

Numerical Investigation of Potential Erosion Mechanisms in Turbulent Flow of sCO₂ Pipe Bends

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Talk Organization

- Background and Motivation
- Objectives and Problem Statement
- Computational Approach and Validation Studies
- Simulations and Results
- Summary and Outlook

Background and Motivation

- 1 **Supercritical CO₂ for power generation in thermal solar, fossil, and nuclear power plants**
 - Ideal fluid for closed-loop cycles as it is non-toxic, non-flammable and cheaper
 - High pressure operation (200-350 bar) means low specific volume, compact designs
 - High temperatures (500-750 C) may require analysis of erosion resistance
- 2 **Erosion Mechanisms**
 - Particulate erosion (mechanical abrasion) in nozzles and turbines
 - Erosion in heat exchangers at high temperatures

Background and Motivation

1 Particulate Erosion

- Mechanical abrasion in nozzles and turbines due to particulates¹

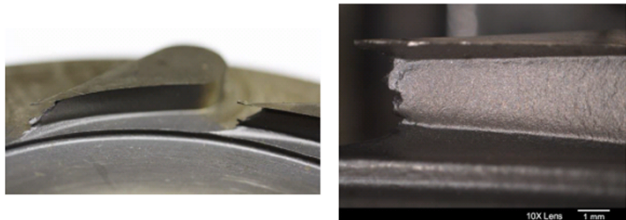


Figure: Erosion of sharp corners.

- ## 2 Erosion *due to flow shear* in heat exchanger pipes at high temperatures.

¹Fleming and Kruiuzenga, Sandia Report SAND2014-15546.

Background and Motivation

Hypotheses:

- Large fluctuations in local temperature and pressure due to turbulence, secondary flow patterns, and property variations may cause substantial shear stresses on the pipe walls.
- Surface or geometric irregularities in pipe fixtures (bends, junctions etc.) may impact wall shear stresses and cause erosion.

Example

- Erosive burning in solid propellant rocket motors²
- Erosion of endothelial walls in arteries.

²Apte and Yang, JFM 2003.

Background and Motivation

Erosive Burning in Solid Propellant Rocket Motors³

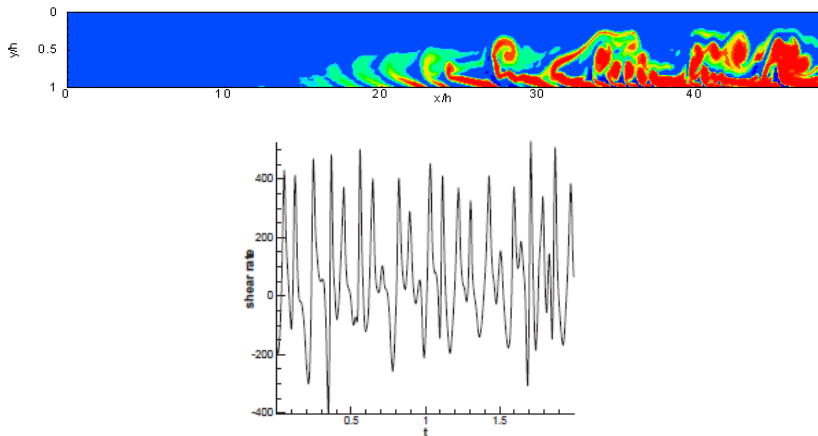


Figure: Instantaneous vorticity contours and shear rate history.

³Apte and Yang, JFM 2003.

Objectives

- Using predictive numerical simulations, investigate potential erosive mechanism in heat exchanger pipes carrying sCO₂ with minimal impurities.
- Investigate effects of heat transfer and temperature dependent property variations on the pipe shear stresses and their eventual impact on erosion.

Problem Statement

Investigate, using predictive large-eddy simulations (LES), turbulent shear force distribution in a 90° bend with and without heat transfer with conditions similar to sCO₂ heat exchangers.

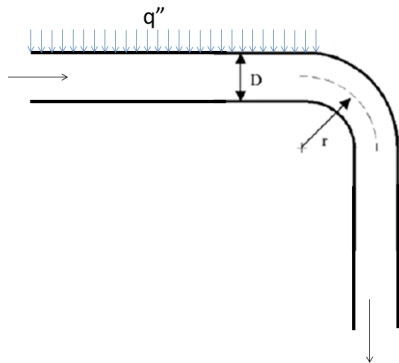


Figure: Flow configuration.

Flow parameters of importance

- Pipe Reynolds number
 $Re_D = DU/\nu = 5000, 27000, 100000$
- Pipe Dean's number
 $De = (D/2r)^{1/2} Re_D = 2886, 15589, 57720.$
- Bend curvature $r/D = 1, 3$
- Thermally developing pipe flow with heat influx (or outflux)

Mathematical Formulation

- Large Eddy Simulation (LES) on arbitrary shaped, unstructured grids for large Reynolds number turbulent flows.
- Variable density, zero Mach number formulation with variable properties.

$$\frac{\partial \overline{\rho_g}}{\partial t} + \frac{\partial \overline{\rho_g} \tilde{u}_j}{\partial x_j} = 0 \quad (1)$$

$$\frac{\partial \overline{\rho_g} \tilde{u}_i}{\partial t} + \frac{\partial \overline{\rho_g} \tilde{u}_i \tilde{u}_j}{\partial x_j} = -\frac{\partial \overline{p}}{\partial x_i} + \frac{\partial}{\partial x_j} \left(2\overline{\mu} \tilde{S}_{ij} \right) - \frac{\partial q_{ij}^r}{\partial x_j} \quad (2)$$

$$\frac{\partial \overline{\rho_g} \tilde{h}}{\partial t} + \frac{\partial \overline{\rho_g} \tilde{h} \tilde{u}_j}{\partial x_j} = \frac{\partial}{\partial x_j} \left(\overline{\rho_g} \tilde{\alpha}_h \frac{\partial \tilde{h}}{\partial x_j} \right) - \frac{\partial q_{hj}^r}{\partial x_j} \quad (3)$$

Mathematical Formulation

Subgrid scale (or unresolved scale) terms are modeled using dynamic Smagorinsky model⁴, with model constants obtained directly from the solver (**NO tuning parameters**)

$$q_{ij}^r = \bar{\rho}(\tilde{u}_i \tilde{u}_j - \widetilde{u_i u_j}) = 2\mu_t \tilde{S}_{ij} - \frac{1}{3}\bar{\rho}q^2 \delta_{ij}; \quad \mu_t = C_\mu \bar{\rho} \bar{\Delta}^2 \sqrt{\widetilde{S_{ij} S_{ij}}}. \quad (4)$$

$$q_{hj}^r = \bar{\rho}(\tilde{h} \tilde{u}_j - \widetilde{h u_j}) = \bar{\rho} \alpha_t \frac{\partial \tilde{h}}{\partial x_j}; \quad \bar{\rho} \alpha_t = C_\alpha \bar{\rho} \bar{\Delta}^2 \sqrt{\widetilde{S_{ij} S_{ij}}}, \quad (5)$$

⁴Germano 1991.

Flow Solver Features

- Unstructured grids with arbitrary elements capable of simulating turbulent flow through complex geometries
- Solves variable density, zero Mach number flow equations
- Finite Volume, collocated grid based algorithm based on the non-dissipative, energy-conserving concepts⁵
- Dynamic subgrid scale modeling
- MPI-Fortran 90 based parallel solver, scalable to 1000s of processors
- Lagrangian particle tracking for particulate flow simulations⁶
- Solver has been validated for turbulent flows in channels, swirling flows in co-axial combustors, as well as flows through complex gas-turbine combustion chambers (Pratt and Whitney)⁷

⁵ Mahesh et al., ASME J. App. Mech. 2006.

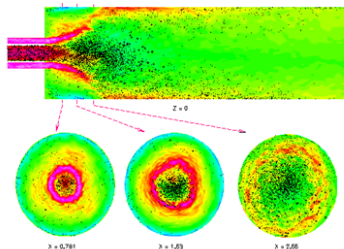
⁶ Apte et al., IJMF, 2003.

⁷ Moin and Apte, AIAA J. 2006.

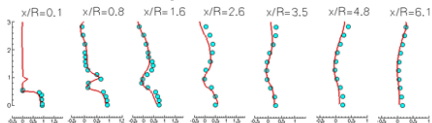
Validation Studies

Sommerfeld Coaxial Combustor Experiment

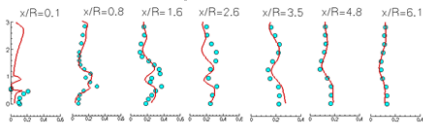
- 1.6 million total hexahedral cells
- 1.1 million particles (glass beads)
- Run on 96 processors
- $Re = 26200$
- 100 CPU-hrs for 1 flow through time on



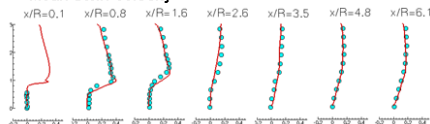
Mean Axial Velocity



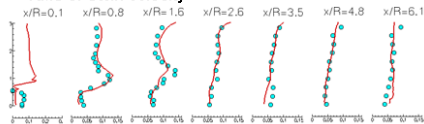
RMS of Axial Velocity



Mean Swirl Velocity

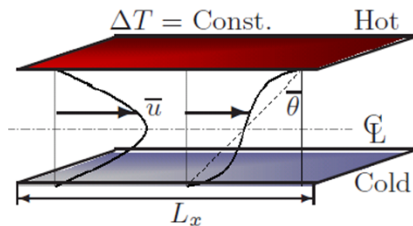


RMS of Swirl Velocity

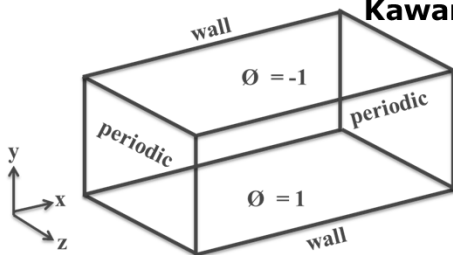


Validation Studies

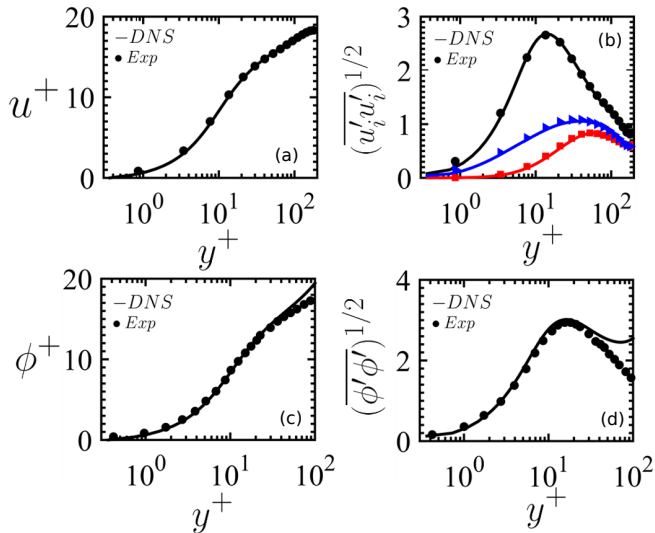
Turbulent Channel with Heat Transfer



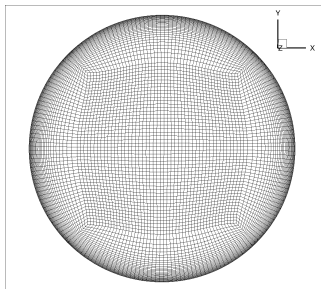
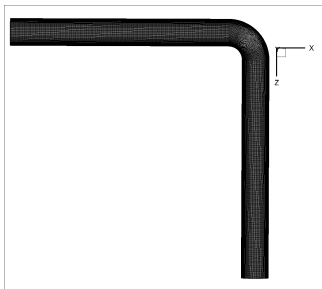
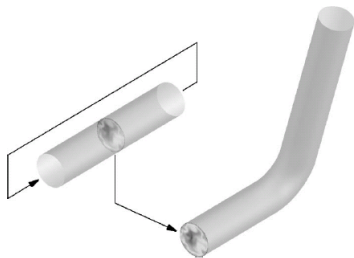
- $Re_\tau = 180$, $Pr = 1$
- Periodic x and z-dir.
- **no-slip isothermal wall BC in y-dir.**
- **Validate Kawamura (1998)**



Turbulent Channel with Heat Transfer



Cold Flow Through Pipe Bend



Velocity Magnitude: $Re = 27000$, $R/D = 3$

Velocity Magnitude, 1 D after the bend

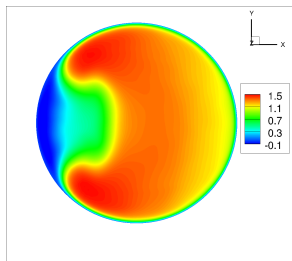
Re = 5000

“

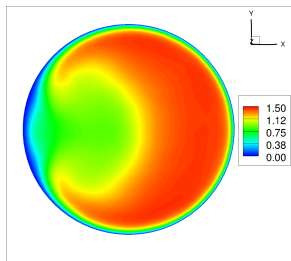
Re = 27000

“

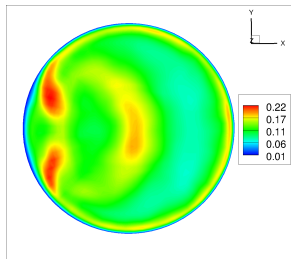
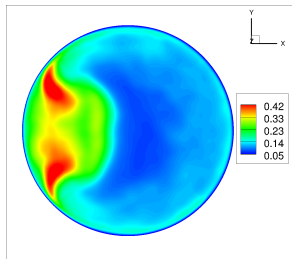
Mean and RMS Flow, $Re = 5000$ at $Z/D = 1$



(d) $R/D = 1$

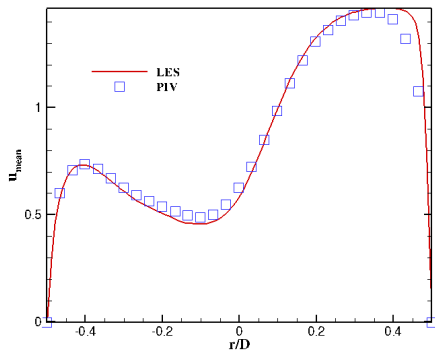


(e) $R/D = 3$

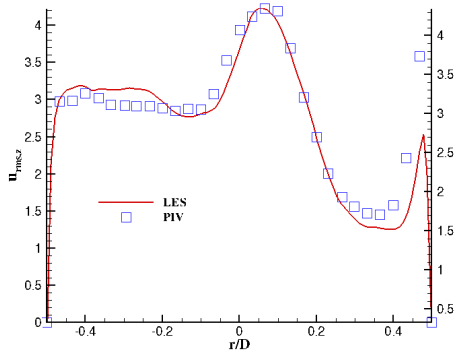


Validation, $Re=5000$, $R/D = 1$

PIV Data of Brucker, 1998 from Rutten et al. 2005, PoF.

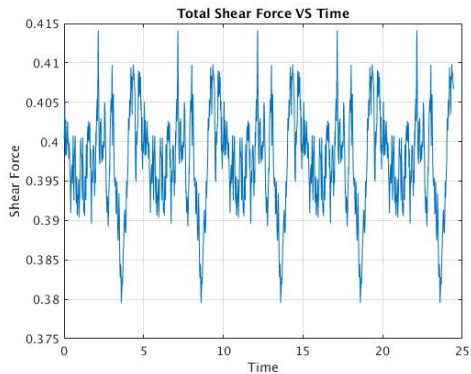


Mean Velocity

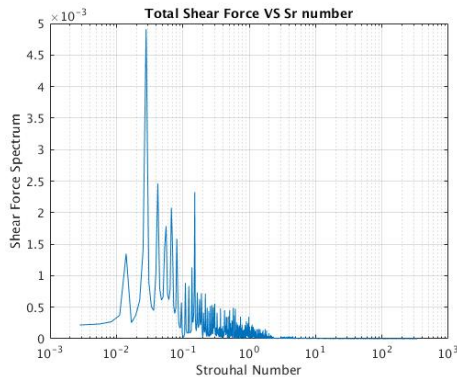


RMS Velocity

Total Shear Force on Bend ($Re = 5000$, $R/D = 3$)

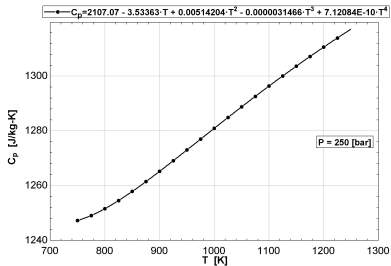
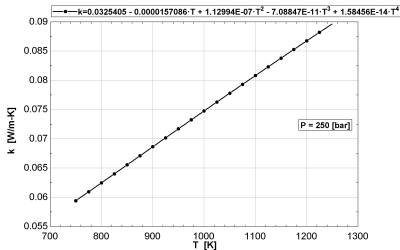
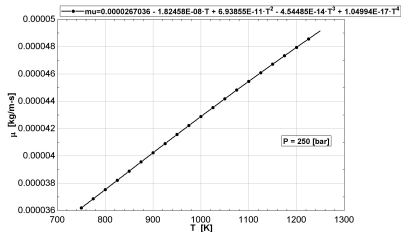
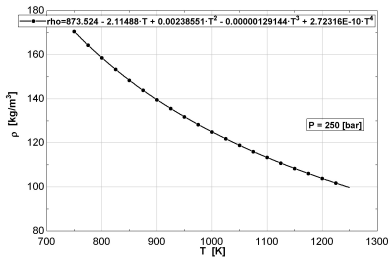


Temporal Signal



Spectrum

Simulations with Heat Transfer



Summary and Outlook

- 1 Initiated predictive large eddy simulations on erosion in pipe bends due to flow shear carrying sCO₂
- 2 Validated the flow solver, capable of handling unstructured grids, for turbulent flow with and without heat transfer in pipes/channels
- 3 Conducted LES in 90° pipe bends at $Re = 5000, 27000$ and $R/D = 1, 3$.
- 4 Variations in shear forces on the bend walls resulted in a broad band spectrum with peaks corresponding to oscillations in the stagnation point after the bend.
- 5 Future work will focus on turbulent flow through the bend with heat transfer and sCO₂ property variations.

Acknowledgement

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