

Flow stratification of supercritical CO₂ in a heated pipe

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Agenda

- Introduction**
 - Motivation
 - Previous work
 - Aim of study
- Numerical method**
 - Governing equations
 - Simulation conditions
- Results and discussion**
 - Bulk properties
 - Flow stratification
 - Secondary flow
 - Turbulence statistics
- Conclusions**

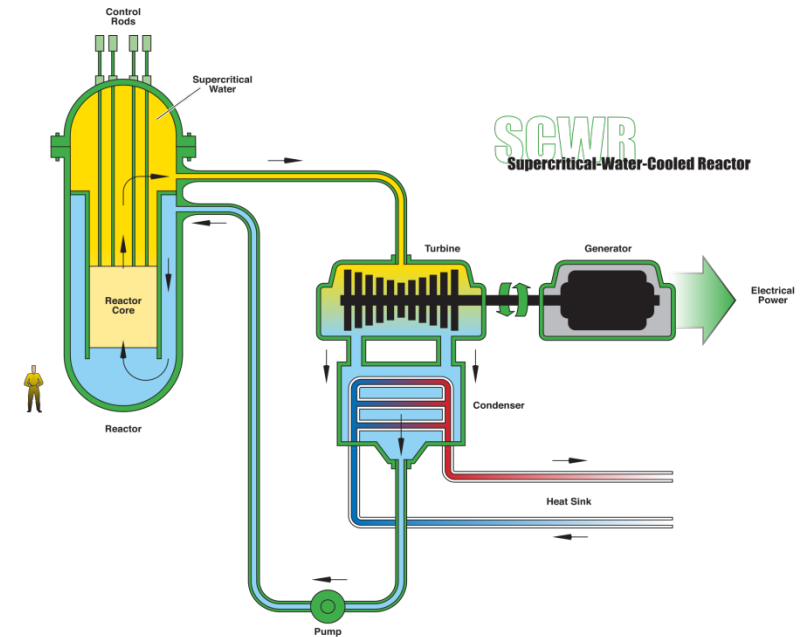
Motivation

Supercritical water reactor (SCWR, HPLWR):

- ❑ High efficiency
- ❑ Compact and simpler system design
- ❑ Water is cheap, non-toxic and transparent
- ❑ Gen IV reactor concept

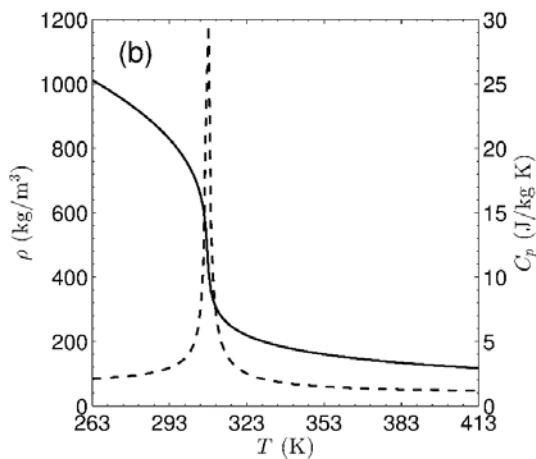
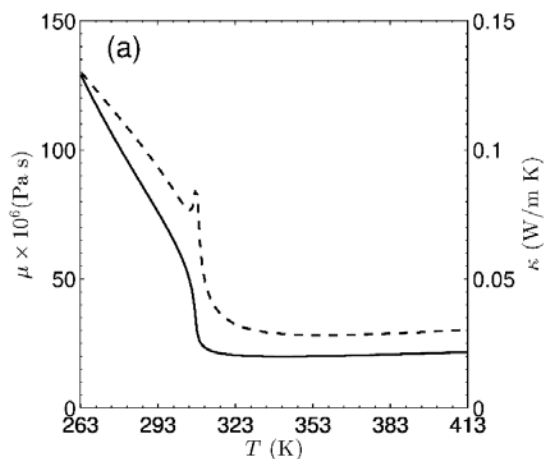
sCO₂ facility (SCARLETT) at IKE, University of Stuttgart

- ❑ Max. mass flux $\dot{m} = 0.1$ (Kg/s), $P_{max} = 120$ bar
- ❑ Followed by development of PCHE (sCO₂-HeRo Project in EU)



Motivation

CFD of heat transfer with supercritical fluid



❑ RANS-Application oriented

- ❑ Various attempt with different models and solvers
- ❑ modelling (classical/advanced) proved to be **unreliable**
- ❑ DNS is needed for further understanding and model improvement

❑ DNS-A powerful tool for turbulence research

- ❑ Details resolved without turbulence modeling
- ❑ Limited to simple geometry
- ❑ Very rare, extremely high computational cost
- ❑ Bae *et al.*, 2005, Nemati/Pecnik, 2015: vertical pipe, CO₂, Re₀=5400, P₀=8 MPa, house code

Previous work

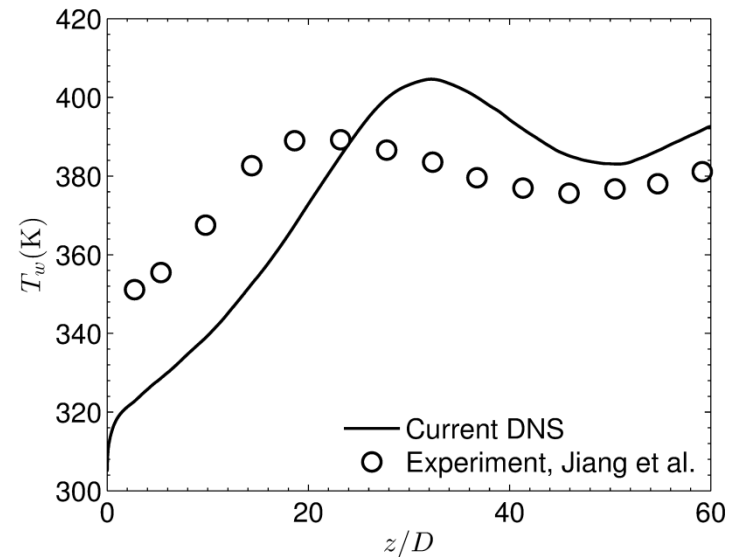
DNS of vertical pipe

DNS vs. DNS (Bae *et al.*, 2005, Nemati/Pecnik, 2015)

- $Re_0=5400$, $P_0=8$ MPa/8.8 MPa, $D=1$ mm/2 mm, variable q_w , T_0
- Up to 80 Mio. cells
- DNS data base (10 cases) with average field, turbulence field, budget, spectrum

DNS vs. Experiments

- Experiments from Jiang *et al.* (U Tsinghua, China), $Re_0=9000$, $P_0=8.8$ MPa, $D=2$ mm
- Well resolved DNS with 150 Mio. cells



Aim of Study

- ❑ Using DNS to investigate heat transfer of $s\text{CO}_2$ under different conditions including vertical/horizontal pipe, complex geometry and conditions in the future
- ❑ Data serves for model improvement/development (see companion paper by Laurien, Pandey and McEligot)

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Numerical method

Governing equation

□ Variation of thermo-physical properties:

Low-Mach N-S equations based on Cartesian Coordinates

$$\frac{\partial(\rho)}{\partial t} + \frac{\partial(\rho U_j)}{\partial x_j} = 0$$

$$\frac{\partial(\rho U_i)}{\partial t} + \frac{\partial(\rho U_i U_j)}{\partial x_j} = -\frac{\partial P}{\partial x_i} + \frac{\partial}{\partial x_j} \left(\mu \left(\frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right) \right) \pm \rho g \delta_{i1}$$

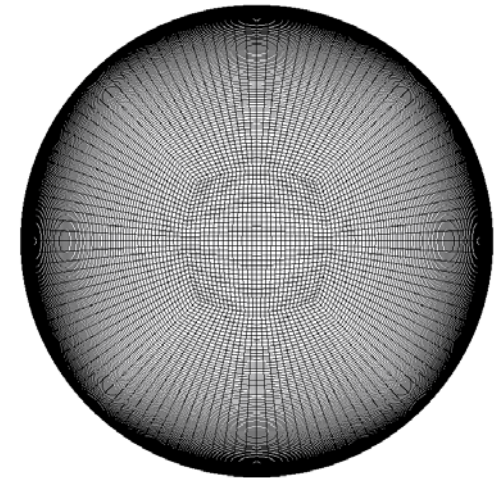
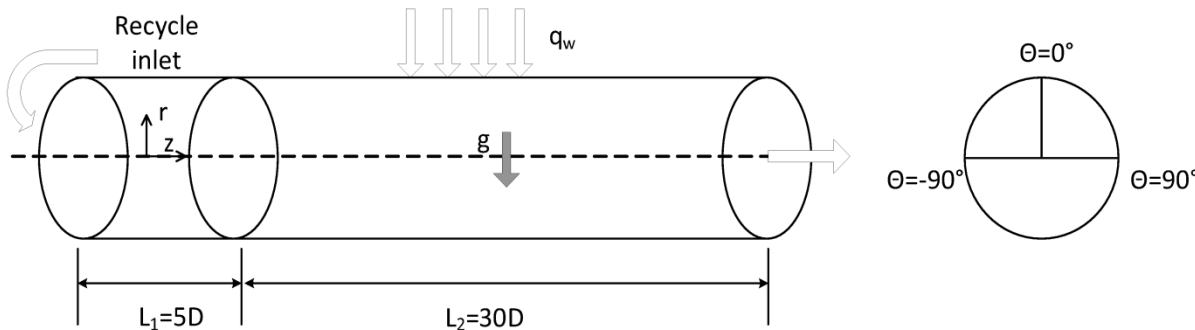
$$\frac{\partial(\rho h)}{\partial t} + \frac{\partial(\rho U_j h)}{\partial x_j} = \frac{\partial}{\partial x_j} \left(k \frac{\partial T}{\partial x_j} \right)$$

$$h = h(P_0, T), T = T(P_0, h), \rho = \rho(P_0, h), \mu = \mu(P_0, h), k = k(P_0, h), C_p = C_p(P_0, h)$$

- OpenFOAM V2.4 as solver, FVM
- PISO as the algorithm for P-U coupling, 2-Order spatial/temporal
- Implementation of properties library: NIST

Numerical method

Computational details



Resolution	r	θ	z	Δr_1^+	$(R\Delta\theta)^+$ (wall)	Δz^+	Δt^+
	168	172	2800	0.11	6.5	4.6	1.1×10^{-4}

- Structured Mesh based on Cartesian Coordinate, 80 Mio. cells
- Fully developed turbulent flow at inlet (Recycle/Rescale BC)
- Used and validated on experiments with heated air (Shehata and McEligot, 1998)

Numerical method

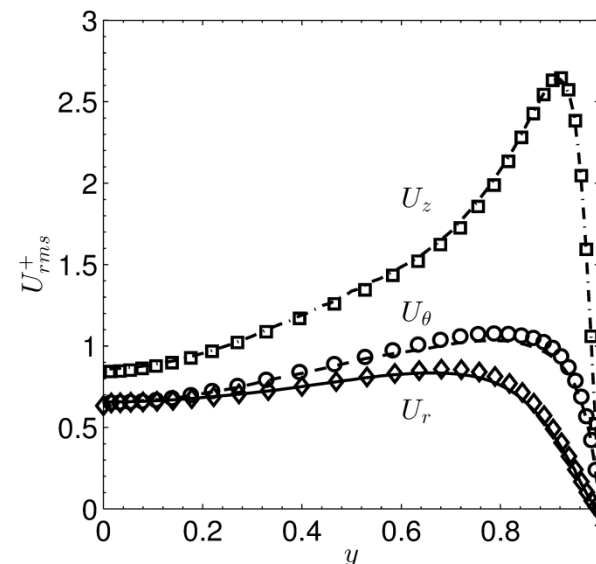
Computational details

- Parallel computation on 1400 CPU cores, 4 days for 10 FTT
- C_f at inlet 0.15% difference as Blasius estimation → numerical quality
- Inflow turbulence quality, validated with Wu and Moin, 2008

Simulation conditions, $P_0 = 8$ MPa

Case	Type	D (mm)	q_w (kW/m ²)	T_0 (K)
SC160	Mixed	1	61.74	301.15
SC230F	Forced (g=0)	2	30.87	301.15
SC230	Mixed	2	30.87	301.15
SC260	Mixed	2	61.74	301.15

$T_{pc} = 307.8$ K



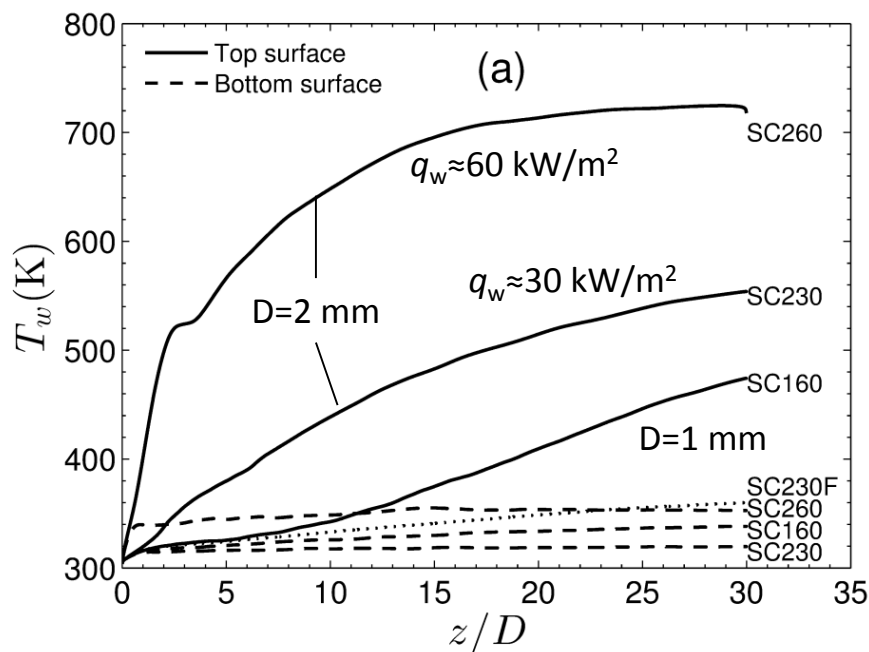
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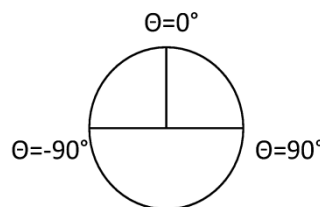
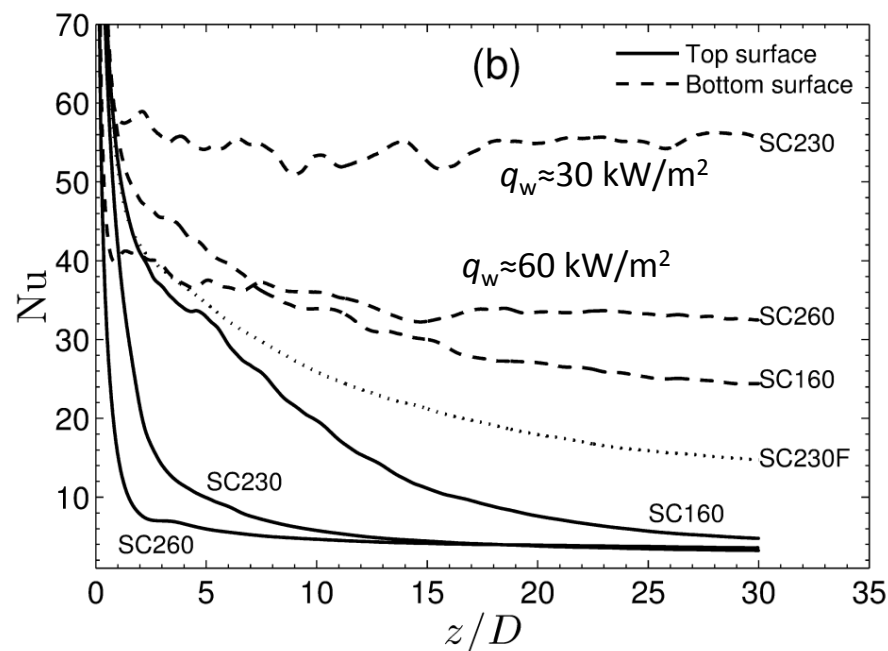
Results and discussion

Bulk properties

Mean wall temperature T_w



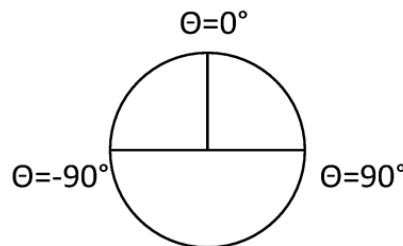
Nusselt number Nu



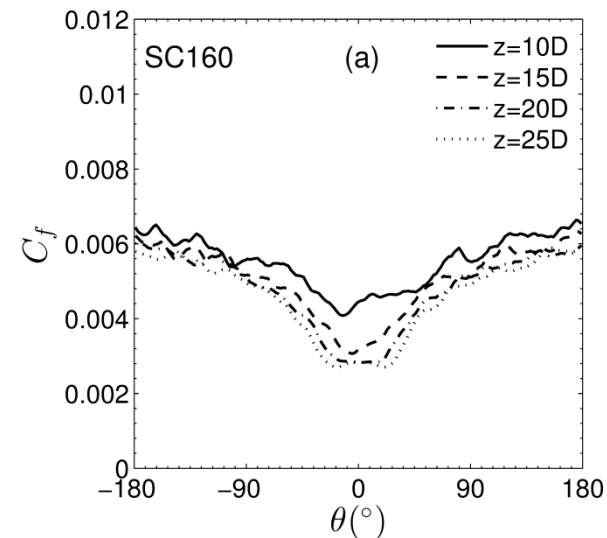
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Bulk properties

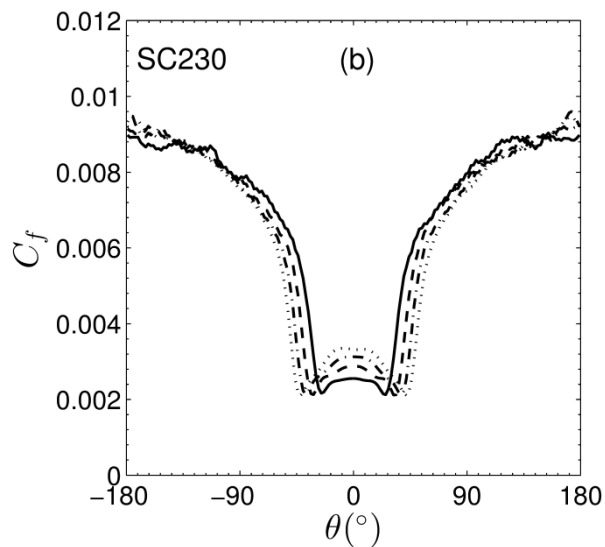
- C_f strongly inhomogeneous
- Non-monotonical tendency



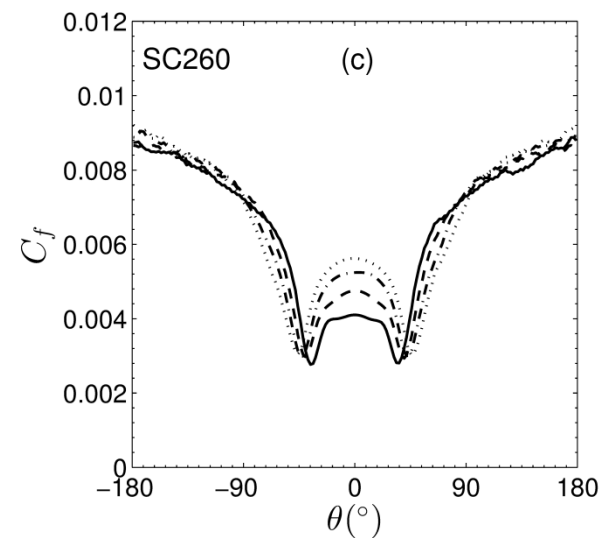
$D=1\text{mm}$



$D=2\text{mm}, q_w \approx 30 \text{ kW/m}^2$

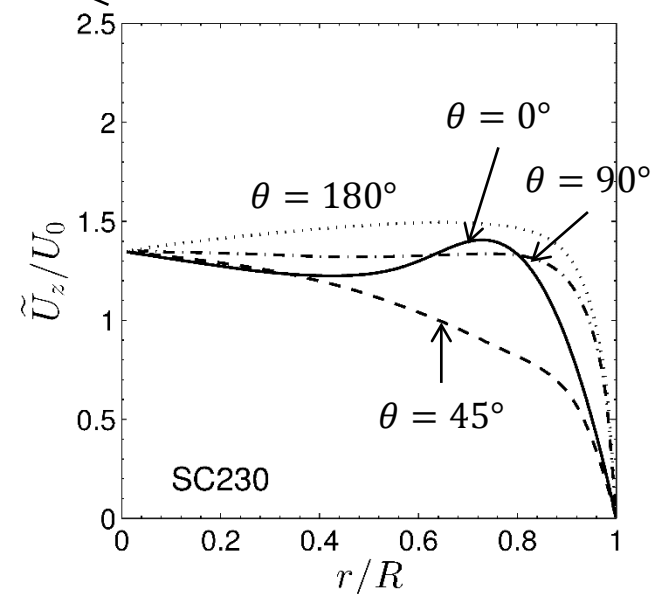
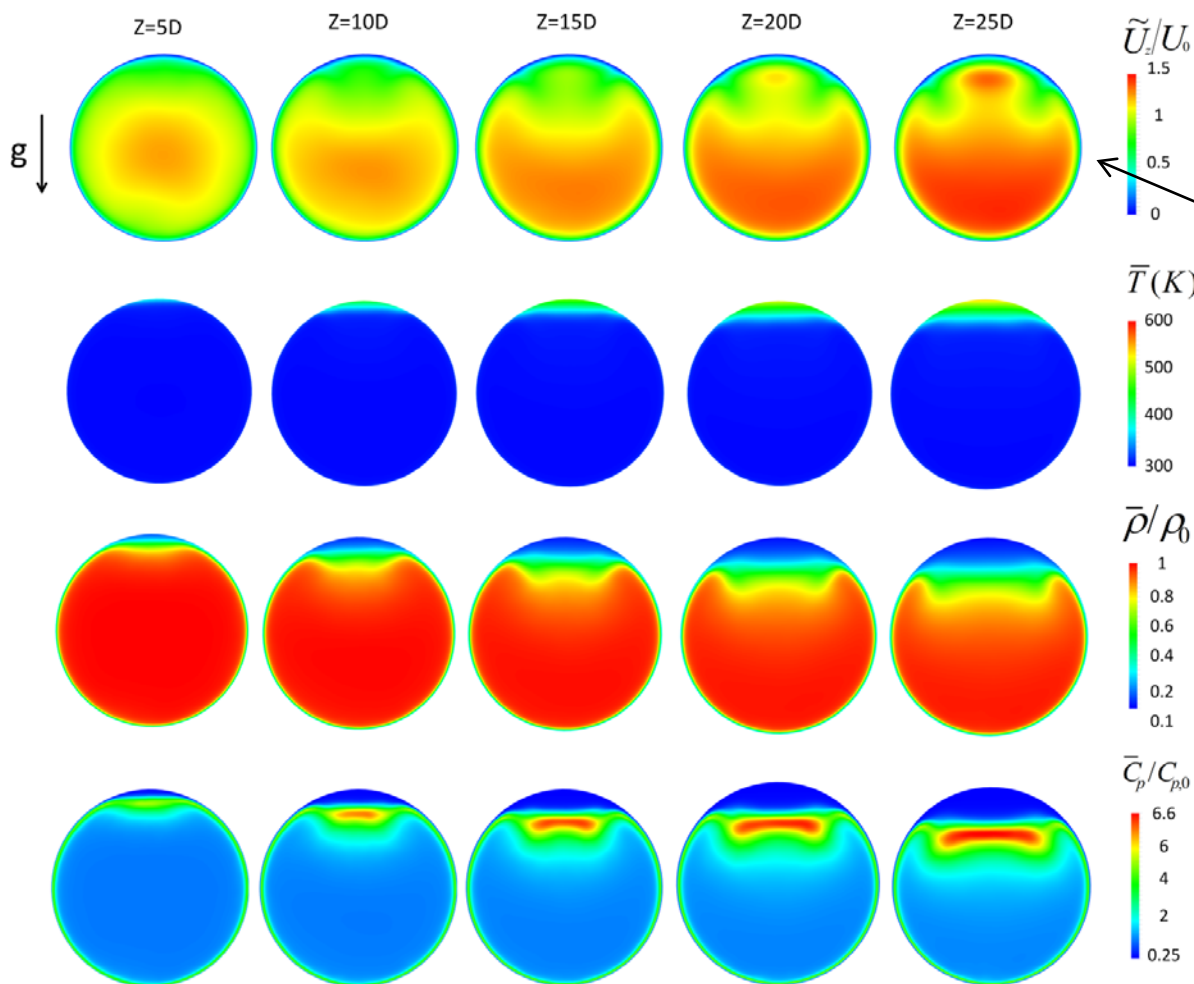


$D=2\text{mm}, q_w \approx 60 \text{ kW/m}^2$



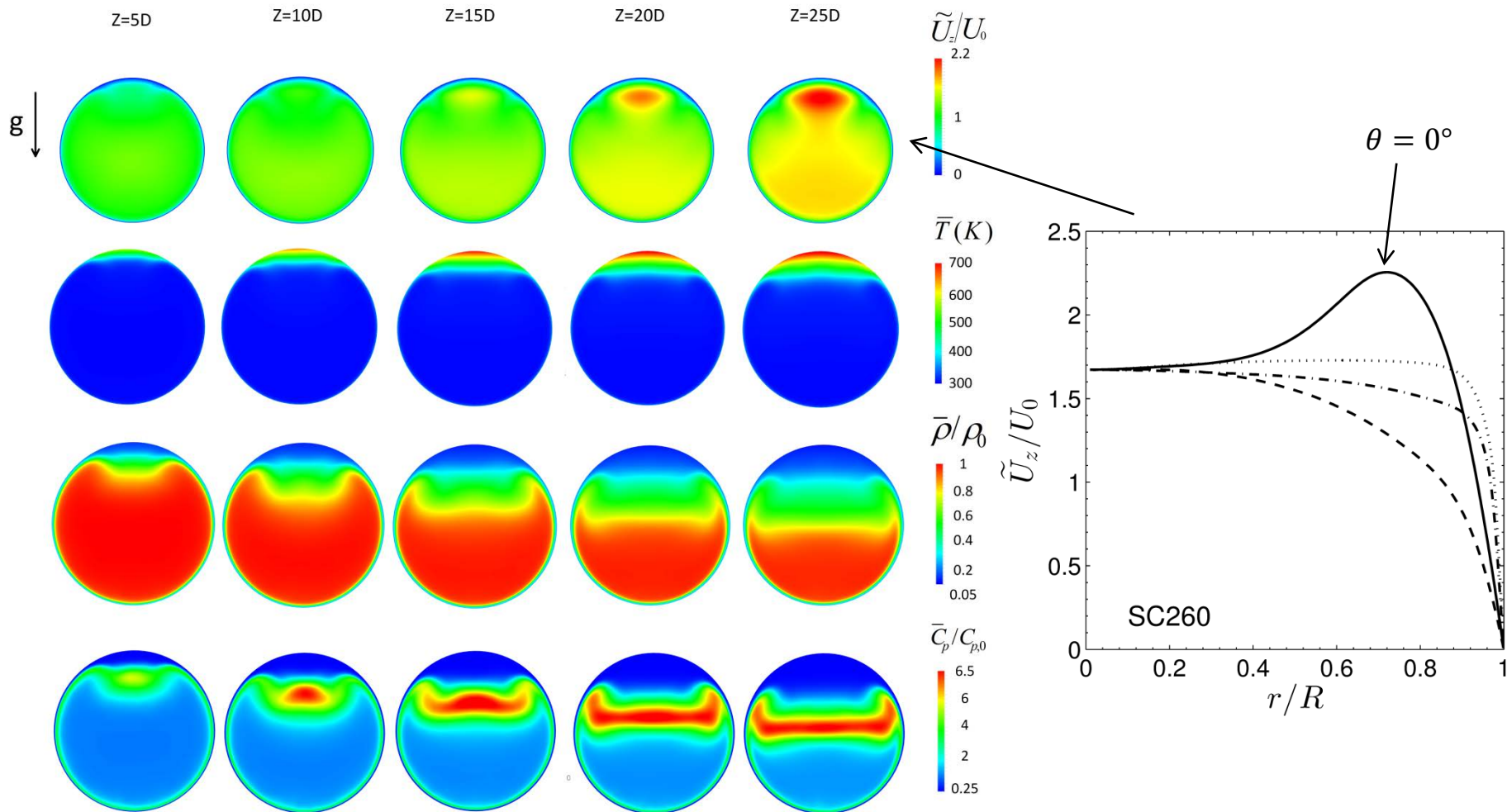
Results and discussion

Flow stratification, SC230, $q_w \approx 30 \text{ kW/m}^2$



Results and discussion

Flow stratification, SC260, $q_w \approx 60 \text{ kW/m}^2$



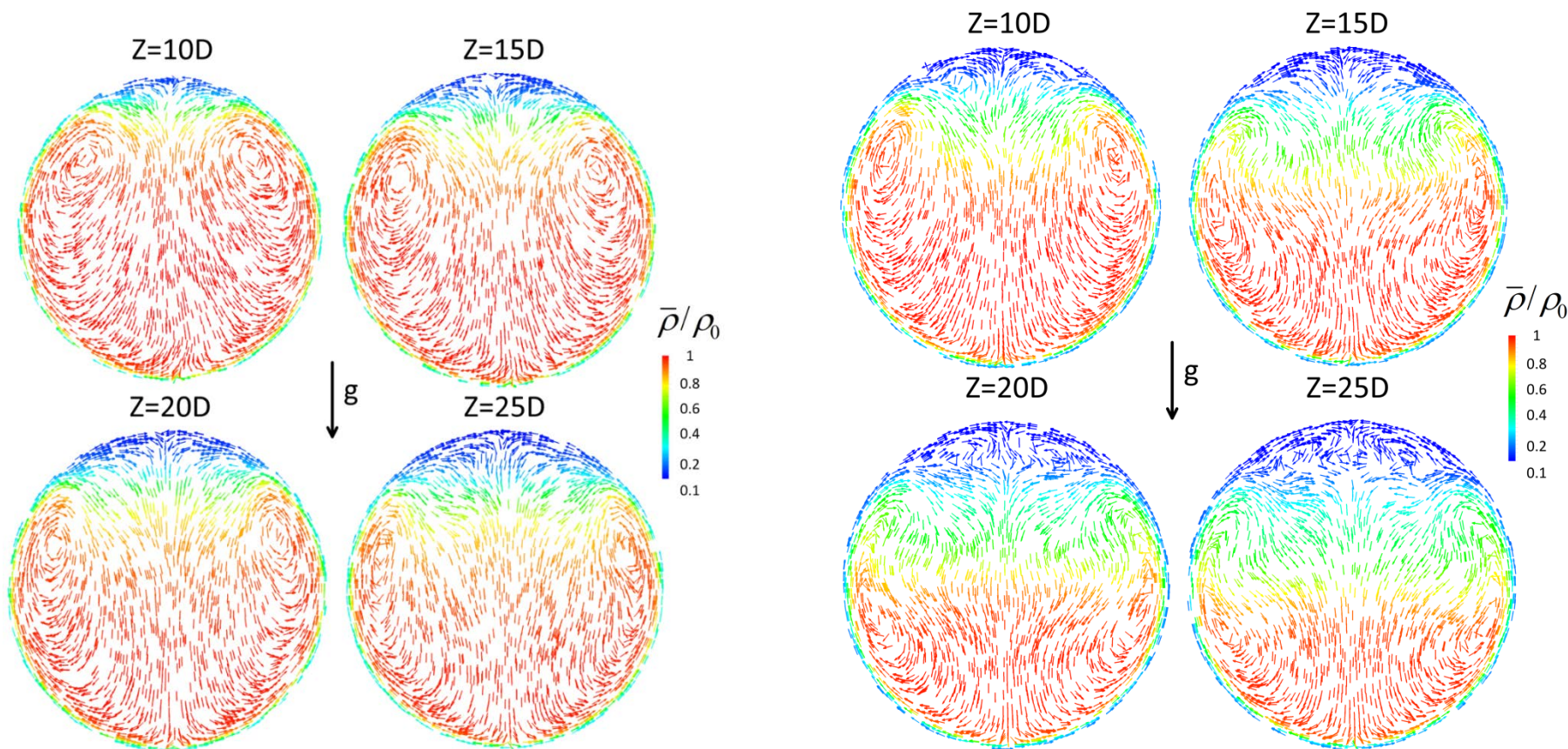
Results and discussion

Secondary flow

Vector plot of \bar{U}_r and \bar{U}_θ

SC230

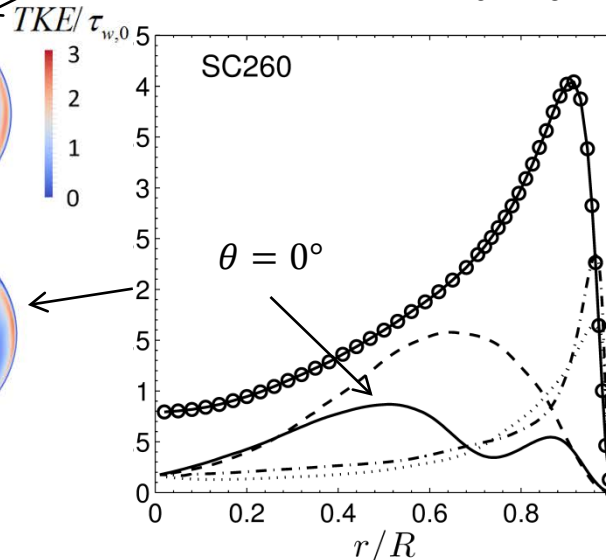
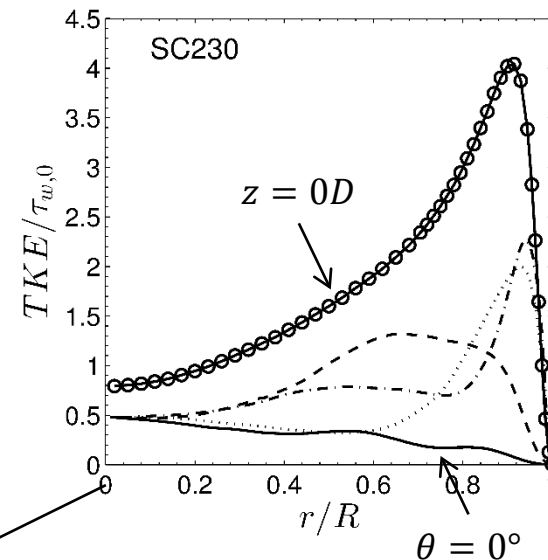
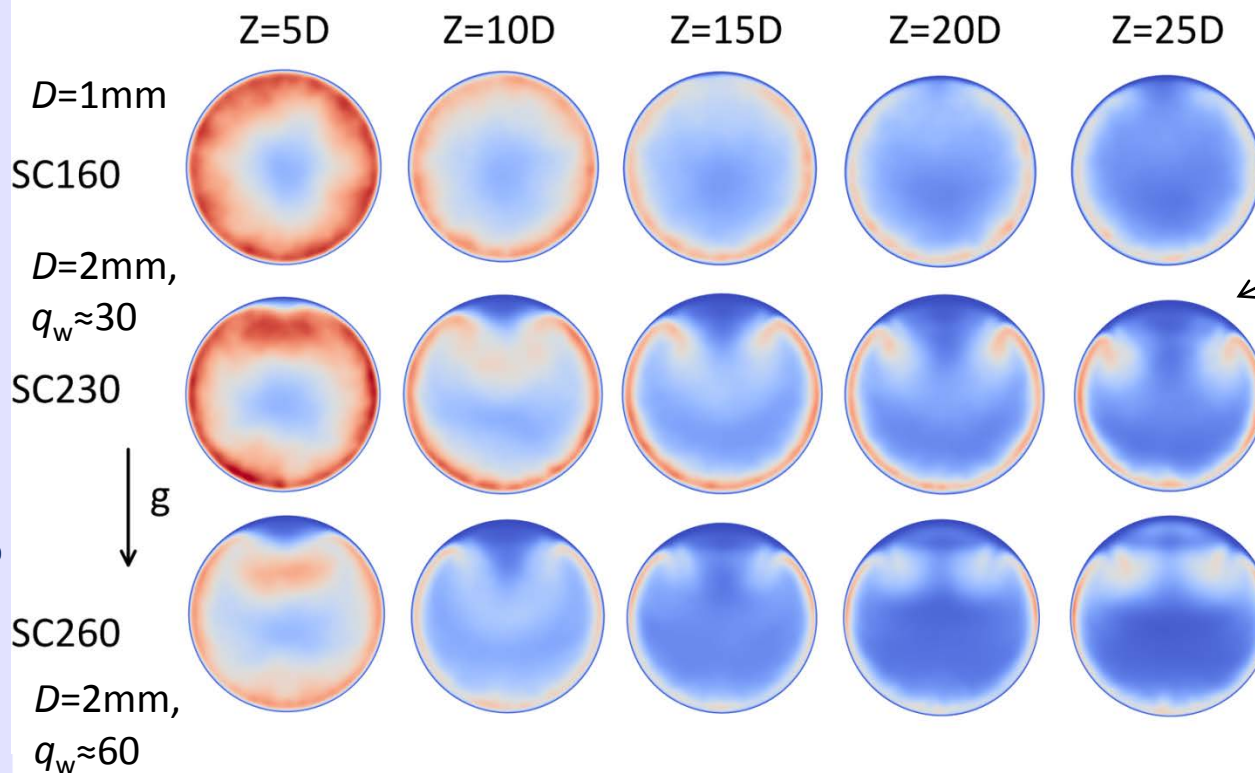
SC260



Results and discussion

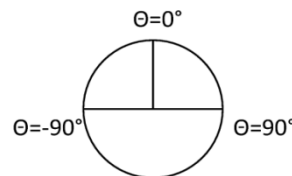
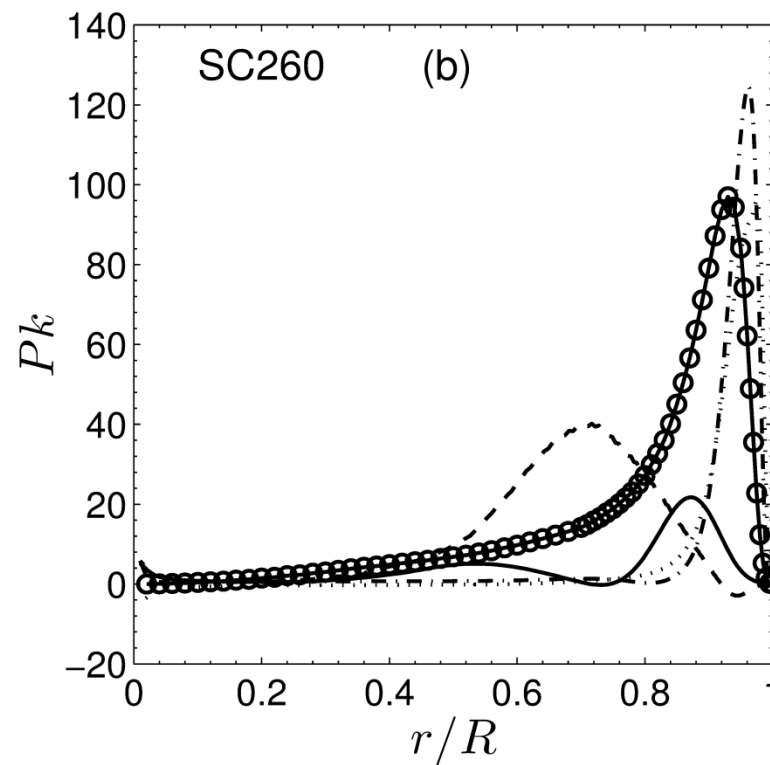
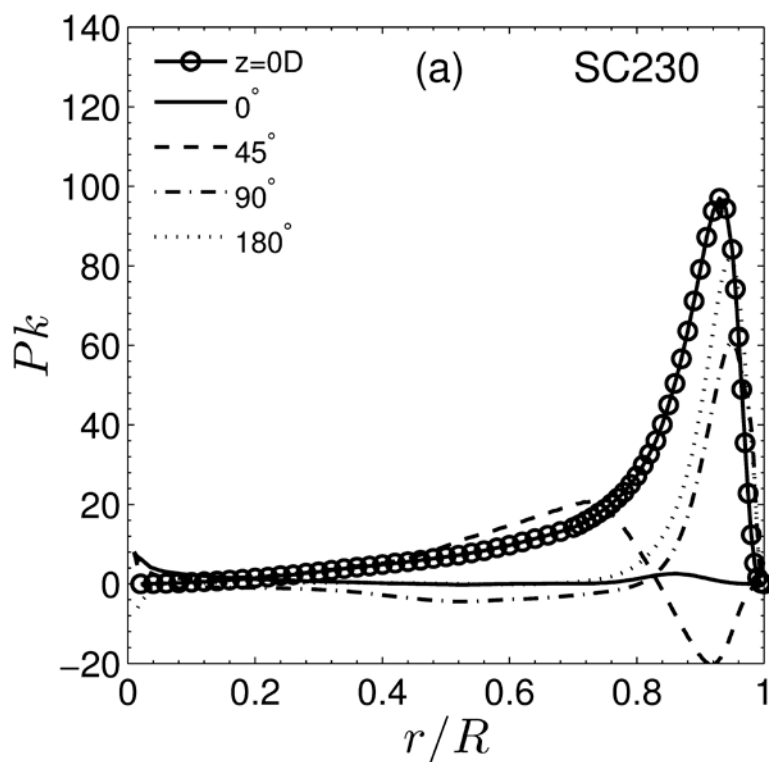
Turbulence statistics

$$TKE = \frac{1}{2} \overline{\rho U_i'' U_i''}$$



Results and discussion

Turbulence statistics



Conclusions

- Effect of buoyancy to the heat transfer of sCO₂ in a horizontal pipe using DNS
- Wall temperature T_w and skin friction coefficient strongly inhomogeneous in the circumferential direction
- Secondary flow is built up due to density difference and it transports the heated fluid to the top surface
- Modified mean velocity field and turbulence field

Thank you for your attention.

