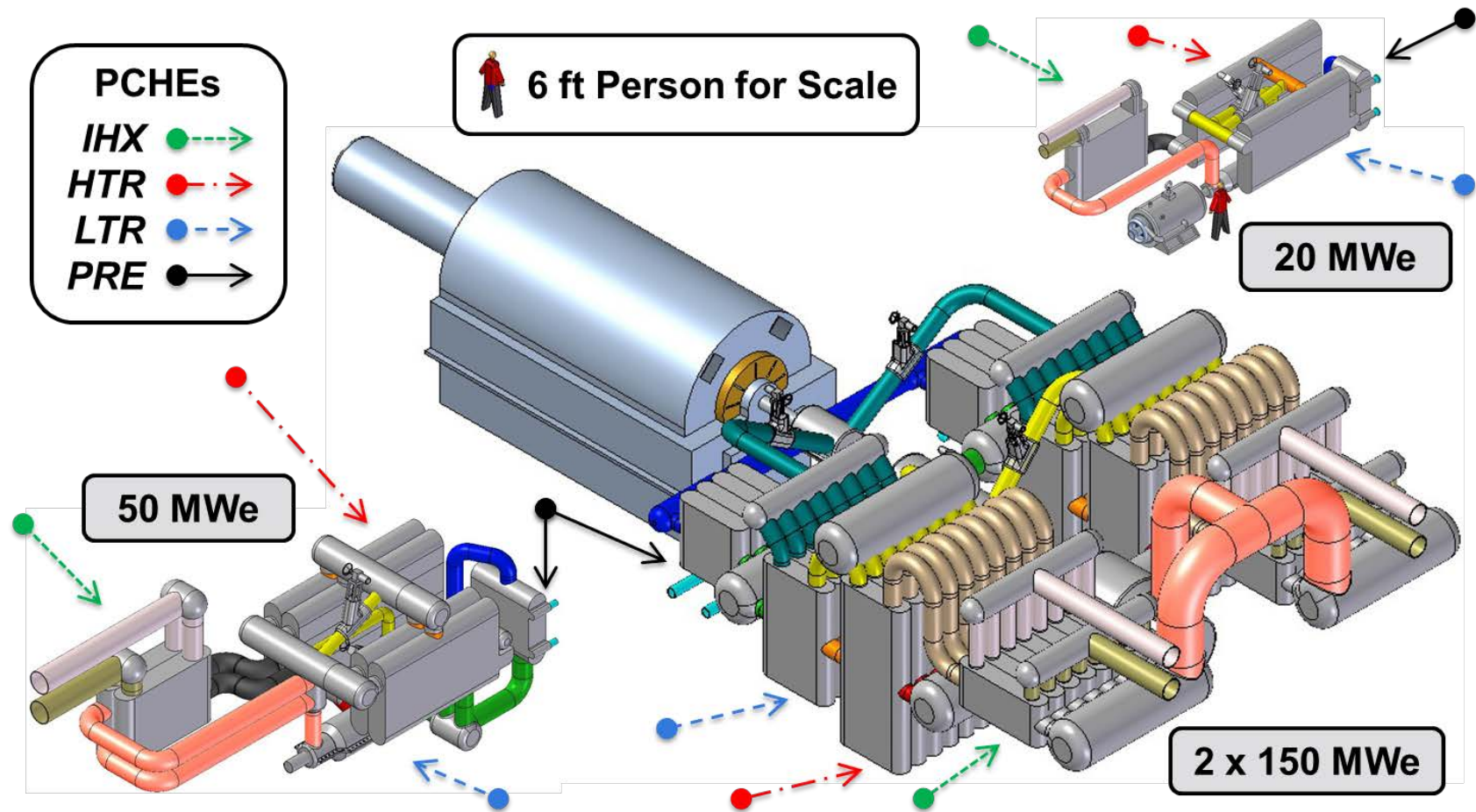
E. J. Parma, S. A. Wright, M. E. Vernon, D. D. Fleming, G. E. Rochau, A. J. Suo-Anttila, A. Al Rashdan, and P. V. Tsvetkov, "Supercritical CO₂ Direct Cycle Gas Fast Reactor (SC-GFR) Concept," Sandia National Laboratories, Albuquerque, NM, USA, SAND 2011-2525, May 2011.

sCO₂ Brayton Cycles Recuperation



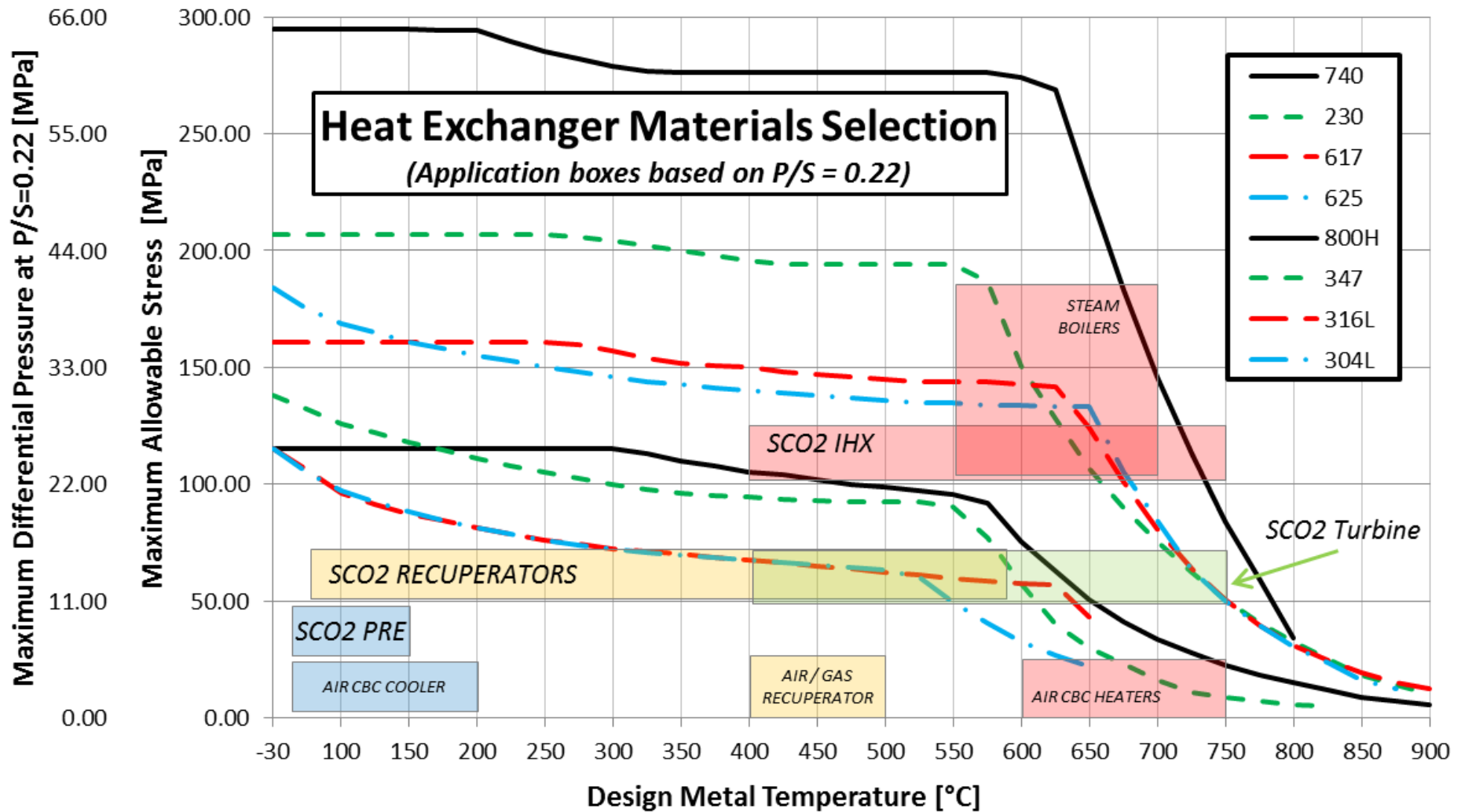
J. Dyreby, S. Klein, G. Nellis, and D. Reindl, "Design Considerations for Supercritical Carbon Dioxide Brayton Cycles With Recompression," *Journal of Engineering for Gas Turbines and Power*, vol. 136, no. 10, p. 101701, Jul. 2014.

Scalable SCO₂ CBC Systems



J.P. Gibbs, P. Hejzlar, & M.J. Driscoll. (2006). *Applicability of Supercritical CO₂ Power Conversion Systems to GEN IV Reactors* (Topical Report No. MIT-GFR-037) (p. 97). Cambridge, MA: Center for Advanced Nuclear Energy Systems MIT Department of Nuclear Science and Engineering.

Heat Exchanger Requirements



Approximate Cost Scaling

$$Cost = C_{ESDU} F_{mat} F_p F_i U A_{sp} P_{elec}$$

C_{ESDU} is the UA-specific cost value [\$/((kW/K))]

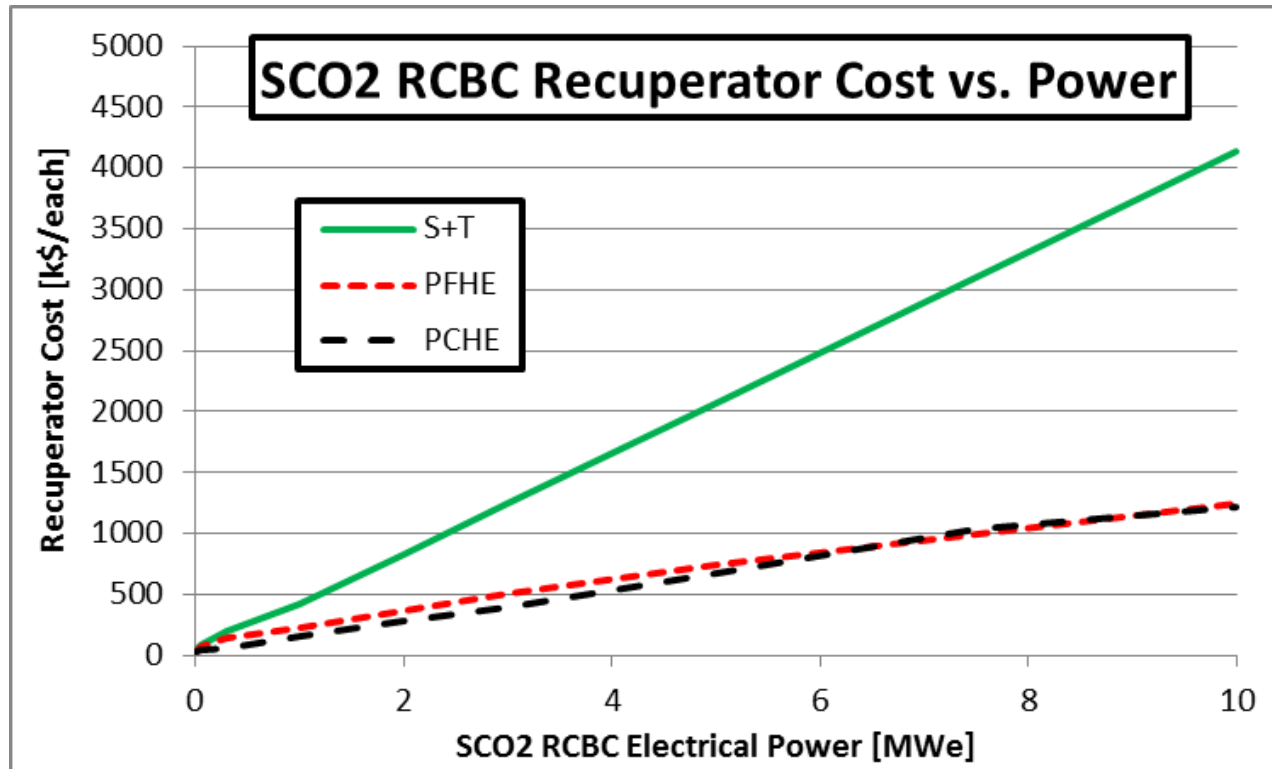
F_{mat} is a material cost factor

F_p is a pressure cost factor

F_i is an adjustment for inflation

$U A_{sp}$ is the cycle power-specific UA [kW/(K-MWe)]

P_{elec} is the cycle power level [MWe]



Development Gaps Addressed

Technology	Readiness Levels	from Direct Gas Combustion	from Exhaust Gas	from 3 MPa Helium	from Steam	from fluoride molten salts	from nitrate molten salts	from liquid sodium	from liquid lead-bismuth	from Heat Transfer Oil	from Combusting Particles	from Inert Solid Particles	from sunlight	Yet To Be Identified Resources	Advanced Nickel Alloys	Conventional Nickel Alloys	Austenitic Stainless Steels	to Water	to Humidified Air	TIT / °C	
		Molten Salt Reactor	NE			3											4-5	6-8	6-8	2	2-4
Sodium Fast Reactor (SFR)	NE					3										6-8	6-8	2	2-4	550	
Lead Fast Reactor (LFR)	NE						3								4-5	6-8	6-8	2	2-4	550 to 800	
Helium Gas Reactor (GFR, VHTR)	NE	4-5											2	3	4-5	6-8	6-8	2	2-4	700 to 1000	
Nuclear Shipboard Propulsion	NE															6-8	6-8			200 to 300	
Direct CSP Tower	EE									4-5					4-5	6-8	6-8	2	2-4	500 to 1000	
CSP Tower with Thermal Storage	EE				3	2		2	3						4-5	6-8	6-8	2	2-4	500 to 1000	
CSP Trough with Thermal Storage	EE				3			2								6-8	6-8	2	2-4	300 to 600	
CSP Dish Generator	EE					2		2				4-5			4-5	6-8			2-4	500 to 1000	
Direct Geothermal Plant	GT									2						6-8	6-8	2	2-4	100 to 300	
Indirect Geothermal Plant	GT		4-5													6-8	6-8	2	2-4	100 to 300	
Direct Natural Gas Combustion	FE	3-5	4										2	3	4-5	6-8	6-8	2	2-4	1100 to 1500	
Integrated Gasification Coal	FE	3-5											2	3	4-5	6-8	6-8	2	2-4	1100 to 1500	
Pulverized Coal Fluidized Bed	FE								4					3	4-5	6-8	6-8	2	2-4	550 to 900	
Waste Heat Recovery	FE		4													6-8	6-8	2	2-4	230 to 650	
Gas Turbine Bottoming	FE		4													6-8	6-8	2	2-4	230 to 650	
Municipal waste to energy	FE		4													6-8	6-8	2	2-4	230 to 650	
10 MWe Pilot	FE		4												4-5	6-8	6-8	2	2-4	550 to 700	
50 MWe Demonstration	FE		4												4-5	6-8	6-8	2	2-4	550 to 700	
		N/A	Gas			Liquid				Solid			>750	750	650	550				Recuperation MDMT / °C	sCO2 Cooling

NE, Peregrine CRADA NEUP NEUP
 SuNLAMP SERIUS
 NE, NEUPs NEUP, APOLLO, NE, CRADAs (VPE, Peregrine)

Development Gaps Addressed

Technology	Readiness Levels	from Direct Gas Combustion	from Exhaust Gas	from 3 MPa Helium	from Steam	from fluoride molten salts	from nitrate molten salts	from liquid sodium	from liquid lead-bismuth	from Heat Transfer Oil	from Combusting Particles	from Inert Solid Particles	from sunlight	Yet To Be Identified Resources	Advanced Nickel Alloys	Conventional Nickel Alloys	Austenitic Stainless Steels	to Water	to Humidified Air	TIT / °C	
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↑ ↑ ↑ ↑ ↑ ↑ ↑
 NE, Peregrine CRADA NEUP NEUP SuNLAMP SERIUS NE, NEUPs NEUP, APOLLO, NE, CRADAs (VPE, Peregrine)

Key Development Metrics

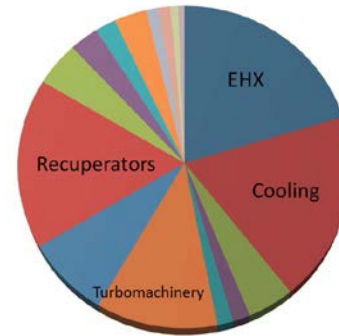
■ Economics

- How do we optimize designs and reduce fabrication costs?
 - Efficiency vs. Effectiveness
 - Efficiency vs. pressure drop
 - Manufacturing techniques

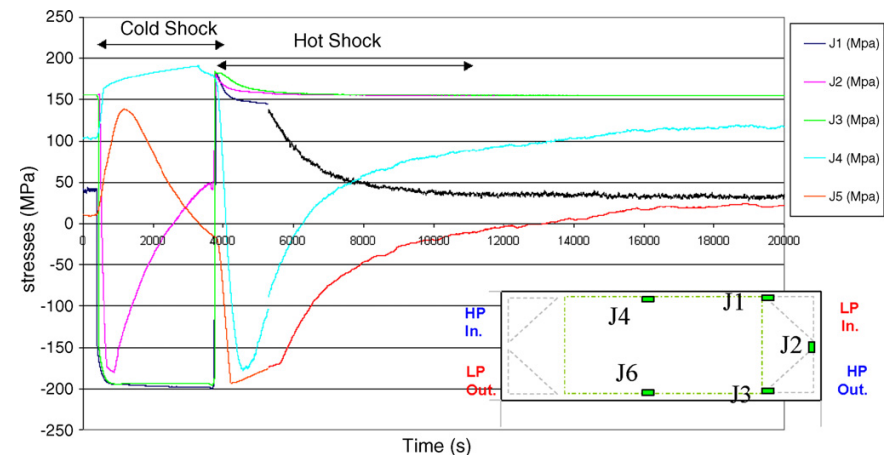
■ Failure Modes

- How do we accommodate thermal stress and fatigue?
 - Pressure containment (material vs. geometry)
 - Higher Temperatures
 - Corrosion and fouling

Echogen



“[A] 30% reduction in HX cost would have [a] meaningful impact on system cost.”



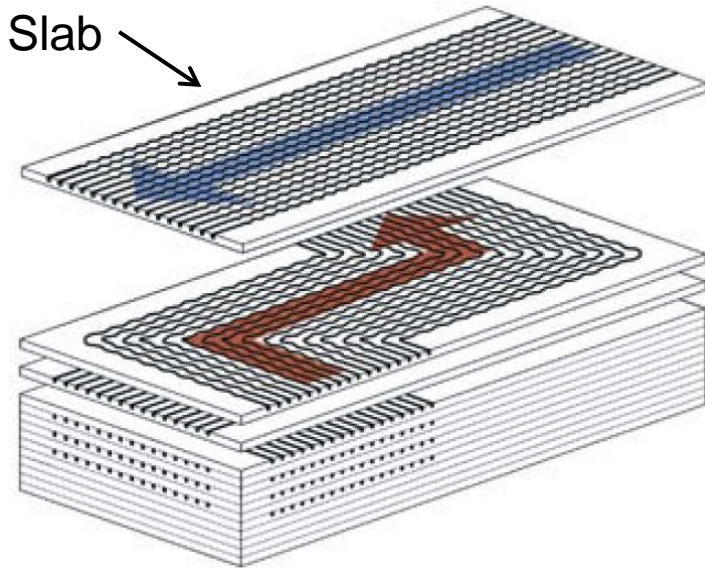
[1] T. Held, “Performance & cost targets for sCO₂ heat exchangers,” presented at the National Energy Technology Laboratory - EPRI Workshop on Heat Exchangers for Supercritical CO₂ Power Cycles, San Diego, CA, USA, 15-Oct-2015.

[2] F. Pra, P. Tochon, C. Mauget, J. Fokkens, and S. Willemsen, “Promising designs of compact heat exchangers for modular HTRs using the Brayton cycle,” *Nuclear Engineering and Design*, vol. 238, no. 11, pp. 3160–3173, Nov. 2008.

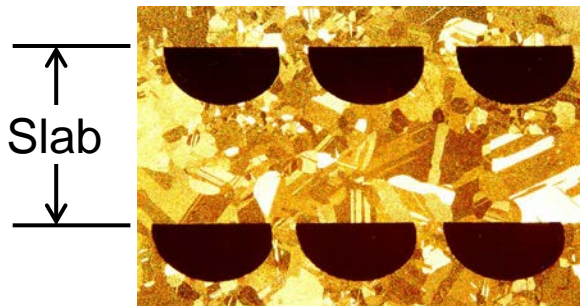
MCHE DESIGN ALGORITHM

The Printed Circuit Heat Exchanger

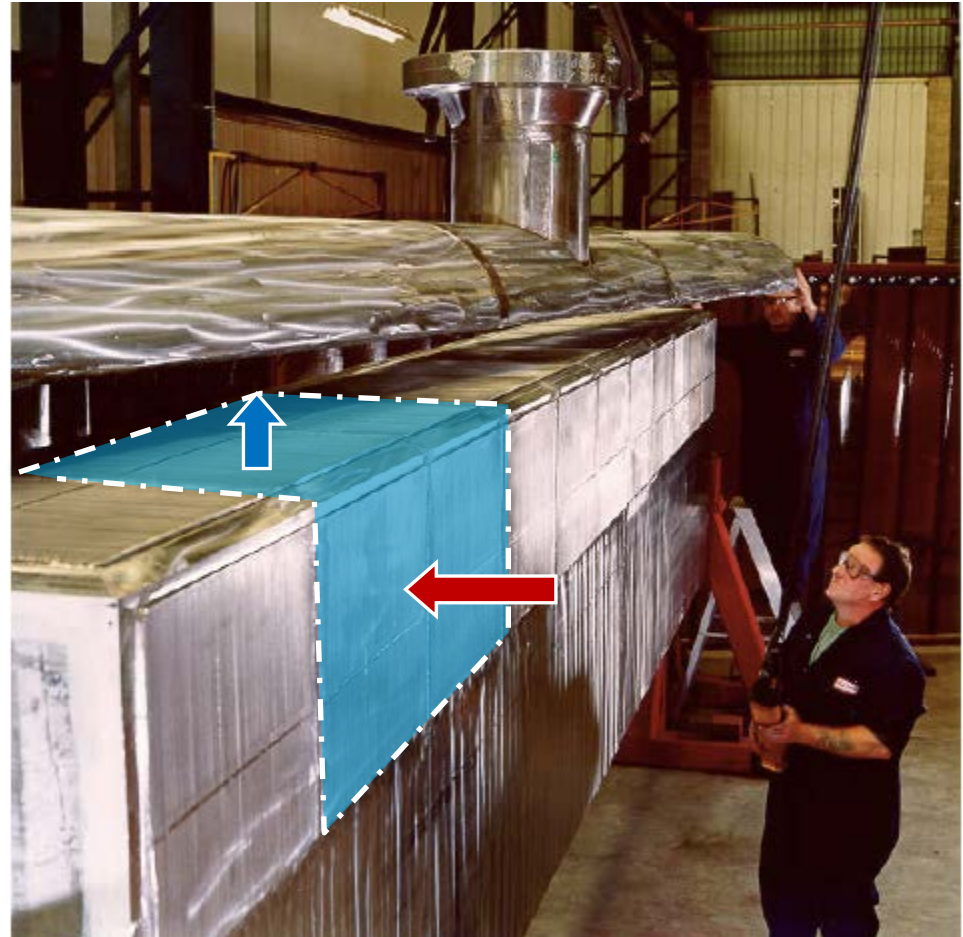
Heat Exchanger Core



Diffusion Bonding



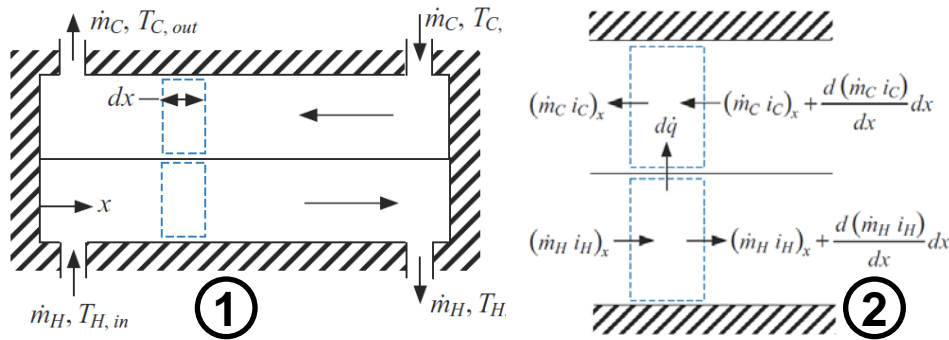
Core and Manifold Assembly



Methods of Heat Exchanger Design

- Effectiveness – NTU / LMTD Methods
 - Uses analytical solutions to various heat exchanger configurations
 - Explicit solution method with reasonable accuracy
- Compact Heat Exchanger Correlations
 - Correlations developed from experimental data for several geometries
 - Explicit accurate solution but for a limited number of correlations
- Sub-Heat Exchanger Method
 - Implements method 1 multiple times to capture property variations
 - Implicit solution needing fewer nodes / iterations than 1D solutions
- 1D Channel Solutions
 - Simulates channels identically or in parallel to determine performance
 - Iterative, intensive solution with the highest accuracy and flexibility
- More complex methods also exist (2D, 3D, CFD)

Effectiveness - NTU Derivation



$$\textcircled{3} \quad \frac{dT_H}{dx} = -\frac{UA}{L\dot{m}_H c_H} (T_H - T_C)$$

$$\textcircled{3} \quad \frac{dT_C}{dx} = \frac{UA}{L\dot{m}_C c_C} (T_H - T_C)$$

$$\textcircled{4} \quad \ln\left(\frac{T_{H,out} - T_{C,in}}{T_{H,in} - T_{C,out}}\right) = -UA\left(\frac{1}{\dot{C}_H} - \frac{1}{\dot{C}_C}\right)$$

$$\textcircled{5} \quad NTU = \begin{cases} \frac{\ln\left[\frac{1 - \varepsilon C_R}{1 - \varepsilon}\right]}{1 - C_R} & \text{for } C_R < 1 \\ \frac{\varepsilon}{1 - \varepsilon} & \text{for } C_R = 1 \end{cases}$$

1. Assume:

- Externally adiabatic
- Incompressible flow
- Constant specific heat capacity
- Enthalpy independent of pressure

2. Finite difference method

- Establish control volumes

3. Coupled differential equations

- Hot and cold-side temperatures

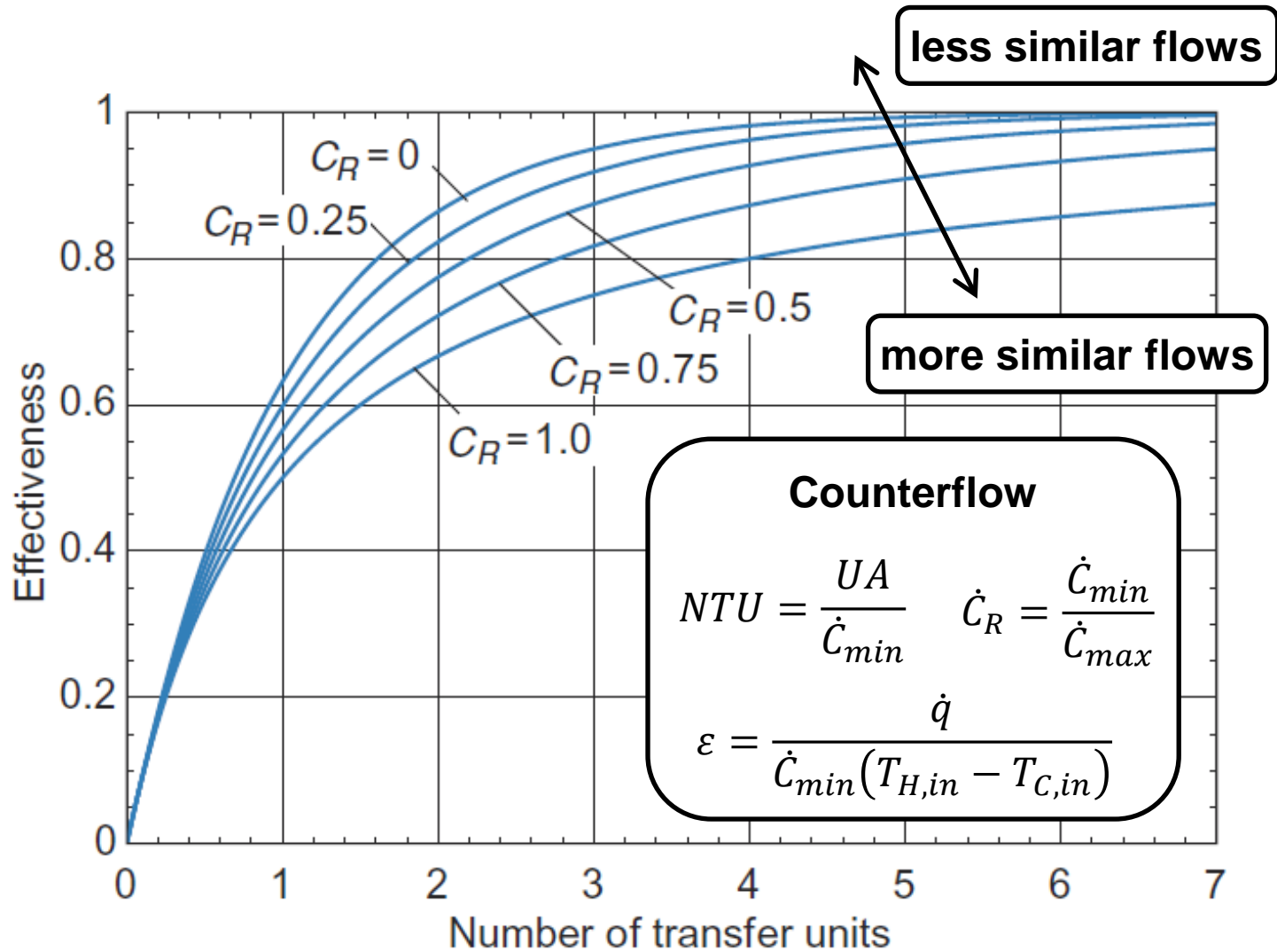
4. General solution

- Relate temperatures, UA, \dot{C} 's

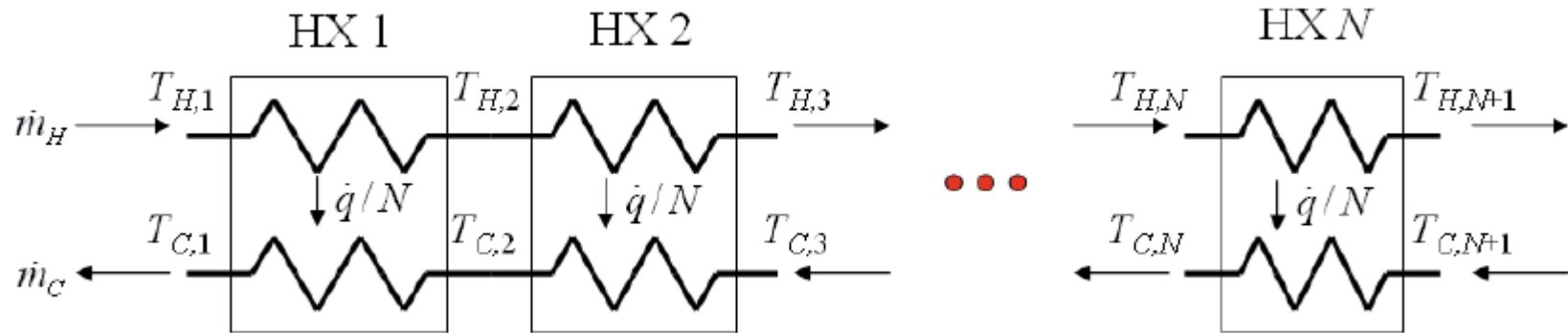
5. Effectiveness-NTU formulation

- $NTU = \frac{UA}{\dot{C}_{min}}$, and $\dot{C}_R = \frac{\dot{C}_{min}}{\dot{C}_{max}}$
- $\varepsilon = q / [\dot{C}_{min}(T_{H,in} - T_{C,in})]$

Effectiveness - NTU Solution



Sub-Heat Exchanger Method



$$\dot{C}_i = \dot{m} \frac{h_i - h_{i+1}}{\text{MAX}(1e-4 \text{ [K]}, |T_i - T_{i+1}| \text{ SIGN}(h_i - h_{i+1}))}$$

$$\varepsilon_i = \frac{\dot{q}_i}{\text{MIN}(\dot{C}_{A,i}, \dot{C}_{B,i})(T_{A,i} - T_{B,i+1})}$$

$$NTU_i = \begin{cases} \frac{\ln \left[\frac{(1 - \varepsilon C_R)}{1 - \varepsilon} \right]}{1 - C_R} & \text{for } C_R < 1 \\ \frac{\varepsilon}{1 - \varepsilon} & \text{for } C_R = 1 \end{cases}$$

$$UA_i = NTU_i \text{ MIN}(\dot{C}_{A,i}, \dot{C}_{B,i})$$

- Divide into a series of HXers
- Extends e-NTU method
- Assumptions apply to each sub-heat exchanger (Δx)
- Best method to obtain UA accurately and quickly with variable property flows

ASME BPVC Design Equations

$$S_{m,stay} = \frac{Ph}{2t_4} \left[\frac{6 + K(11 - \alpha^2)}{3 + 5K} \right]$$

$$S_{m,1} = \frac{Ph}{2t_1} \left[3 - \frac{6 + K(11 - \alpha^2)}{3 + 5K} \right]$$

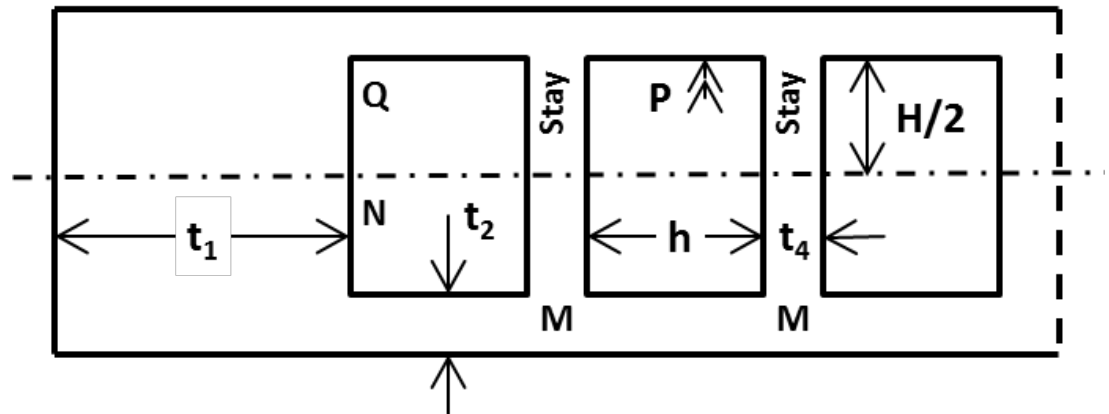
$$S_{m,2} = \frac{PH}{2t_2}$$

$$S_{b,stay} = 0$$

Section of a printed circuit heat exchanger



Vessel sketch from the ASME BPVC VIII-1-13-2(a)(8)



$$(S_{b,1})_{at N} = \frac{Pc_1}{24I_1} \left[-3H^2 + 2h^2 \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right) \right]$$

$$(S_{b,1})_{at Q} = \frac{Ph^2 c_1}{12I_1} \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right)$$

$$(S_{b,2})_{at M} = \frac{Ph^2 c_2}{12I_2} \left[\frac{3 + K(6 - \alpha^2)}{3 + 5K} \right]$$

$$(S_{b,2})_{at Q} = \frac{Ph^2 c_2}{12I_2} \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right)$$

Non-Dimensionalized Equations

Section of a printed circuit heat exchanger

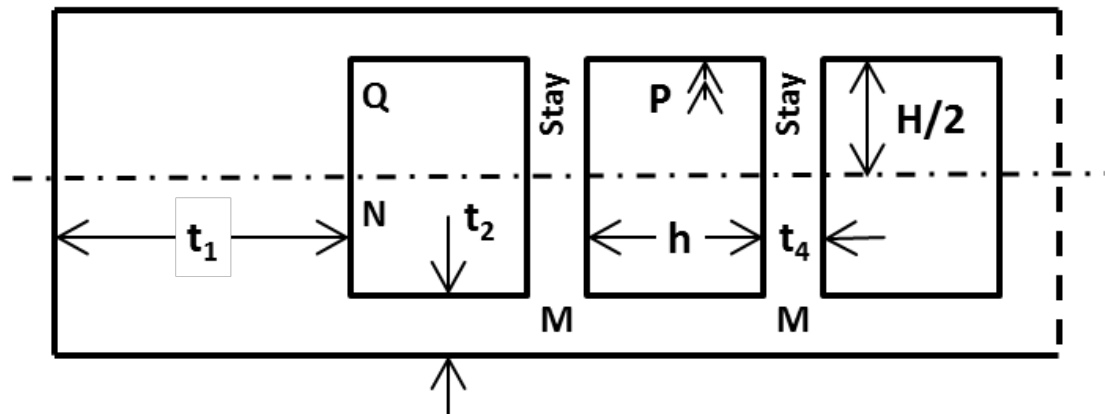
$$\frac{P}{SE} \leq \left(\frac{1}{wf} - 1 \right)$$

$$\frac{P}{S} \leq 2 \left(\frac{1}{df} - 1 \right)$$



Vessel sketch from the ASME BPVC VIII-1-13-2(a)(8)

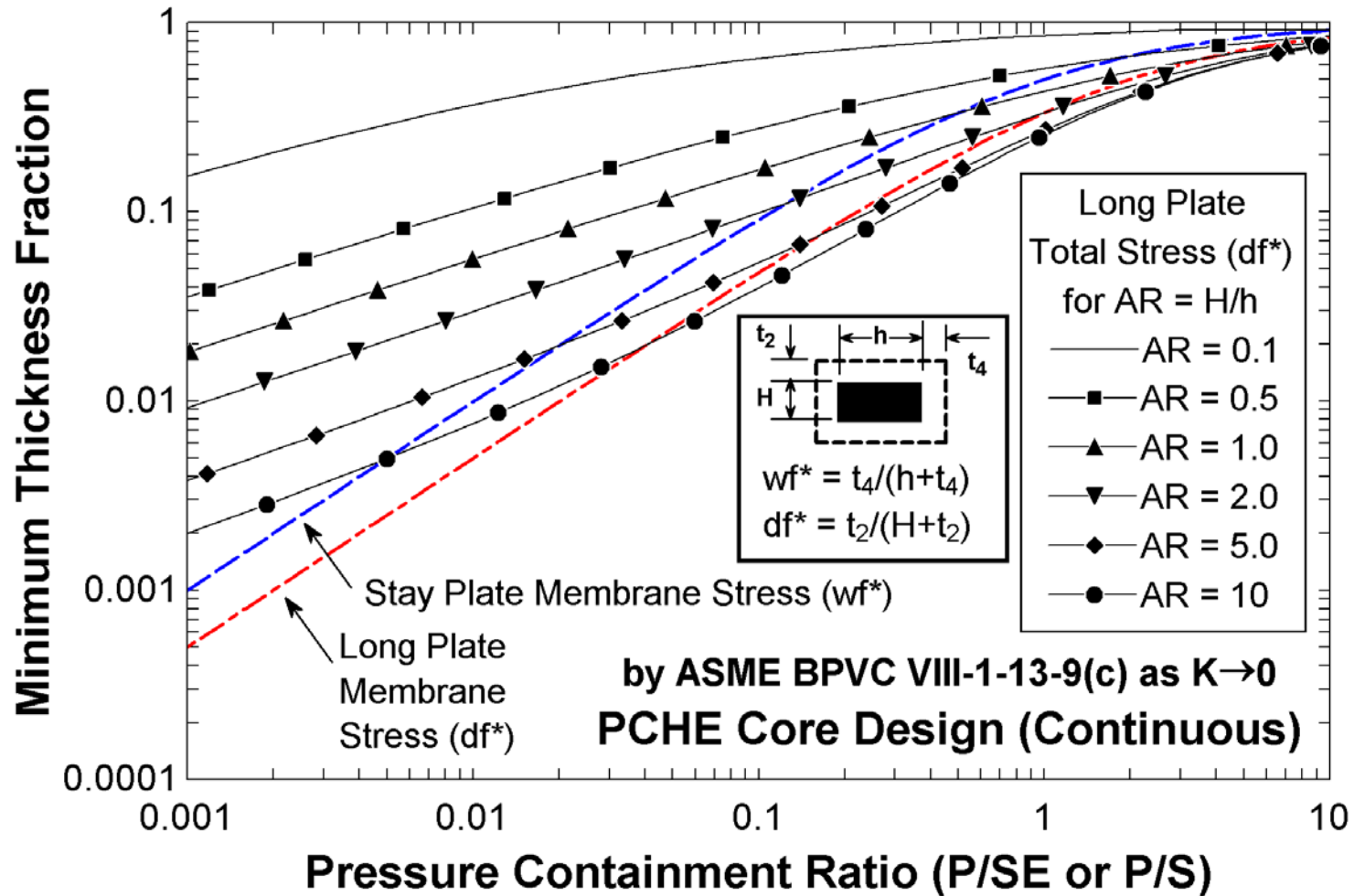
$$\frac{P}{S} \leq 3 \left(\frac{df}{1-df} + \frac{1}{AR^2} \left(\frac{df}{1-df} \right)^2 \right)^{-1}$$



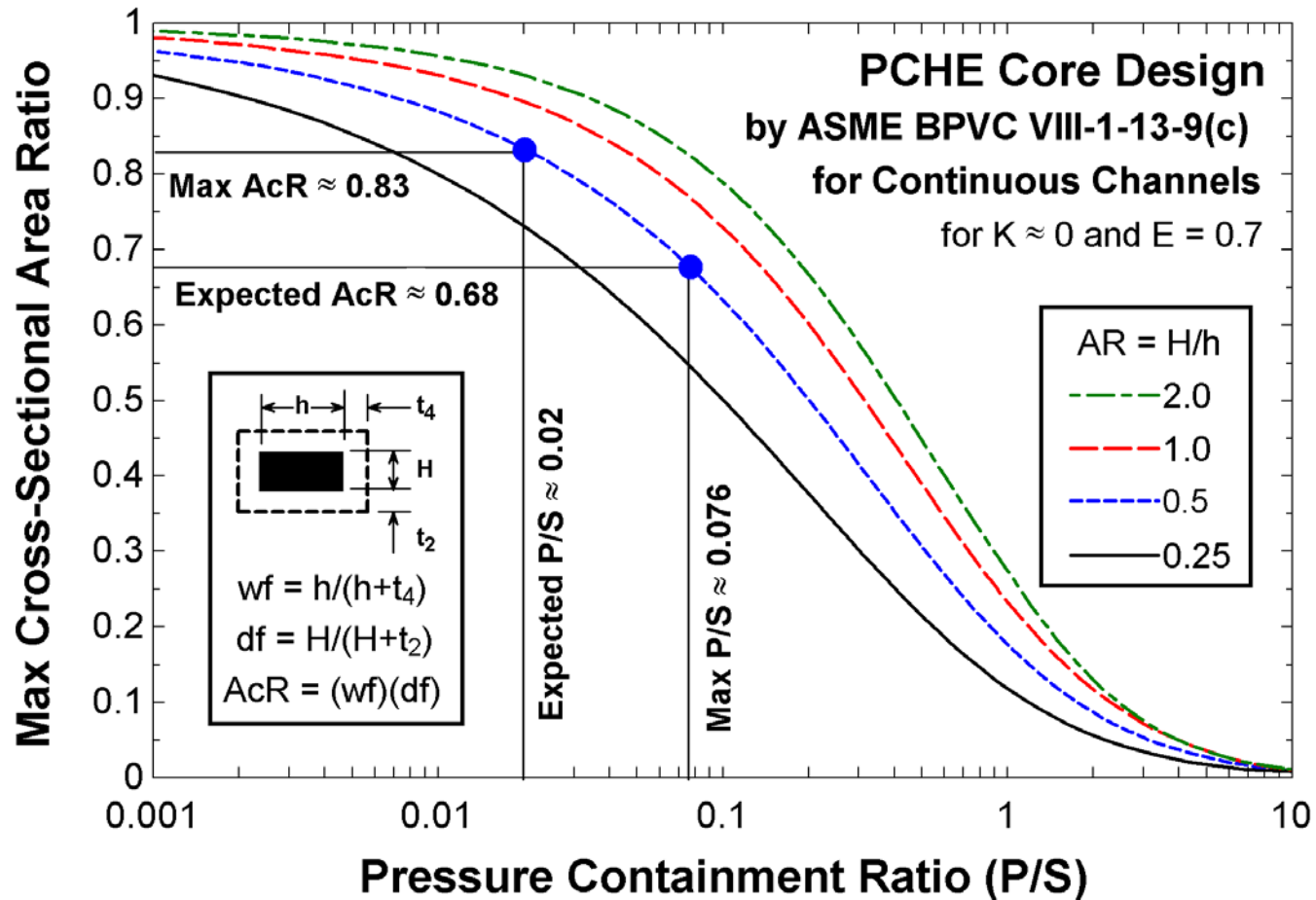
$$wf = \frac{h}{h + t_4}$$

$$df = \frac{H}{H + t_2}$$

PCHE Core Pressure Containment

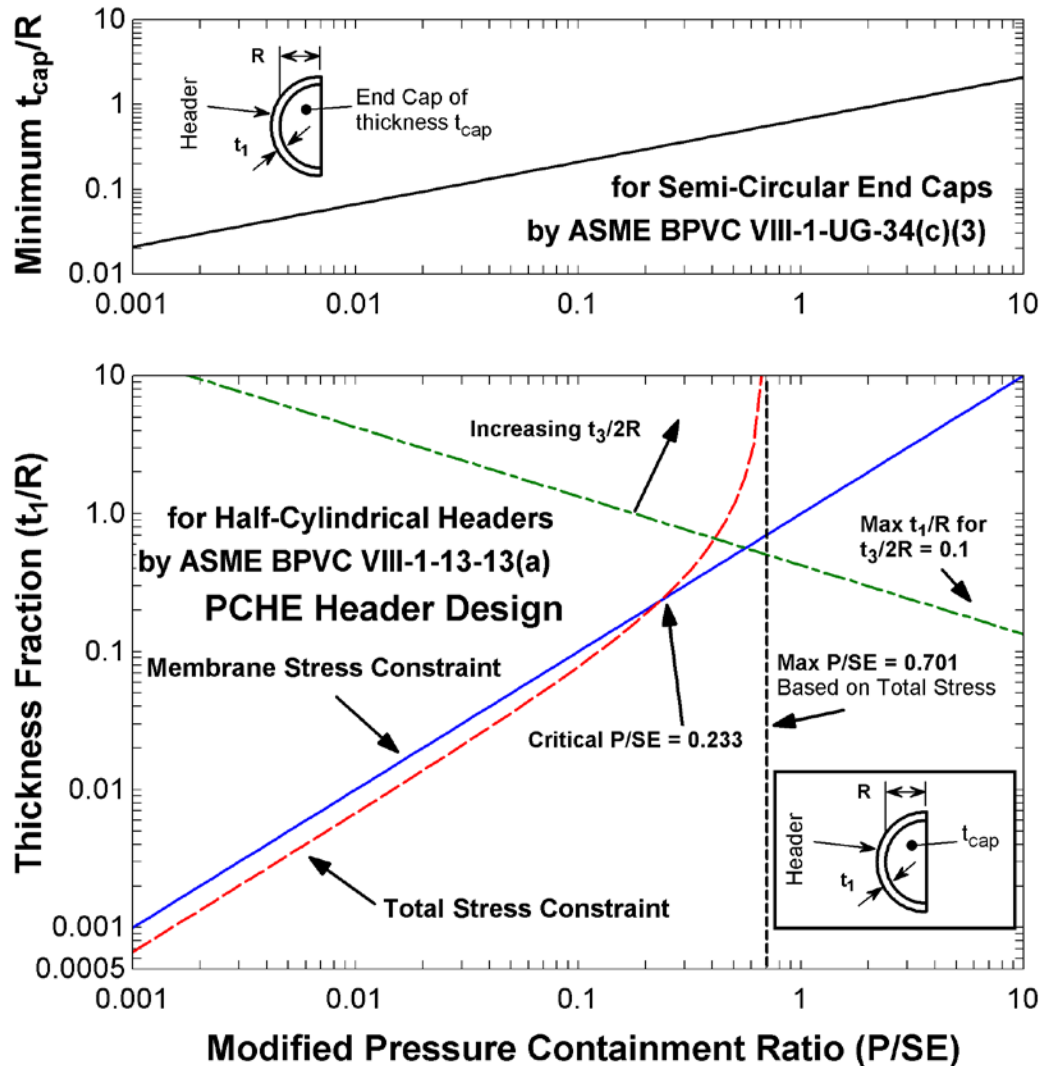


PCHE Core Pressure Containment



Carlson, M. (2012). *Measurement and Analysis of the Thermal and Hydraulic Performance of Several Printed Circuit Heat Exchanger Channel Geometries* (Master of Science). University of Wisconsin - Madison, Madison, WI.

Half-Cylindrical Headers



Thermal-Hydraulics

$$\Delta x_i = UA_i \left(\underbrace{\frac{1}{h_{A,i} N_{ch,A} \rho_{ch,A}}}_{\textcircled{1}} + \underbrace{\frac{R_{f,A,i}}{N_{ch,A} \rho_{ch,A}}}_{\textcircled{2}} + \underbrace{\frac{t_m}{k_{m,i} W}}_{\textcircled{3}} + \underbrace{\frac{1}{h_{B,i} N_{ch,B} \rho_{ch,B}}}_{\textcircled{4}} + \underbrace{\frac{R_{f,B,i}}{N_{ch,B} \rho_{ch,B}}}_{\textcircled{5}} \right)$$

1. Sub-heat exchanger length
2. Sub-heat exchanger conductance-area product
3. Convective thermal resistances
4. Conductive thermal resistance
5. Fouling thermal resistances

PCHE Design Software

- Sub-hxer model
- ASME BPVC
- Single, two-phase, supercritical flows
- Over 400 fluids

Document Number: RC1		Revision Number: 1		Heat Exchanger Data Sheet																																	
Side A (straight)		Side B (Z-side)		solutionScope= All design steps (mech, thermo, TH)																																	
<div style="display: flex; justify-content: space-between;"> Calculate Save Inputs Load Inputs </div>																																					
<p>Step 1. Side A and B Stream Compositions (by mass %)</p> <p>Choose the fluid set: Refprop Fluid(s)</p> <table border="1"> <tr> <td>100 (%)</td> <td>WATER.FLD</td> <td>100 (%)</td> <td>R1233ZD.FLD</td> </tr> <tr> <td>0 (%)</td> <td>ACETONE.FLD</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>Nitrogen.flid</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>co2.flid</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>Propane.FLD</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>BUTANE.FLD</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>IPENTANE.FLD</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> <tr> <td>0 (%)</td> <td>HEXANE.FLD</td> <td>0 (%)</td> <td>1BUTENE.FLD</td> </tr> </table> <p>Fouling (val A, val B) CO2 vapor CO2 vapor</p> <p>Fouling Factor: $R_{f,A} = 0.0001 \text{ [m}^2\text{]}$ $R_{f,B} = 0.0001 \text{ [m}^2\text{]}$</p>						100 (%)	WATER.FLD	100 (%)	R1233ZD.FLD	0 (%)	ACETONE.FLD	0 (%)	1BUTENE.FLD	0 (%)	Nitrogen.flid	0 (%)	1BUTENE.FLD	0 (%)	co2.flid	0 (%)	1BUTENE.FLD	0 (%)	Propane.FLD	0 (%)	1BUTENE.FLD	0 (%)	BUTANE.FLD	0 (%)	1BUTENE.FLD	0 (%)	IPENTANE.FLD	0 (%)	1BUTENE.FLD	0 (%)	HEXANE.FLD	0 (%)	1BUTENE.FLD
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<p>Step 2. Specify Fluid Flow Rates</p> <table border="1"> <tr> <td>Flow Rate (mass A, mass B)</td> <td>$\dot{m}_A = 80.4 \text{ [kg/s]}$</td> <td>$\dot{m}_B = 34.9 \text{ [kg/s]}$</td> </tr> <tr> <td></td> <td>$\dot{V}_A = \text{'''''' [m}^3\text{/s]}$</td> <td>$\dot{V}_B = \text{'''''' [m}^3\text{/s]}$</td> </tr> </table>						Flow Rate (mass A, mass B)	$\dot{m}_A = 80.4 \text{ [kg/s]}$	$\dot{m}_B = 34.9 \text{ [kg/s]}$		$\dot{V}_A = \text{'''''' [m}^3\text{/s]}$	$\dot{V}_B = \text{'''''' [m}^3\text{/s]}$																										
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<p>Step 3. Specify Inlet State for Sides A and B</p> <table border="1"> <tr> <td>Inlet States (T_A, P_A, T_B, P_B)</td> <td></td> <td></td> </tr> <tr> <td>Inlet Pressure</td> <td>$P_A = 7.170E+08 \text{ [Pa]}$</td> <td>$P_B = 2.330E+07 \text{ [Pa]}$</td> </tr> <tr> <td>Inlet Temperature</td> <td>$T_{A,in} = 572.8 \text{ [K]}$</td> <td>$T_{B,in} = 378.1 \text{ [K]}$</td> </tr> <tr> <td>Inlet Quality ($\pm 100 = \text{sup or sub}$)</td> <td>$Q_{A,in} = \text{''''}$</td> <td>$Q_{B,in} = \text{''''}$</td> </tr> <tr> <td>Outlet Pressure</td> <td>$P_{A,out} = \text{'''''''' [Pa]}$</td> <td>$P_{B,out} = \text{'''''''' [Pa]}$</td> </tr> <tr> <td>Outlet Temperature</td> <td>$T_{A,out} = \text{'''' [K]}$</td> <td>$T_{B,out} = 504.2 \text{ [K]}$</td> </tr> <tr> <td>Outlet Quality ($\pm 100 = \text{sup or sub}$)</td> <td>$Q_{A,out} = \text{''''}$</td> <td>$Q_{B,out} = \text{''''}$</td> </tr> </table>						Inlet States (T_A, P_A, T_B, P_B)			Inlet Pressure	$P_A = 7.170E+08 \text{ [Pa]}$	$P_B = 2.330E+07 \text{ [Pa]}$	Inlet Temperature	$T_{A,in} = 572.8 \text{ [K]}$	$T_{B,in} = 378.1 \text{ [K]}$	Inlet Quality ($\pm 100 = \text{sup or sub}$)	$Q_{A,in} = \text{''''}$	$Q_{B,in} = \text{''''}$	Outlet Pressure	$P_{A,out} = \text{'''''''' [Pa]}$	$P_{B,out} = \text{'''''''' [Pa]}$	Outlet Temperature	$T_{A,out} = \text{'''' [K]}$	$T_{B,out} = 504.2 \text{ [K]}$	Outlet Quality ($\pm 100 = \text{sup or sub}$)	$Q_{A,out} = \text{''''}$	$Q_{B,out} = \text{''''}$											
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Inlet Pressure	$P_A = 7.170E+08 \text{ [Pa]}$	$P_B = 2.330E+07 \text{ [Pa]}$																																			
Inlet Temperature	$T_{A,in} = 572.8 \text{ [K]}$	$T_{B,in} = 378.1 \text{ [K]}$																																			
Inlet Quality ($\pm 100 = \text{sup or sub}$)	$Q_{A,in} = \text{''''}$	$Q_{B,in} = \text{''''}$																																			
Outlet Pressure	$P_{A,out} = \text{'''''''' [Pa]}$	$P_{B,out} = \text{'''''''' [Pa]}$																																			
Outlet Temperature	$T_{A,out} = \text{'''' [K]}$	$T_{B,out} = 504.2 \text{ [K]}$																																			
Outlet Quality ($\pm 100 = \text{sup or sub}$)	$Q_{A,out} = \text{''''}$	$Q_{B,out} = \text{''''}$																																			
<p>Step 4. Specify the Allowable Pressure Drop</p> <table border="1"> <tr> <td>Pressure Drop</td> <td>$dP_{sum,A} = \text{'''''' [Pa]}$</td> <td>$dP_{sum,B} = \text{'''''' [Pa]}$</td> </tr> <tr> <td>Drop / Operating Pressure</td> <td>$dP_{A,\%} = \text{'''''' [%]}$</td> <td>$dP_{B,\%} = \text{'''''' [%]}$</td> </tr> </table>						Pressure Drop	$dP_{sum,A} = \text{'''''' [Pa]}$	$dP_{sum,B} = \text{'''''' [Pa]}$	Drop / Operating Pressure	$dP_{A,\%} = \text{'''''' [%]}$	$dP_{B,\%} = \text{'''''' [%]}$																										
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<p>Step 5. Specify Header Orientations</p> <table border="1"> <tr> <td>Header Axis Orientation</td> <td>Vertical</td> <td>Vertical</td> </tr> </table>						Header Axis Orientation	Vertical	Vertical																													
Header Axis Orientation	Vertical	Vertical																																			
<p>Step 7. Specify Core Channel Geometry</p> <table border="1"> <tr> <td>Channel Width</td> <td>$w_A = 0.001289 \text{ [m]}$</td> <td>$w_B = 0.001289 \text{ [m]}$</td> </tr> <tr> <td>Channel Depth</td> <td>$d_A = 0.000763 \text{ [m]}$</td> <td>$d_B = 0.000763 \text{ [m]}$</td> </tr> </table>						Channel Width	$w_A = 0.001289 \text{ [m]}$	$w_B = 0.001289 \text{ [m]}$	Channel Depth	$d_A = 0.000763 \text{ [m]}$	$d_B = 0.000763 \text{ [m]}$																										
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Channel Depth	$d_A = 0.000763 \text{ [m]}$	$d_B = 0.000763 \text{ [m]}$																																			
<p>Summary of PCHE Design</p> <p>Job Number: RC1</p> <p>Run Date: ''''''''</p> <p>Job Title: Test</p> <p>Code Used: ASME Code Section VIII Division 1 - 2013</p> <p>Core Length (bet. headers): $L = \text{'''''' [m]}$</p> <p>Core Width (bet. headers): $W = \text{'''''' [m]}$</p> <p>Core Height: $H = \text{'''''' [m]}$</p> <p>Core Cross-Section (H x W): $A_c = \text{'''''' [m}^2\text{]}$</p> <p>Side A Surface Area: $A_{s,A} = \text{'''''' [m}^2\text{]}$</p> <p>Side B Surface Area: $A_{s,B} = \text{'''''' [m}^2\text{]}$</p> <p>Wetted Volume (core + hdrs): $Vol_{wet} = \text{'''''''' [m}^3\text{]}$</p> <p>Metal Mass (core + hdrs): $M = \text{'''' [kg]}$</p> <p>Heat Transfer Rate (Duty): $\dot{q} = \text{'''''''' [W]}$</p> <p>Conductance-Area Product: $UA_{sum} = \text{'''''' [W/K]}$</p> <p>Side A MAWP: $MAWP_A = \text{'''''''' [Pa]}$</p> <p>Side B MAWP: $MAWP_B = \text{'''''''' [Pa]}$</p> <p>MAWT (same as MDMT): $MAWT = \text{'''''' [K]}$</p> <p>Number of Etched Plate Pairs: $N_{rows} = \text{'''' [-]}$</p> <p>Side A Channels per Plate: $N_{chp,A} = \text{'' [-]}$</p> <p>Side B Channels per Plate: $N_{chp,B} = \text{'' [-]}$</p> <p>Number of Un-etched Plates: $N_{ex} = \text{'' [-]}$</p>																																					
<p>Step 9. Other Controls</p> <table border="1"> <tr> <td>Max Active core volume width</td> <td>$W_{ACV,max} = 0.1597 \text{ [m]}$</td> </tr> <tr> <td>Max Active core volume height</td> <td>$H_{ACV,max} = 2.5 \text{ [m]}$</td> </tr> <tr> <td>Extra width provided</td> <td>$W_{extra} = 0 \text{ [m]}$</td> </tr> <tr> <td>Extra height provided</td> <td>$H_{extra} = 0 \text{ [m]}$</td> </tr> </table>						Max Active core volume width	$W_{ACV,max} = 0.1597 \text{ [m]}$	Max Active core volume height	$H_{ACV,max} = 2.5 \text{ [m]}$	Extra width provided	$W_{extra} = 0 \text{ [m]}$	Extra height provided	$H_{extra} = 0 \text{ [m]}$																								
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Extra height provided	$H_{extra} = 0 \text{ [m]}$																																				
<p>Step 6. Specify the Performance Measure</p> <p>Choose Measure Type: Side B Outlet Temperature</p> <p>Diffusion Bonding Joint Efficiency: $E_{DB} = 0.7 \text{ [-]}$</p> <p>Header Cylinder Joint Efficiency: $E_{cyl} = 0.7 \text{ [-]}$</p>																																					

PROTOTYPE PCHE DESIGN

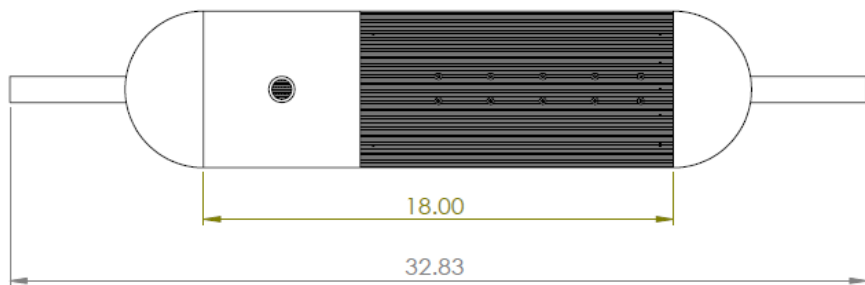
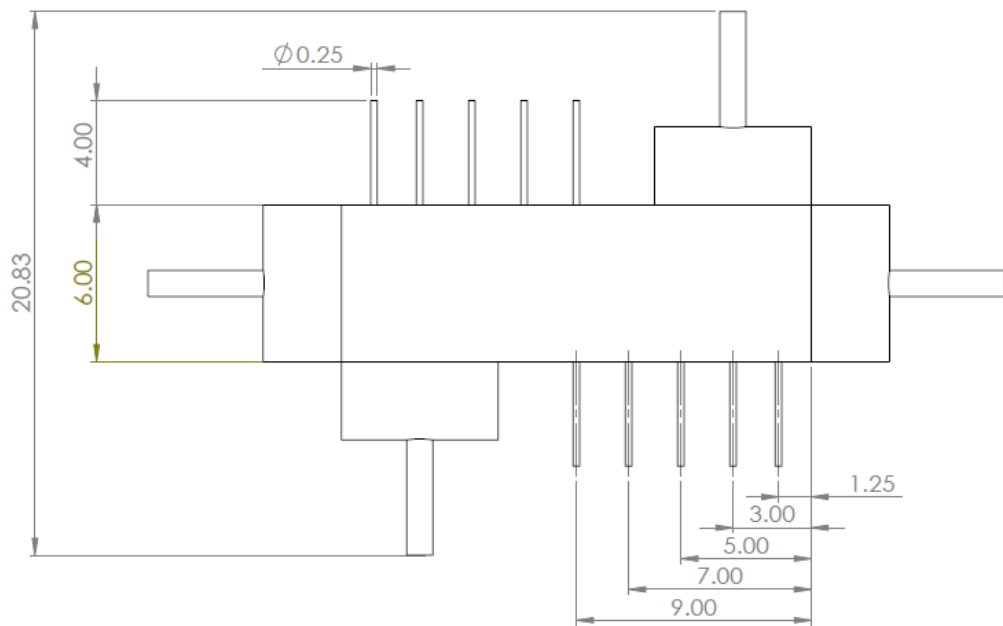
Heat Exchanger Data Sheet

Parameter	Unit	Side A (Straight)	Side B (Z)
<i>Fluid</i>	-	water	water
<i>Mass Flow Rate</i>	kg/s (lbm/hr)	1.5 (12000)	1.5 (12000)
<i>Volumetric Flow Rate</i>	m ³ /s (gpm)	1.5e-3 (24)	1.5e-3 (24)
<i>Inlet Temperature</i>	°C (°F)	82 (180)	37 (98)
<i>Inlet Pressure</i>	kPa (psi)	300 (44)	300 (44)
<i>Pressure Drop</i>	kPa (psi)	55 (7.9)	62 (9.0)
<i>Fouling Factor</i>	m ² -K/W	8e-5	8e-5
<i>MAWP</i>	MPa (psi)	20 (2900)	
<i>MAWT</i>	°C (°F)	550 (1000)	
<i>Duty</i>	kW _{th} (Btu/hr)	103 (350000)	
<i>Height x Width x Length</i>	m (in)	0.15 x 0.15 x 0.46 (6 x 6 x 18)	
<i>Active Surface Area</i>	m ² (in ²)	1.2 (13)	
<i>Material</i>	-	316L Stainless Steel	

Design for Multiple Phases

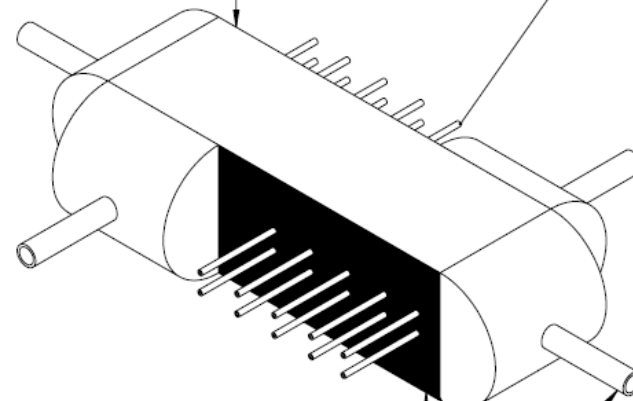
1. Pressure Containment
 - Evaluated by hydrostatic pressure testing
2. Single-phase Thermal Hydraulics
 - Evaluated in the NESL water test loop
3. Supercritical Thermal Hydraulics
 - Evaluated in the NESL sCO₂ loop
4. Fatigue Lifetime (to failure)
 - Tested by thermal cycling under pressure

Instrumentation



4.000 Long 0.25ϕ 0.065 Thickness Swagelok 316L Tube (sim.)

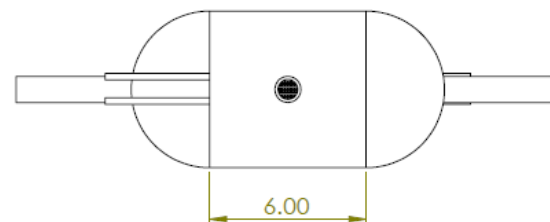
5 Pairs of holes w/o tubes



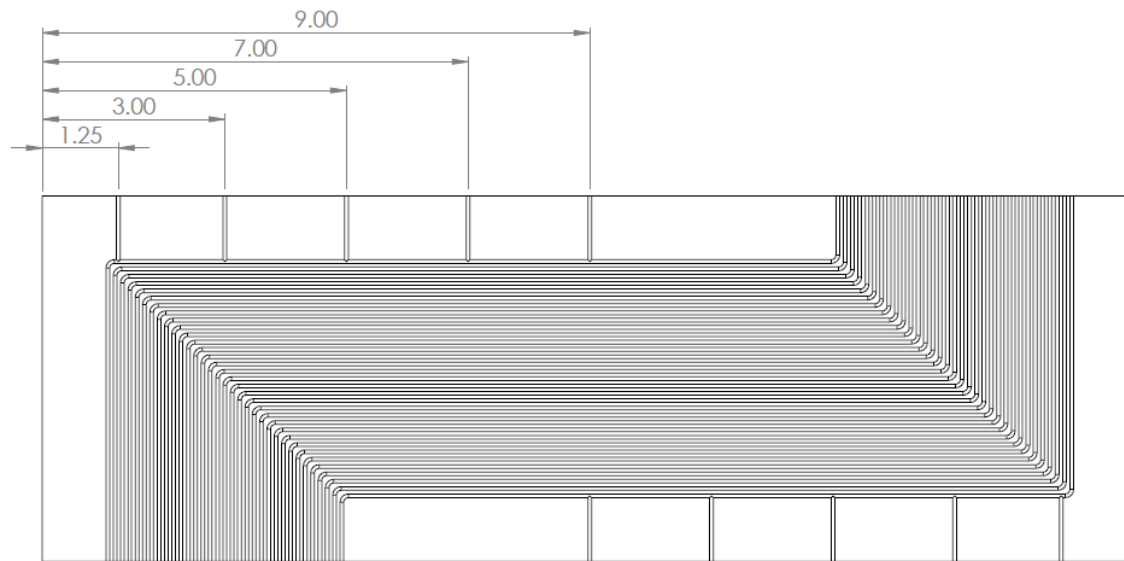
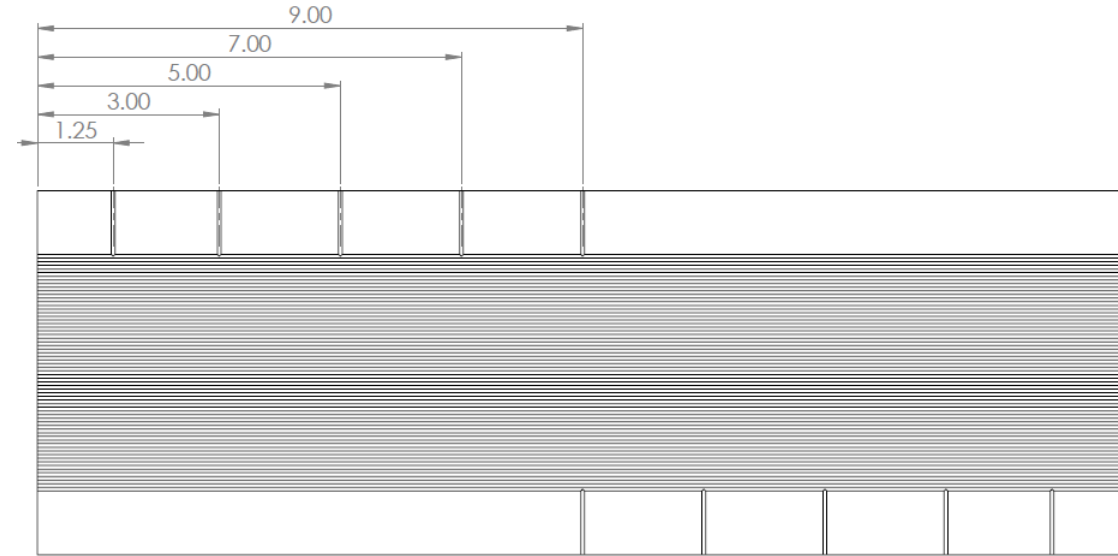
5 Pairs of holes w/o tubes

Support from base when handling and mounting.

1.000 ϕ 0.120 Thickness Swagelok 316L Tube (sim.)



Instrumentation – Tap Locations

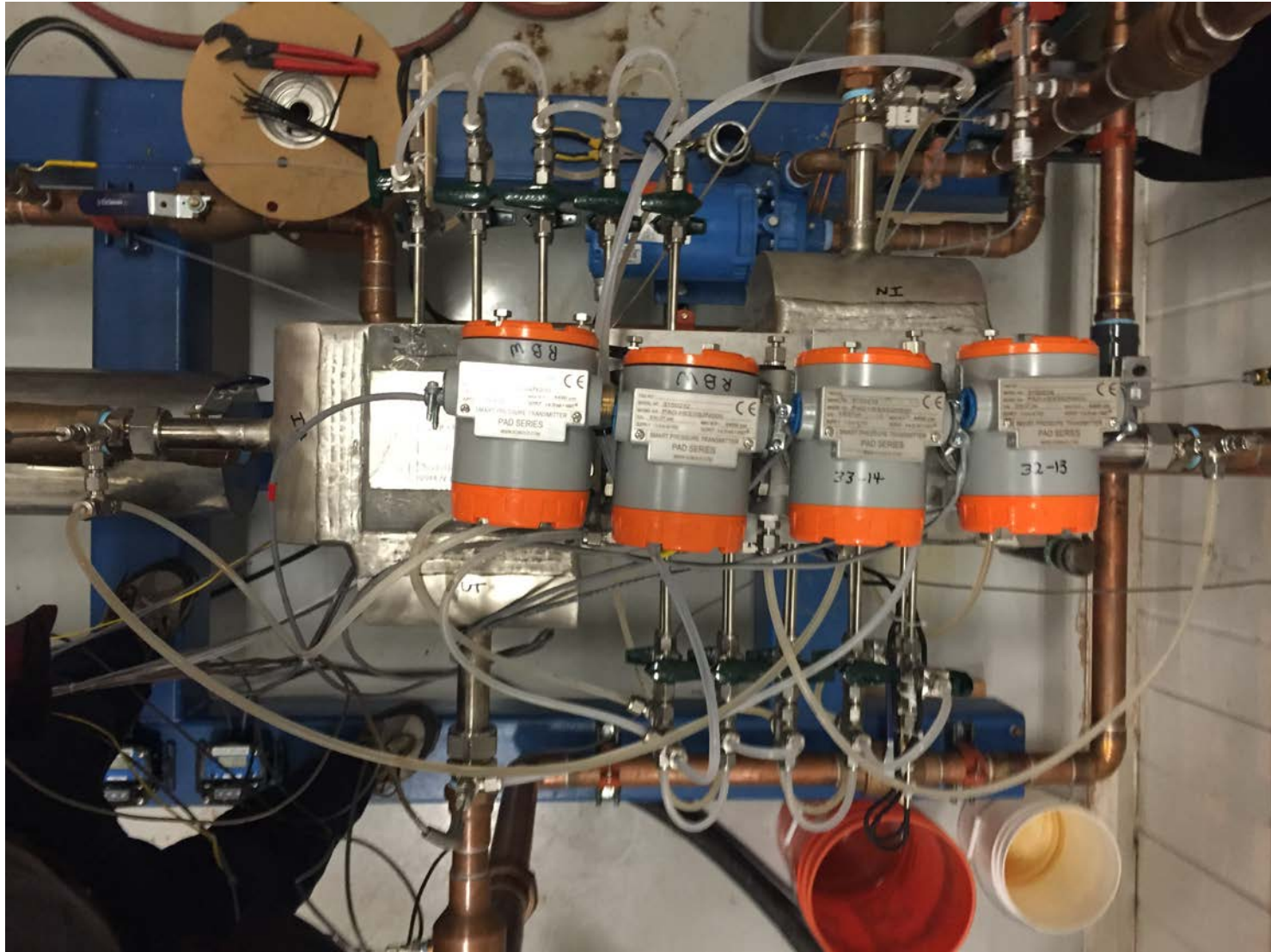


HEAT EXCHANGER TEST PLATFORM

Test Platform Configuration

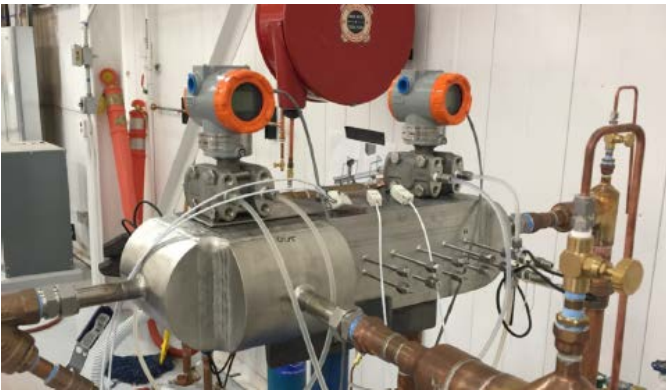
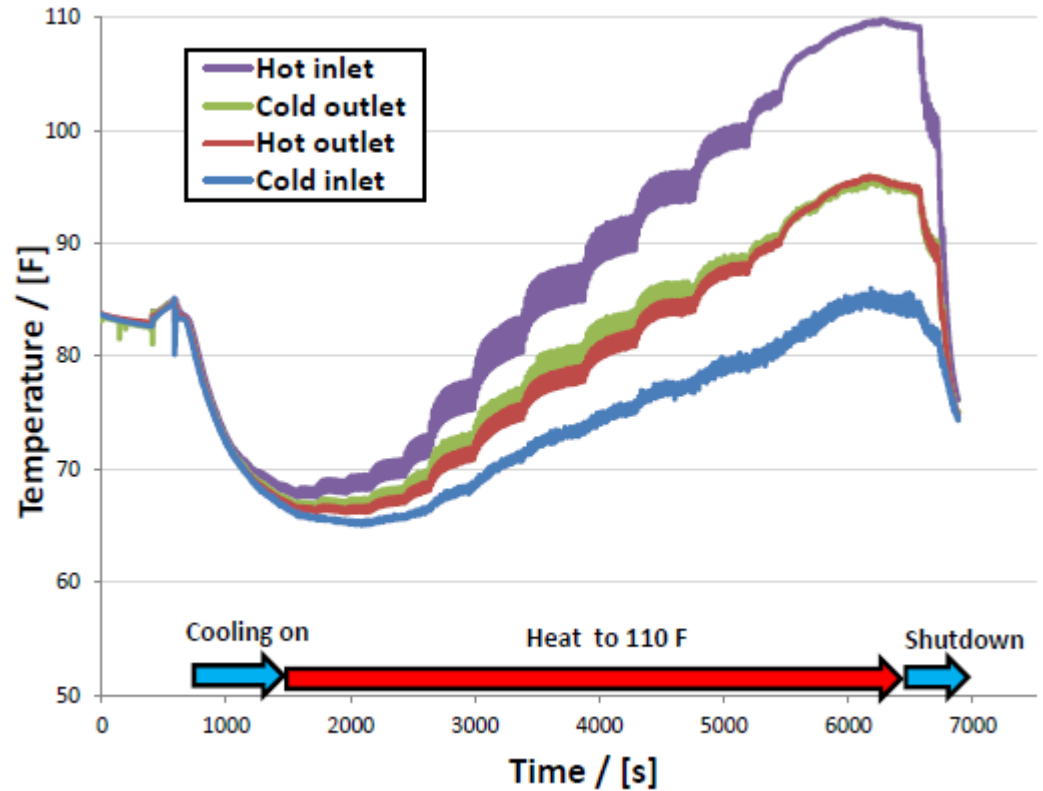


PCHE Instrumentation



PCHE PERFORMANCE COMPARISON

Performance Testing



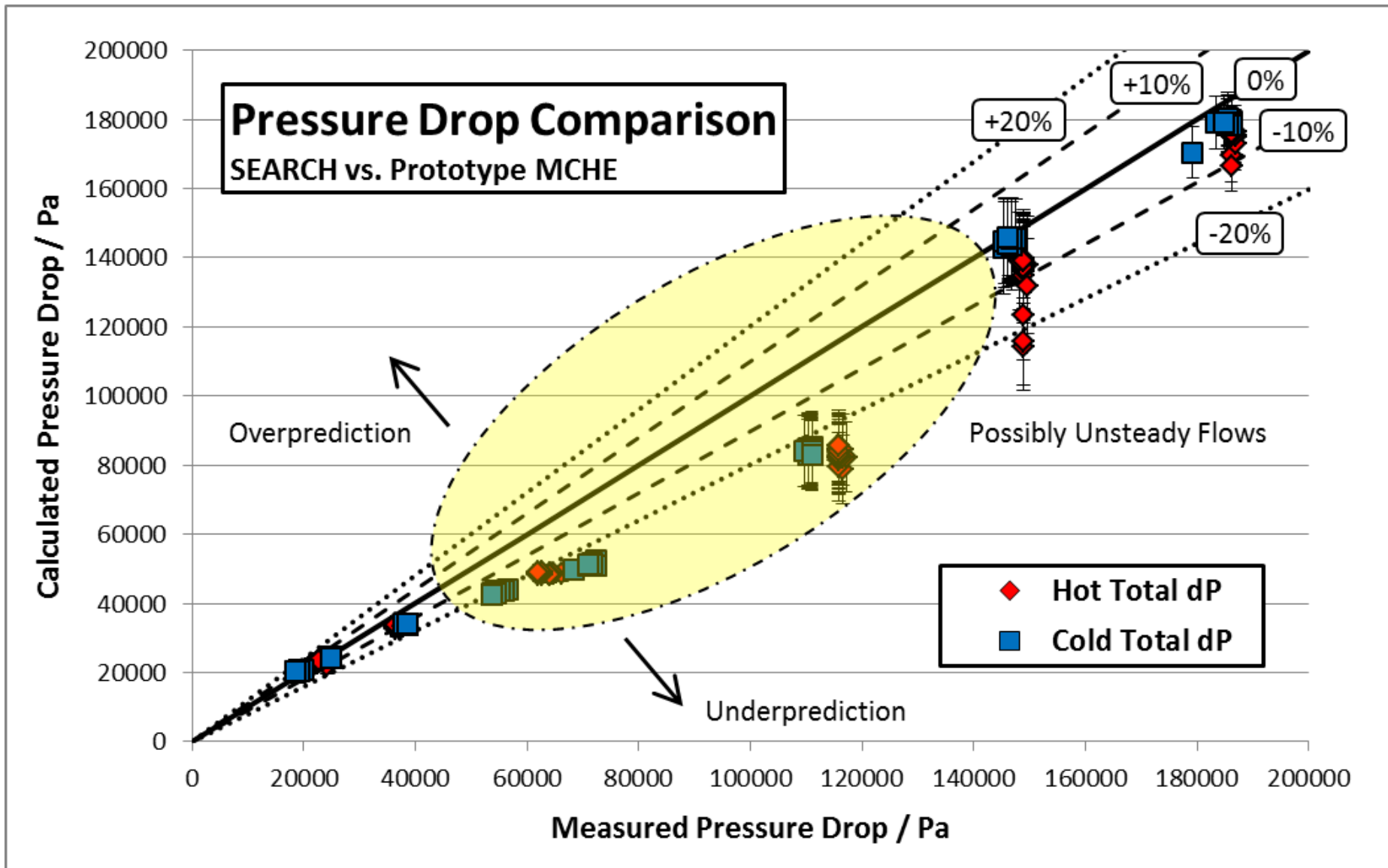
SEARCH appears conservative by at least 10% on q , UA, effectiveness

Performance Comparison

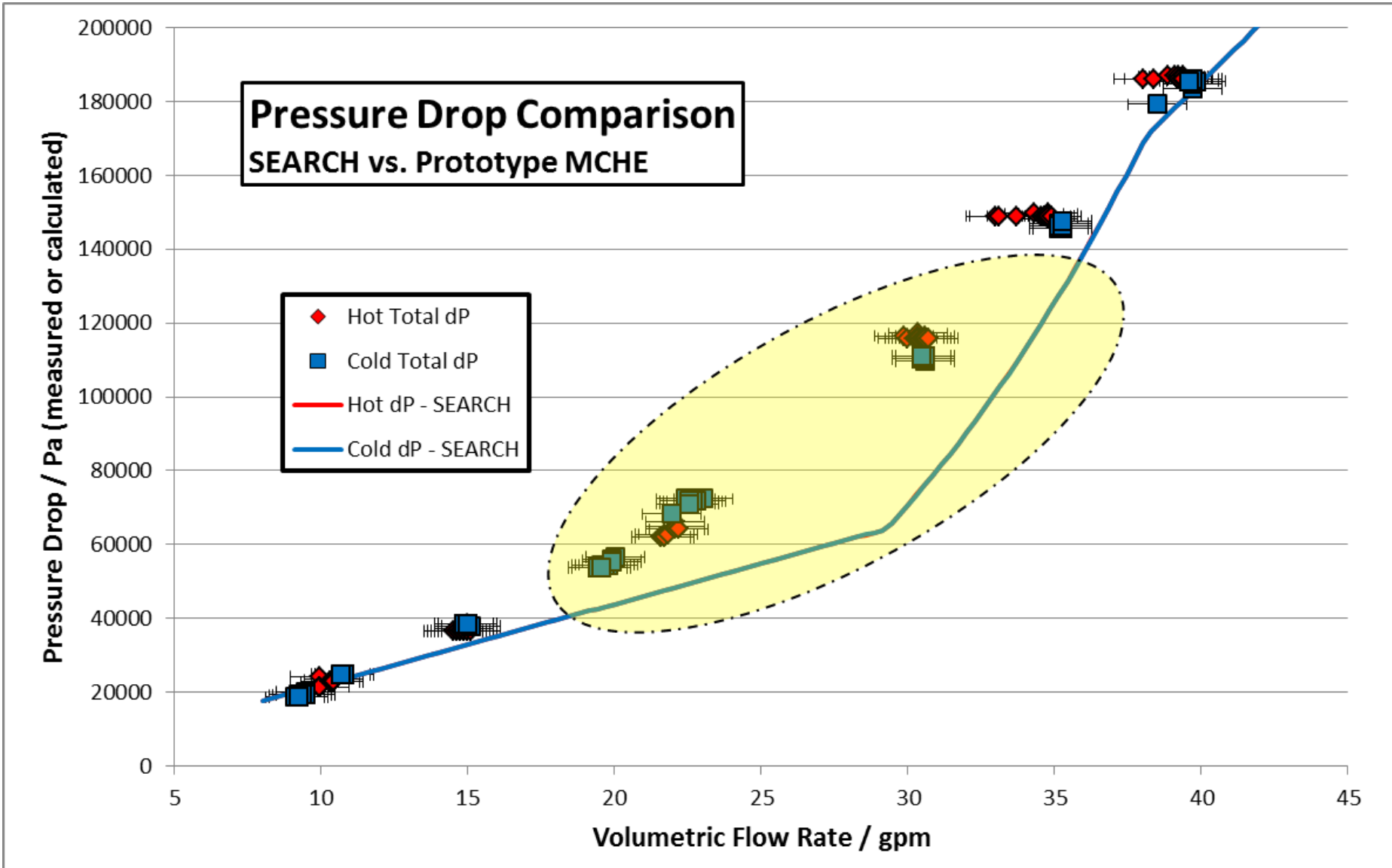
Time Range	Description
0-750	Baseline, prepare to start test. Hot flow started first, wait to reach steady state.
750-1500	Start cooling flow; keep at maximum rate until loop below 70°F.
1500-6500	Increased heater power gradually (5-10% increments) to 100% = 110°F.
6500-7000	Shut off heater power, cooling remains on.

Time / s	\dot{q} / W		$UA / (W/K)$		ε	
	SEARCH	Measured	SEARCH	Measured	SEARCH	Measured
4200	44000	+7%	8100	+13%	43%	+6%
4700	44000	+12%	8200	+23%	43%	+11%
5100	54000	+13%	8400	+26%	43%	+12%
5400	61000	+14%	8500	+28%	44%	+13%
5700	67000	+14%	8600	+27%	44%	+13%
6260	67000	+16%	8700	+32%	44%	+15%

Calculated vs. Meas. Pressure Drop



Pressure Drop Prediction Capability



Conclusions

- Based on our first set of tests:
 - SEARCH is within 25% accuracy on key metrics
 - Thermal performance is predicted conservatively
 - Pressure drop is under-predicted in some regimes
- These results have already been applied
- Testing is planned after loop upgrades
 - Additional thermal-hydraulic observations
 - Intermediate state (T & P) profiles
 - Future test phases (sCO₂, fatigue)

BACKUP SLIDES

The Argument for S-CO₂ Brayton

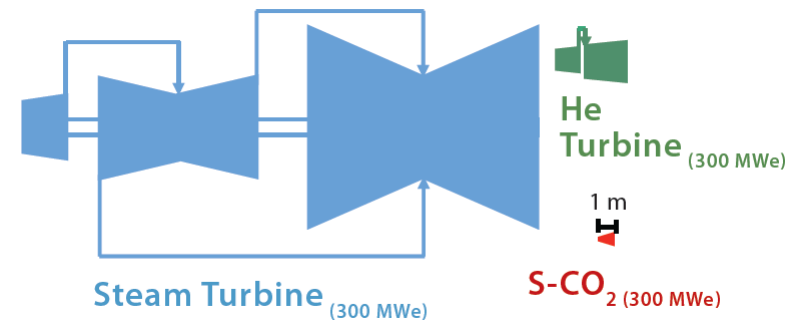
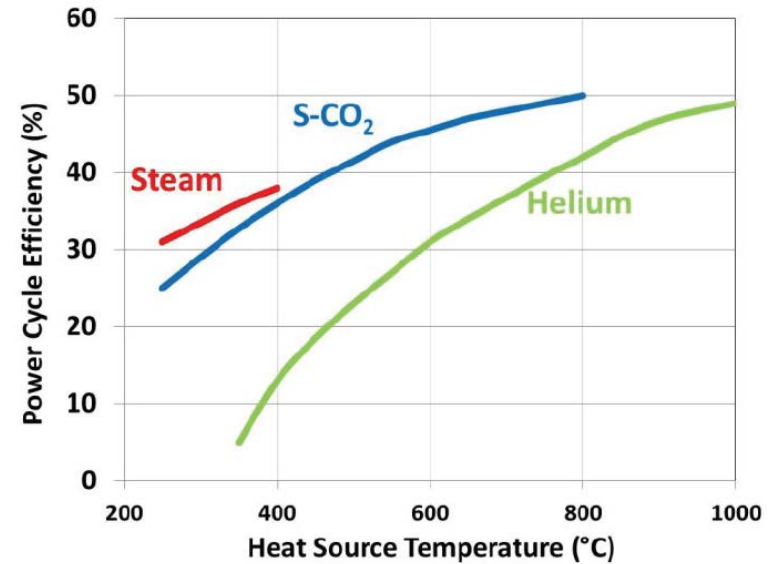
Versus Helium and Steam

1. Higher efficiency

- Sodium Fast Reactor operating at 550 °C
- Concentrated Solar Power up to 700 °C
- CCS Gasified Coal and Natural Gas up to 1150 °C

2. Compact turbomachinery

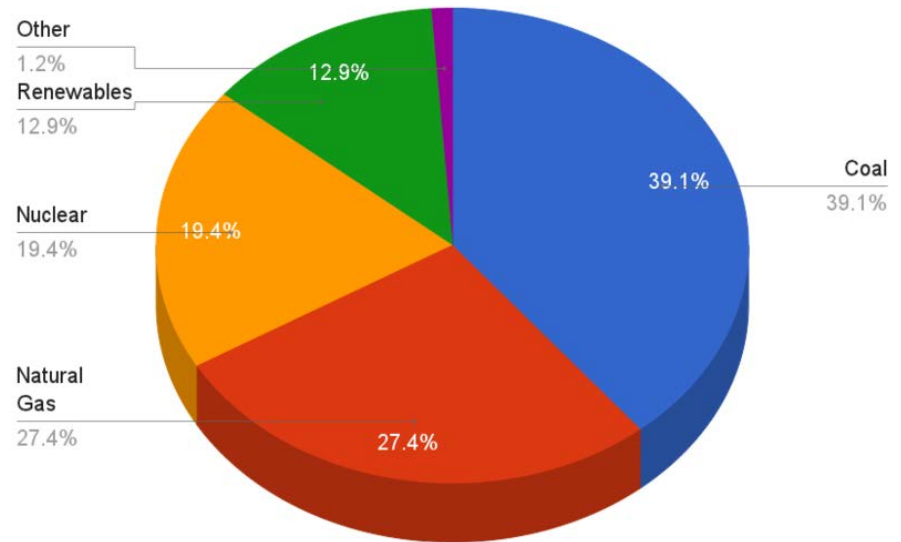
- Smaller system footprint
- Possibly reduced cost



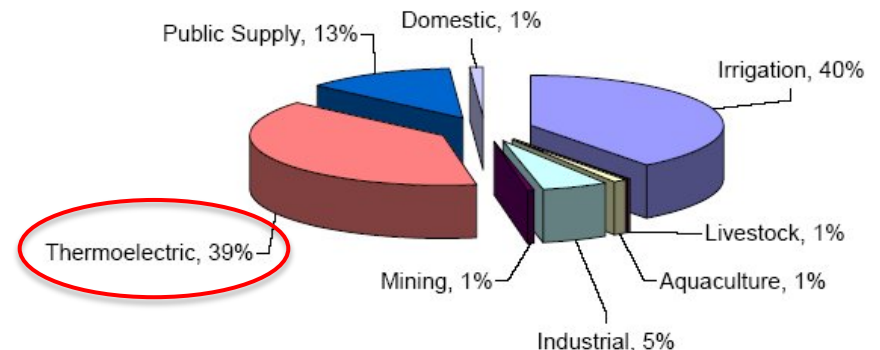
Current Electrical Generation

- Electrical Generation
 - Dominated by fossil
 - Nuclear is a critical part
 - Expected that natural gas and nuclear will grow; coal will shrink
- Two main technologies
 - Steam Rankine cycle
 - Coal, Nuclear, CCNG
 - Gas Brayton cycle
 - Natural gas

U.S. 2013 Electricity Generation By Type



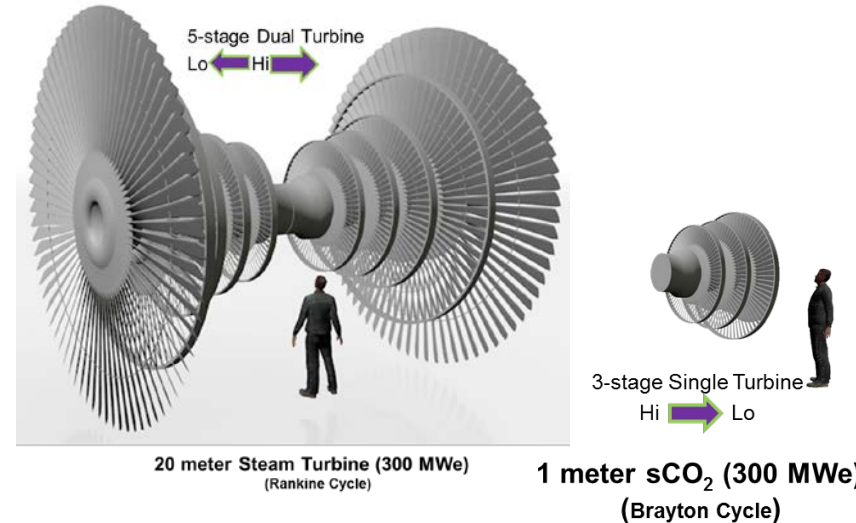
U.S. 2000 Water Withdrawals by Market



Supercritical CO₂ (sCO₂) Brayton Cycle

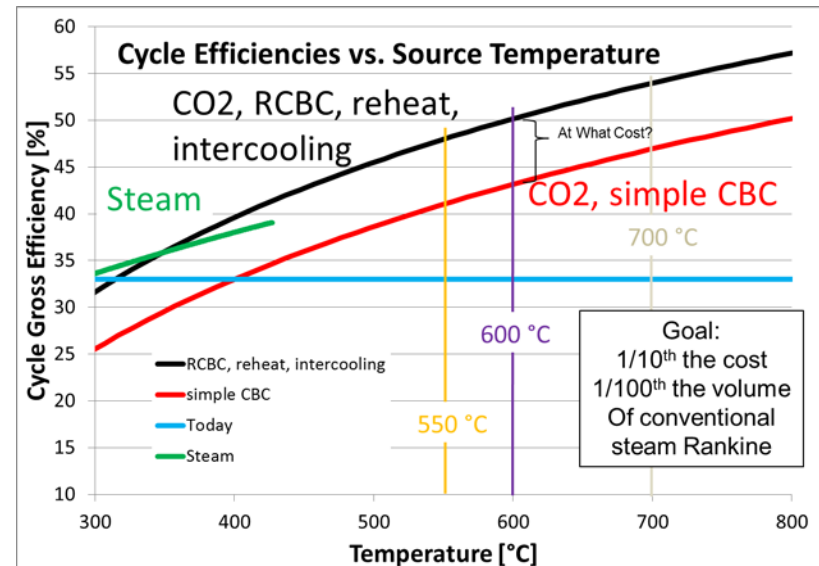
■ Key Advantages over Steam

- Smaller turbomachinery
- Single-phase fluid (no quality issues)
- Recuperation becomes practical

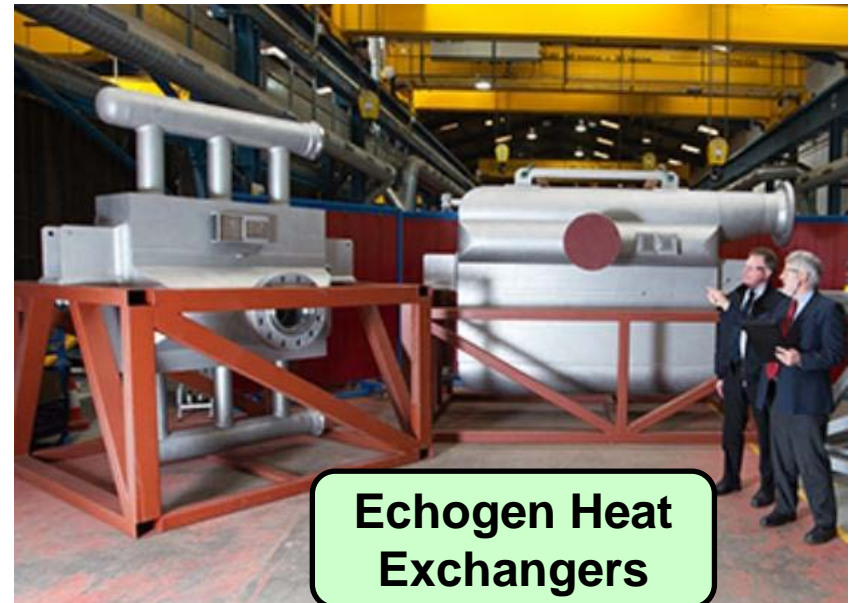
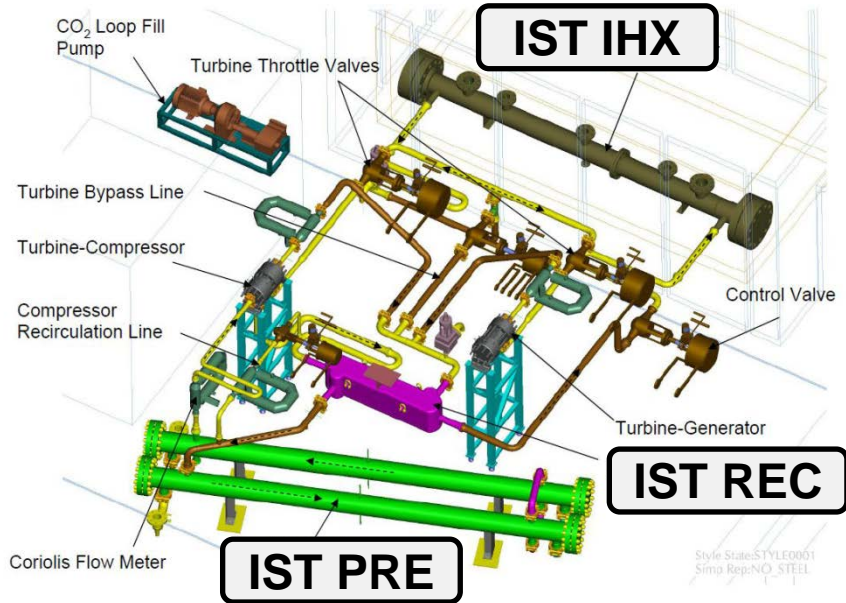


■ Key Advantages over Gas

- High efficiency at low temperatures
- Lower compression work
- Smaller turbomachinery



Current SCO2 CBC HXers



G. O. Musgrove, C. Pittaway, D. Shiferaw, and S. Sullivan, "Tutorial: Heat Exchangers for Supercritical CO₂ Power Cycle Applications," San Antonio, Texas, USA, 03-Jun-2013.

Commercial Unit Potential

Key Requirements:

- ✓ High Pressure
- ✓ High Temperature
- ✓ Corrosion Resistant
- ✓ High Reliability
- ✓ Compact Geometry
- ✓ Scalable to 150 MWe

$$\beta = \frac{A_s}{V} = \frac{4\phi}{d_h}$$



Coil-Wound
10 to 300 [m²/m³]



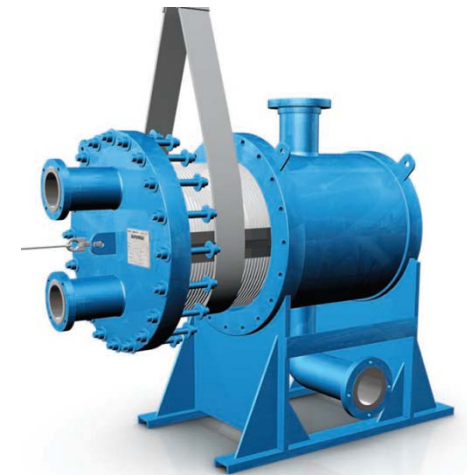
Shell and Tube
10 to 200 [m²/m³]



Plate-Fin
200 to 800 [m²/m³]

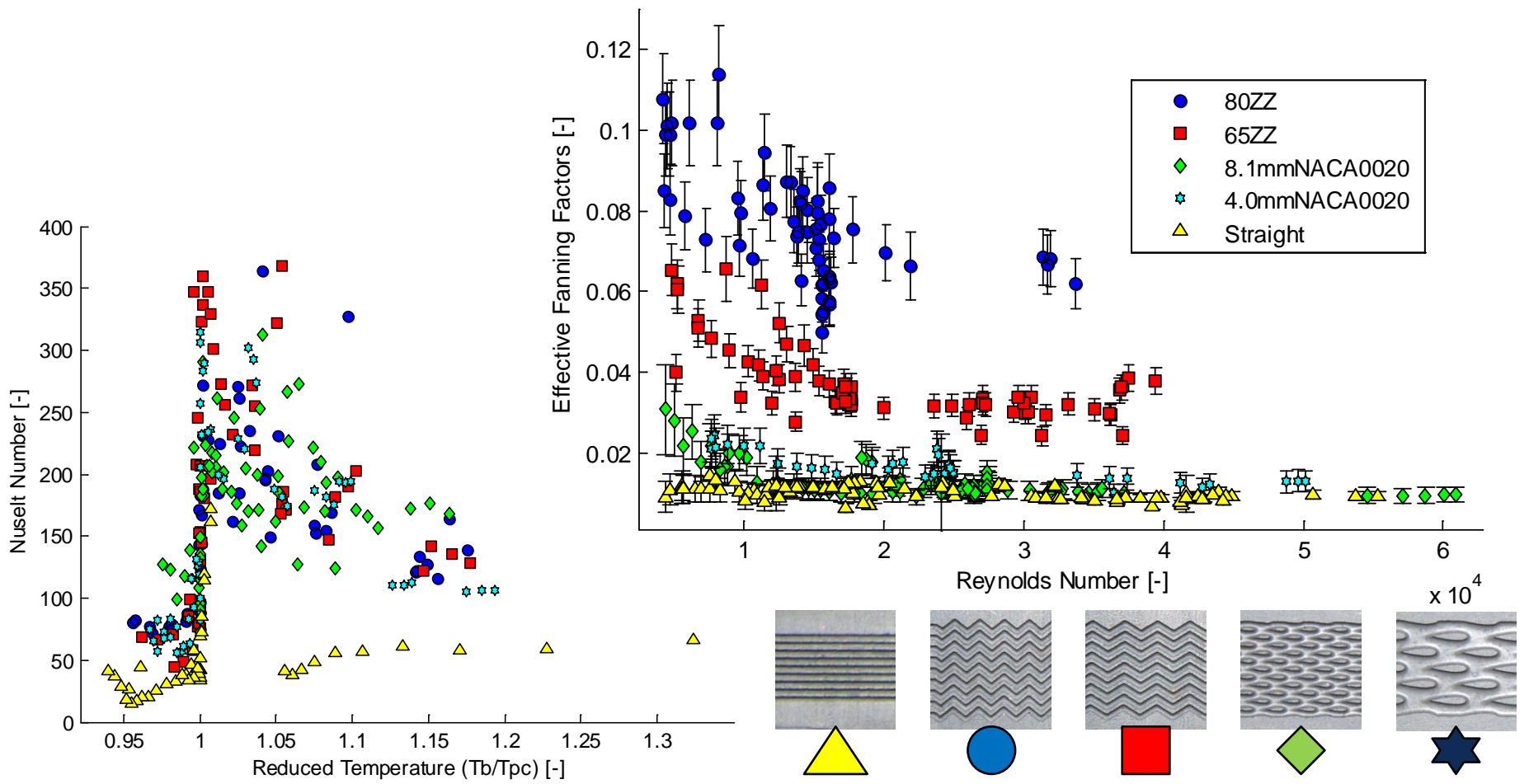


Printed Circuit
200 to 5000 [m²/m³]

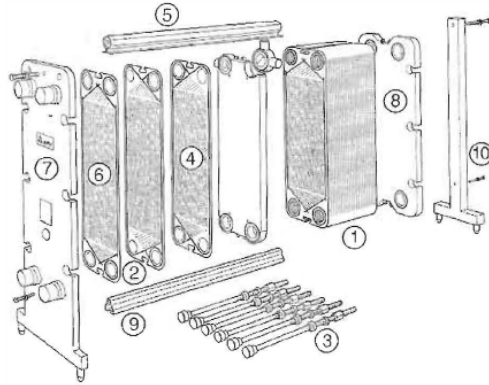


Shell and Plate
100 to 600 [m²/m³]

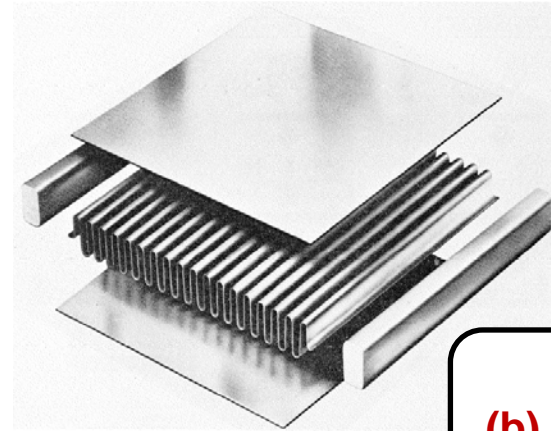
PCHE Thermal-Hydraulic Performance



Carlson, M. (2012). *Measurement and Analysis of the Thermal and Hydraulic Performance of Several Printed Circuit Heat Exchanger Channel Geometries* (Master of Science). University of Wisconsin - Madison, Madison, WI.



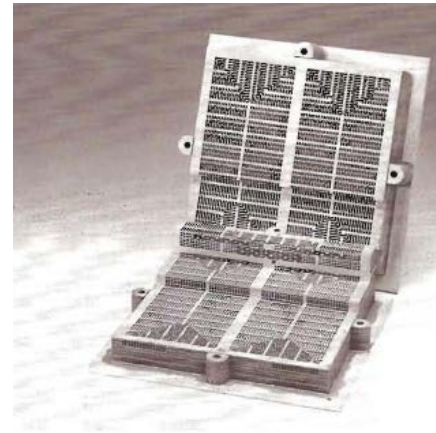
PHE
120 to 660



PFHE
(b) 800 to 1500
(d) 700 to 800



PCHE
(d) 200 to 5000



CBHE
(Marbond)
Up to 10000

HEAT EXCHANGER COMPACTNESS

Surface Area Density: $\beta = \frac{A_s}{V} = \frac{4\phi}{d_h}$

Potential Applications



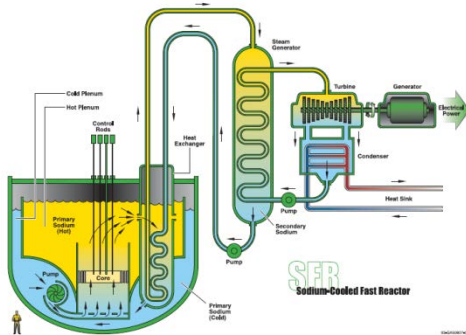
Coal / Nuclear
Steam Rankine



MARINE
Rolls-Royce WR-21
Type 45 Destroyer



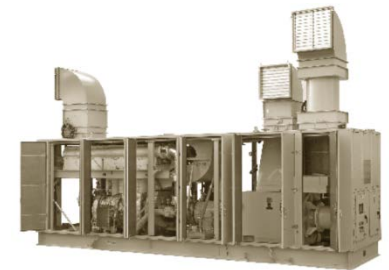
VEHICULAR
Honeywell AGT1500
M1 Abrams Tank



GenIV Nuclear
Sodium Fast Reactor



Refrigeration
Commercial, Cryogenic



STATIONARY
Solar Turbines
Mercury 50

Effectiveness and Scaling Behavior

Heat Transfer Rate

Heat Transfer Surface Area

Temperature Differential

Hot Inlet

Cold Inlet

$$\dot{q} = UA\Delta T = \varepsilon (\dot{m} \bar{c}_p)_{\min} (T_{H,in} - T_{C,in})$$

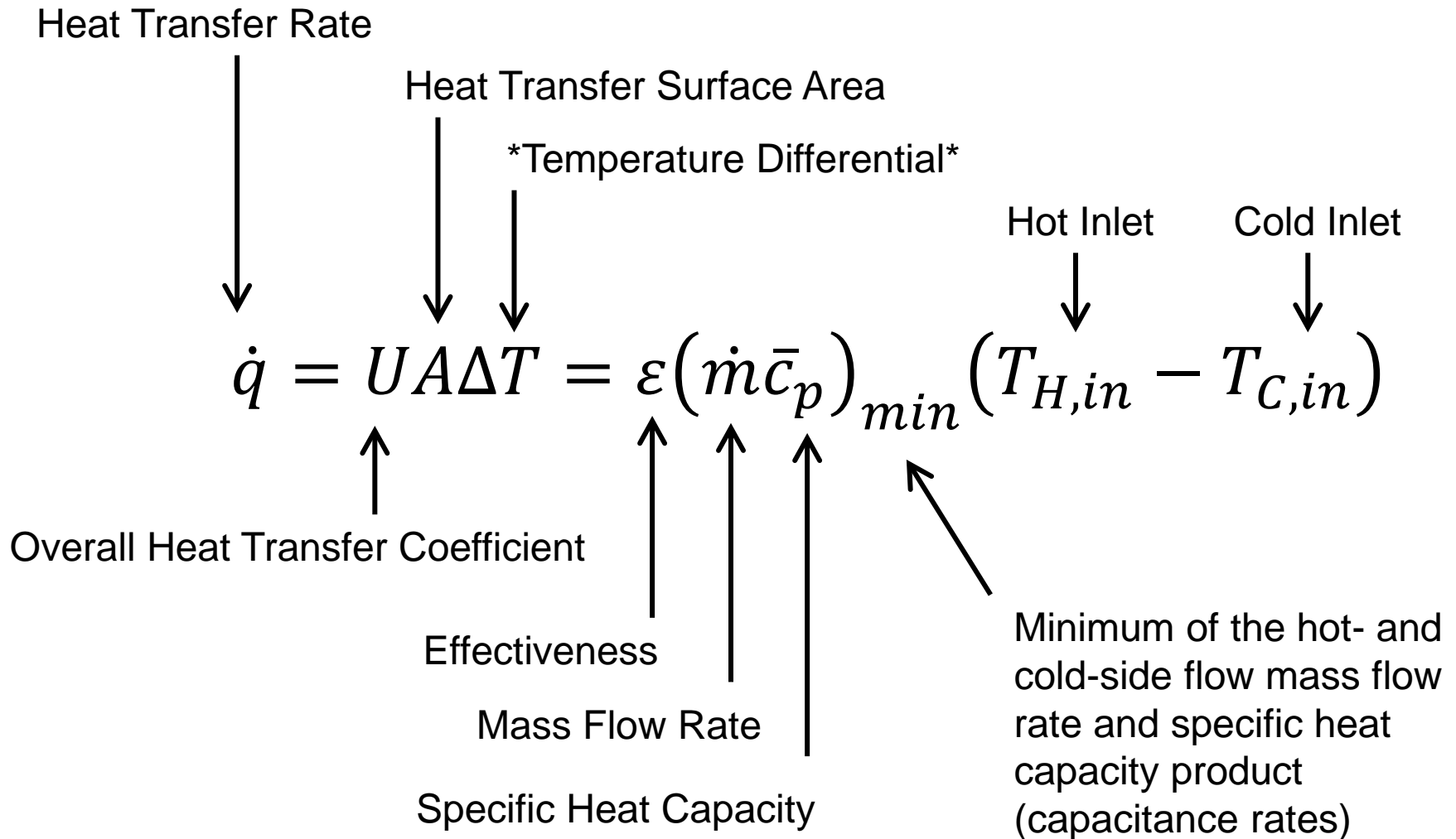
Overall Heat Transfer Coefficient

Effectiveness

Mass Flow Rate

Specific Heat Capacity

Minimum of the hot- and cold-side flow mass flow rate and specific heat capacity product (capacitance rates)



Fundamental Scaling Behavior

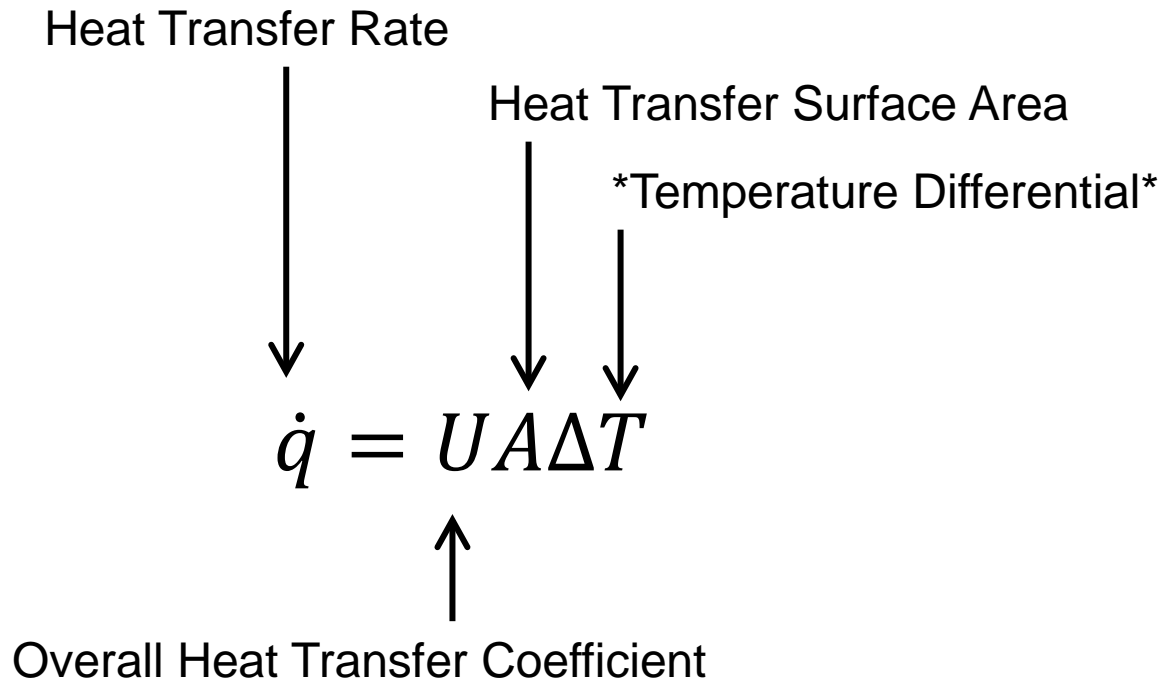
Heat Transfer Rate

Heat Transfer Surface Area

Temperature Differential

$$\dot{q} = UA\Delta T$$

Overall Heat Transfer Coefficient



Fundamental Scaling Behavior

$$\dot{q} = UA\Delta T$$

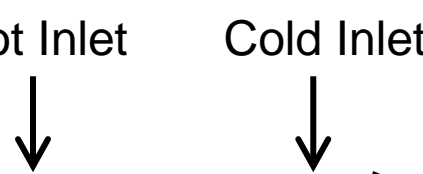
Fluid	Transmission Surface	Fluid	Overall Heat Transmission Coefficient	
			(Btu/ft ² hr °F)	(W/m ² K)
Water	Cast Iron	Air or Gas	1.4	7.9
Water	Mild Steel	Air or Gas	2.0	11.3
Water	Copper	Air or Gas	2.3	13.1
Water	Cast Iron	Water	40 - 50	230 - 280
Water	Mild Steel	Water	60 - 70	340 - 400
Water	Copper	Water	60 - 80	340 - 455
Air	Cast Iron	Air	1.0	5.7
Air	Mild Steel	Air	1.4	7.9
Steam	Cast Iron	Air	2.0	11.3
Steam	Mild Steel	Air	2.5	14.2
Steam	Copper	Air	3.0	17
Steam	Cast Iron	Water	160	910
Steam	Mild Steel	Water	185	1050
Steam	Copper	Water	205	1160
Steam	Stainless Steel	Water	120	680

Effectiveness and Scaling Behavior

Heat Transfer Rate

$$\dot{q} = UA\Delta T = \varepsilon (\dot{m} \bar{c}_p)_{\min} (T_{H,in} - T_{C,in})$$

Hot Inlet Cold Inlet

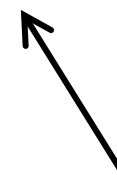


Effectiveness

Mass Flow Rate

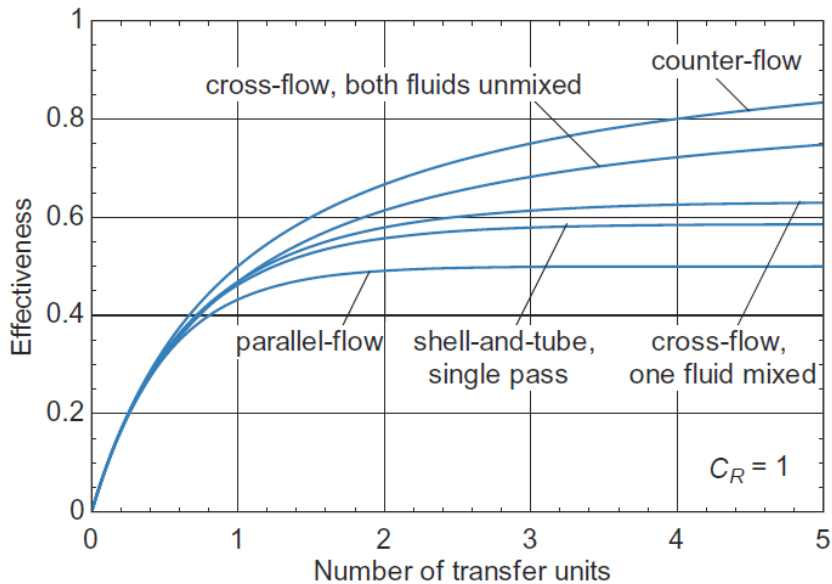
Specific Heat Capacity

Minimum of the hot- and cold-side flow mass flow rate and specific heat capacity product (capacitance rates)

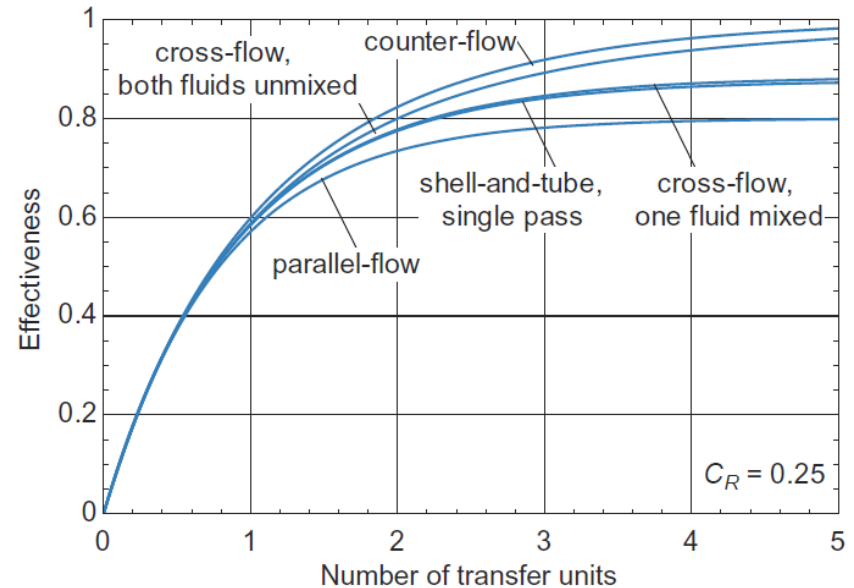


Other Useful e-NTU Scaling

- Configuration matters most for $C_R = 1$; counter-flow is best
- Effectiveness is asymptotic with NTU (size); 1 for counter-flow
- Configuration matters less as C_R approaches 0



$C_R = 1$



$C_R = 0.25$

Pressure Drop Correlations

$$\Delta P = \sum \Delta P_{friction} + \sum \Delta P_{local} + \sum \Delta P_{acceleration} + \sum \Delta P_{body\ forces}$$

■ Body Forces

$$\Delta P_{friction} = f \frac{L_s}{d_{hyd}} \frac{1}{2} \frac{G^2}{\rho}$$

$$\Delta P_{gravity} = g \left(\frac{i_{out} \rho_{out} + i_{in} \rho_{in}}{i_{out} + i_{in}} \right) L \sin(\theta)$$

Blasius

Kondrat'ev

$$f = 0.316 Re^{-0.25}$$



$$f = 0.188 Re^{-0.22}$$

■ Local Form Losses

$$\frac{\Delta P_{local}}{G^2/2\rho} = K_{loss} = f \left(\frac{L_{equivalent}}{d_{hyd}} \right)$$

Haaland

Filonenko

$$f = \frac{1}{\left(1.8 \log_{10} \left[\left(\frac{RR}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right] \right)^2}$$



$$f = \frac{1}{\left(1.82 \log_{10} Re_b - 1.64 \right)^2}$$

■ Acceleration Difference

$$\Delta P_{acceleration} = G^2 \left(\frac{1}{\rho_{out}} - \frac{1}{\rho_{in}} \right)$$

Colebrook Equation

$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left(\frac{RR}{3.7} + \frac{2.51}{Re \sqrt{f}} \right)$$

Heat Transfer Correlations

Constant Property

Dittus-Boelter Correlation

$$Nu = C Re^n Pr^m$$



Supercritical Fluids

Jackson's Correlation

$$Nu = 0.0183 Re_b^{0.82} Pr_b^{0.5} \left(\frac{\rho_w}{\rho_b} \right)^{0.3} \left(\frac{\bar{c}_p}{c_{p,b}} \right)^n$$

Gnielinski Correlation

$$Nu = \frac{\left(\frac{f}{8} \right) (Re - 1000) Pr}{1 + 12.7 \sqrt{\frac{f}{8}} (Pr^{\frac{2}{3}} - 1)}$$



Pitla Correlation

$$Nu = \left(\frac{Nu_w|_{Gnielinski} + Nu_b|_{Gnielinski}}{2} \right) \frac{k_w}{k_b}$$