



Experimental investigation of effect of buoyancy on supercritical carbon dioxide heat transfer in round tubes

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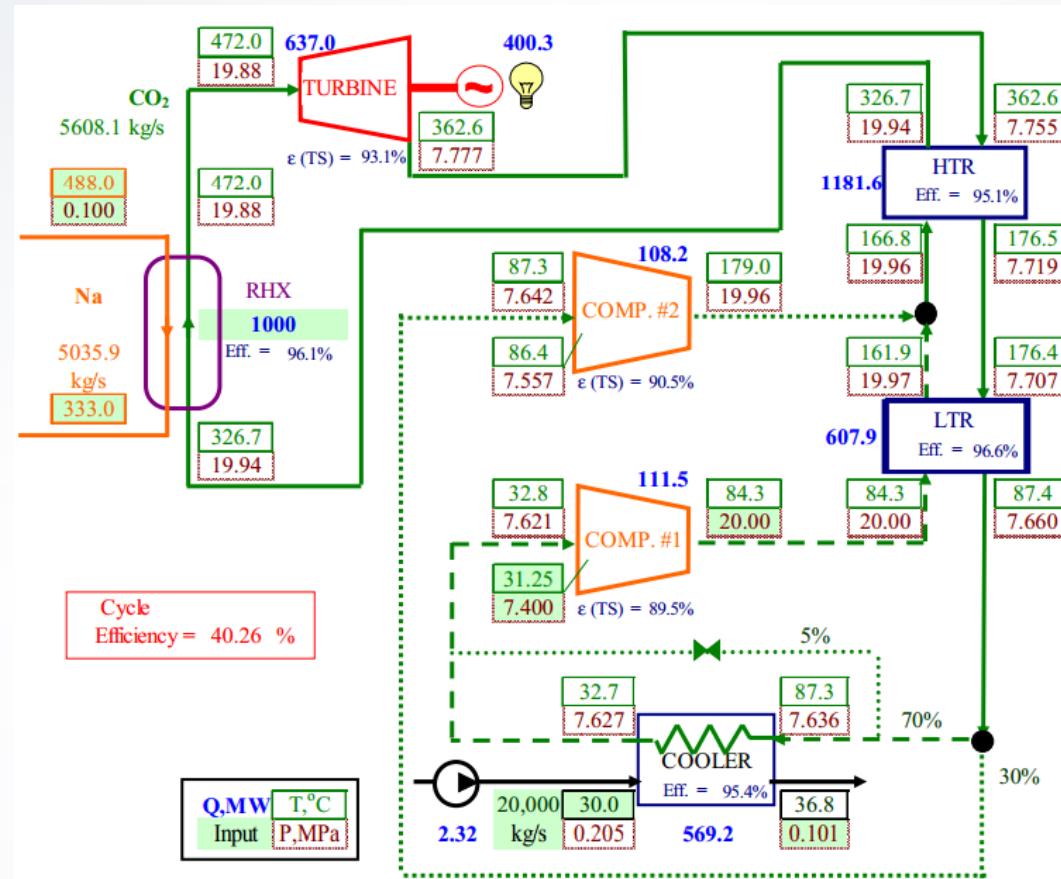


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Motivation for the study

- Heat exchangers in the cycle
 - High temperature recuperator (HTR)
 - Low temperature recuperator (LTR)
 - Cooler
- Expected operating conditions
 - 7.6 – 20 MPa
 - 20 – 50 KW/m²
 - 200 – 300 Kg/m²s
- For these conditions, there is a need for fundamental understanding of effects of buoyancy on heat transfer
 - Various channel sizes



From ANL Plant Dynamics Code [Moisseytsev *et al*]

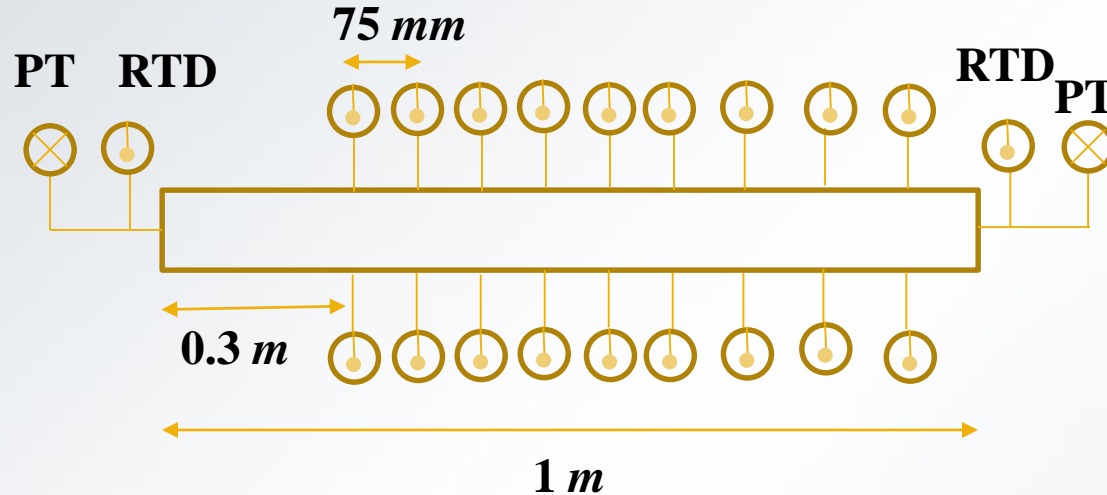
Experimental facility

- Heat transfer deterioration due to buoyancy effects and flow acceleration
- Key components of the test facility – A high pressure CO₂ supply pump, circulation pump, flow meter, pre-cooler, preheater, and DC power supply
- Test section orientation can be changed with minor tubing modifications

Component	Capabilities
HPLC pump	Up to $\sim 10,000$ <i>psi</i>
Circulation pump	0.6 – 7.0 <i>GPM</i>
Coriolis flow meter	0 – 0.27 <i>Kg/sec</i>
Pre-heater	Maximum 5.5 <i>KW</i>
Water chiller	Maximum 5.28 <i>KW</i>
Pre-cooler	Double tube HEX
DC power supply	0 – 5 <i>KW</i>
Buffer Tank	~ 0.5 <i>m</i> ³



Test section



- Direct current volumetric heating
 - 10 V, 500 A power supply
- $L = 1m$, $D_{in} \sim 10.9mm$, $D_{out} \sim 12.7mm$
- RTD probes are calibrated against boiling water and ice bath
- Wall temperatures are measured using 20 E type thermocouples
 - Calibrated against RTDs under no heat flux conditions

Data analysis procedure

- Data recorded for 500 s @ 1Hz

$$Q''_{PS} = \frac{V_{PS}I_{PS}}{\pi D_i L} \text{ [PS – power supply]}$$

$$T_{wi} = T_{wo} + \frac{\dot{q}}{4k_{ss}} \left[\left(\frac{D_{out}}{2} \right)^2 - \left(\frac{D_{in}}{2} \right)^2 \right] - \frac{\dot{q}}{2k_{ss}} \left(\frac{D_{out}}{2} \right)^2 \ln \left(\frac{D_{out}}{D_{in}} \right)$$

$$\dot{q} = \frac{V_{PS}I_{PS}}{\left[\frac{\pi}{4} (D_{out}^2 - D_{in}^2) L \right]}$$

Where, k_{ss} is the thermal conductivity of stainless steel 316

$$T_{b+1} = T_b + \frac{Q''_{PS}}{\dot{m}C_p} \pi D x$$

- Local heat transfer coefficients and Nusselt numbers are calculated as,

$$h = \frac{Q''_{PS}}{A(T_{wi} - T_b)}$$

$$Nu_b = \frac{hD}{k_b}$$

Results

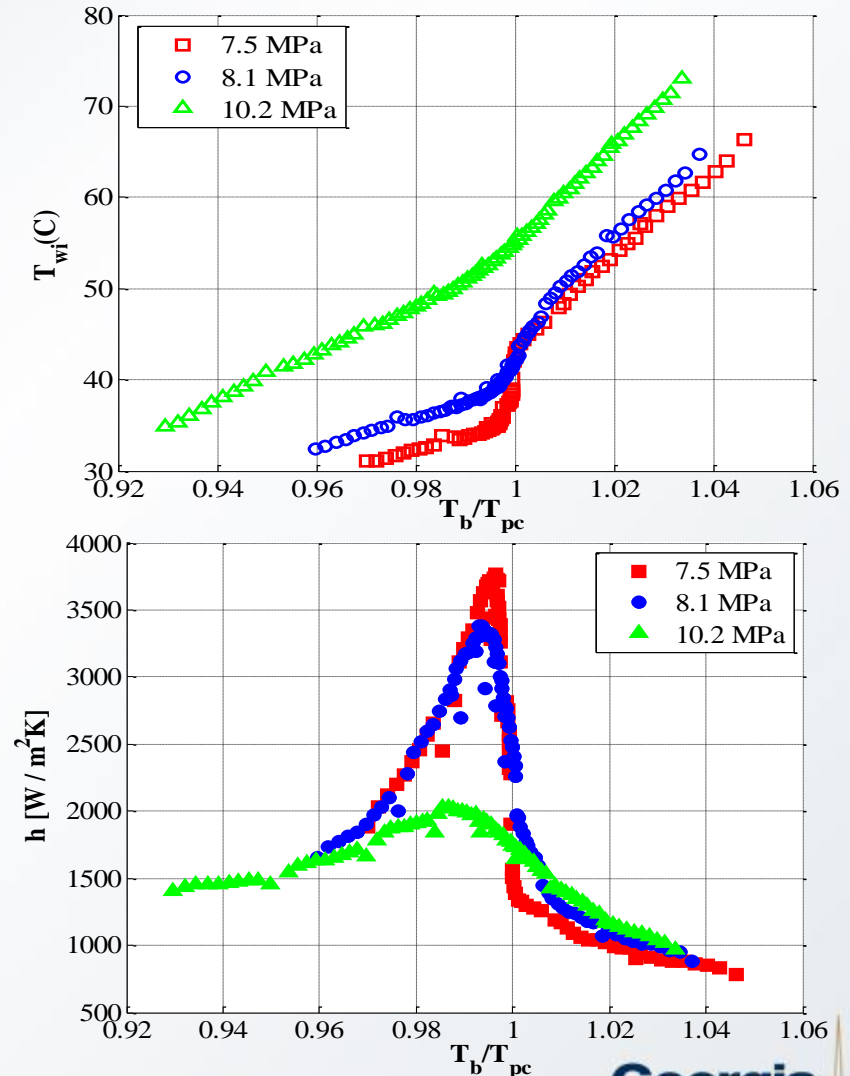
- Effect of
 - Operating pressure
 - Flow direction
 - Inlet temperature
 - Heat flux

Control Parameters	Range of Study
Inlet Temperature	20 – 55 ⁰ C
Operating pressure	7.5, 8.1, and 10.2 MPa
Mass flux	195, 320 Kg/m ² sec
Heat flux	0 - 65 KW/m ²
Flow direction	Horizontal, Upward, and Downward

- Buoyancy factor calculations

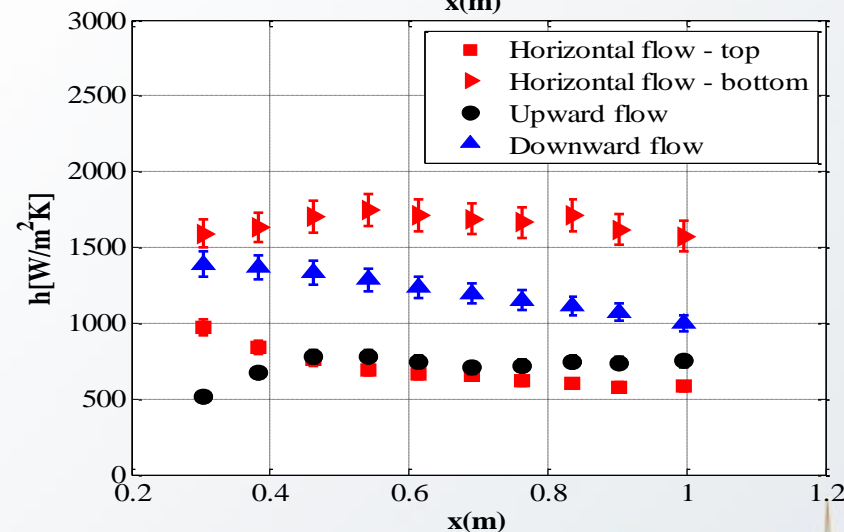
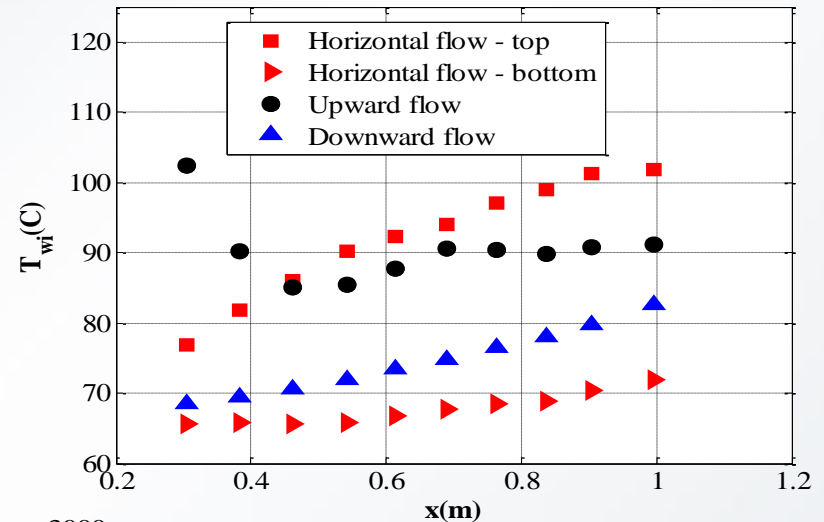
Effect of operating pressure

- Test conditions
 - Mass flux, 195 Kg/m²sec
 - Heat flux, 13.5 KW/m²
 - Downward flow
- Heat transfer enhancement close to the pseudo-critical point
- $T_b < T_{pc}$, lower operating pressure results in higher HTC's
- $T_b > T_{pc}$, higher operating pressure results in higher HTC's
- Attributed to variation of isobaric Prandtl number



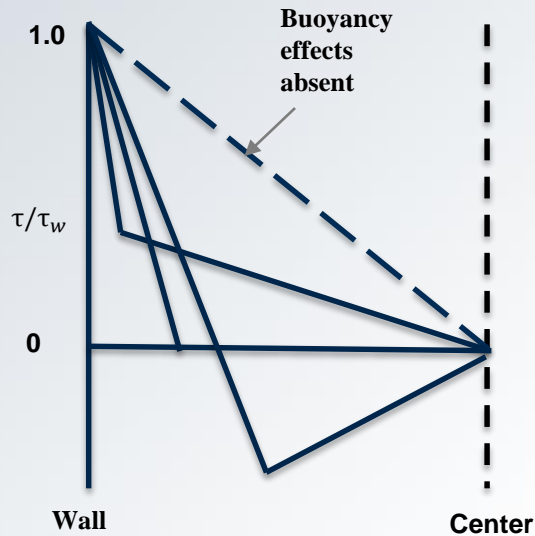
Effect of flow direction

- Test conditions
 - Mass flux, 195 Kg/m²sec
 - Heat flux, 24 KW/m²
 - Operating pressure, 10.2 MPa
 - Bulk inlet temperature, 46^o C
- Horizontal flow – Circumferential variation in wall temperature
- Upward flow – Localized spikes in wall temperature
- Downward flow – Wall temperatures are significantly lower than upward flow

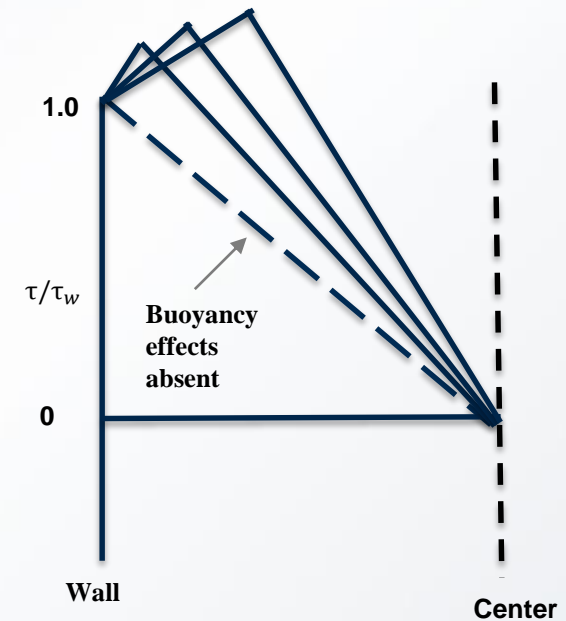


Effect of flow direction

Upward flow



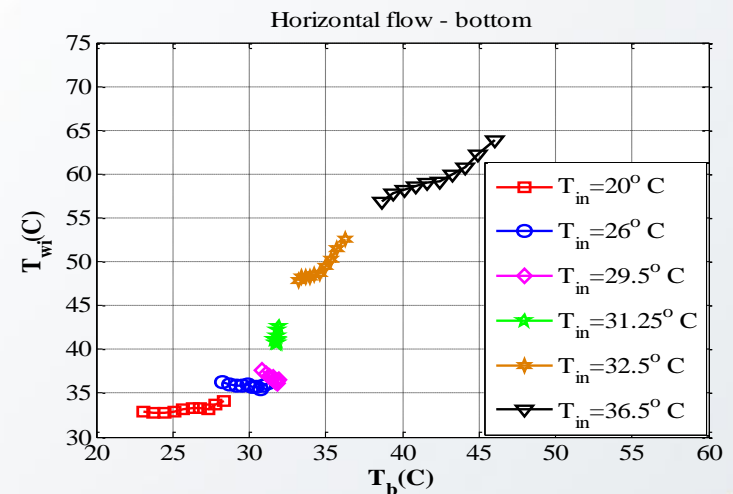
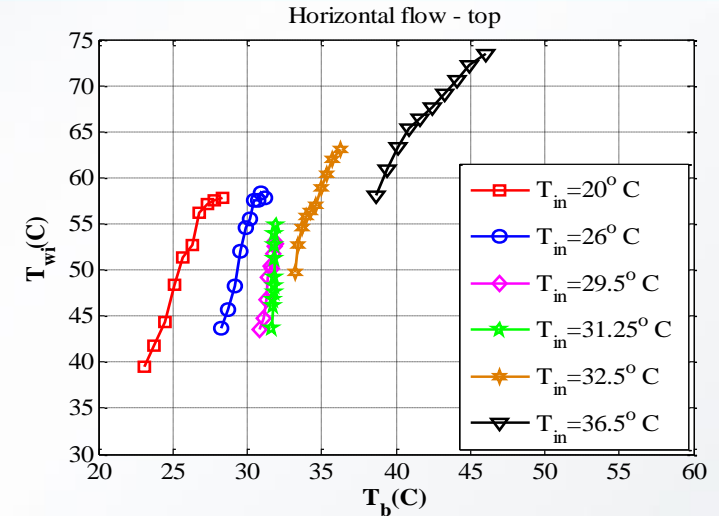
Downward flow



- Upward flow – Turbulent shear stress is reduced by buoyancy force
- Downward flow – Turbulent shear stress is enhanced by buoyancy force

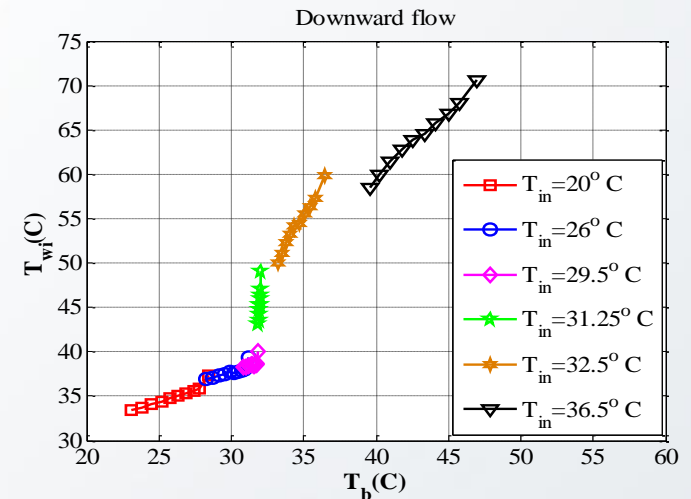
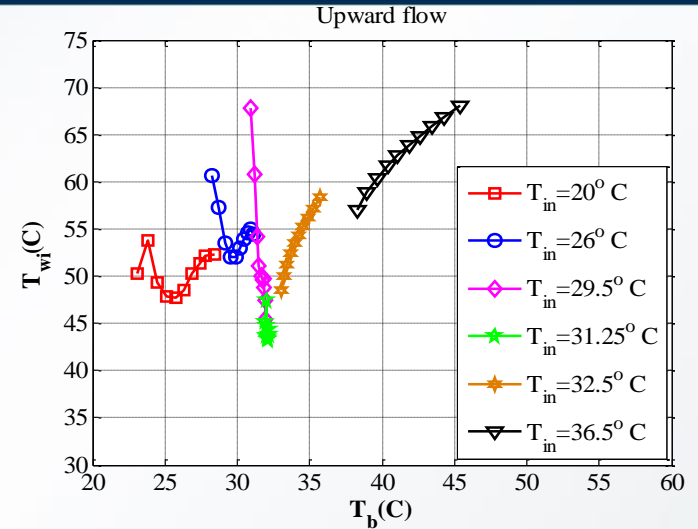
Effect of inlet temperature

- Test conditions
 - Mass flux, 320 Kg/m²sec
 - Heat flux, 24 KW/m²
 - Operating pressure, 7.5 MPa
 - Horizontal, upward and downward flow
- Horizontal flow – Severe discontinuity in the wall temperature as the inlet temperature is changed
- Thermal entrance length effects
- Temperature differences between top and bottom sides reduce for $T_b > T_{pc}$



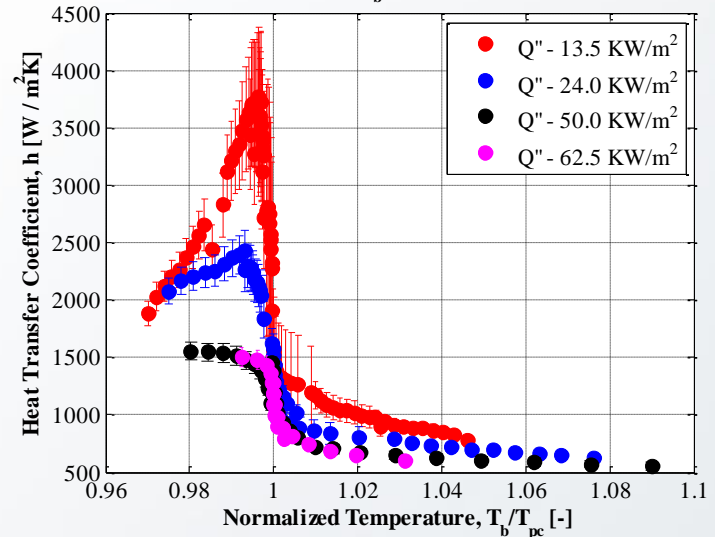
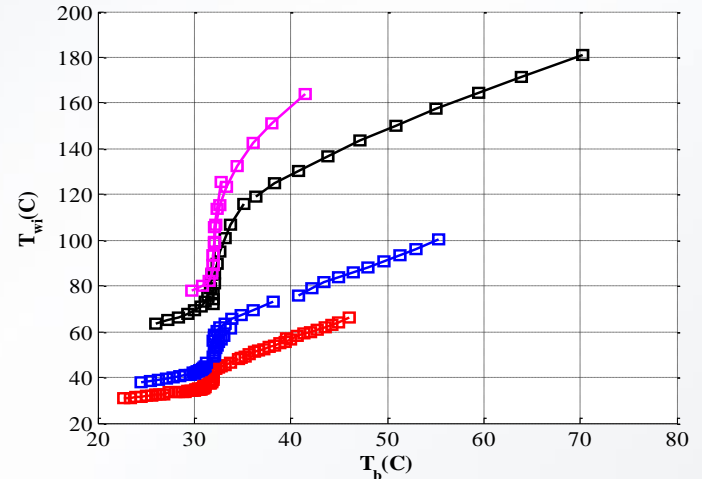
Effect of inlet temperature

- Upward flow – Location of spikes can be readily be changed by changing the inlet temperature
- Downward flow – Sharp increase in wall temperature for $T_{in} \sim T_{pc}$
- Pseudo-film boiling phenomenon similar to film boiling at subcritical pressures
- For $T_b > T_{pc}$, wall temperatures similar for both upward and downward flows



Effect of heat flux

- Test conditions
 - Mass flux, 195 Kg/m²sec
 - Operating pressure, 7.5 MPa
 - Downward flow
- Heat transfer enhancement reduces with heat flux
- Area integrated values of C_p reduces
- Pseudo-film boiling phenomenon is evident for all heat fluxes



Buoyancy criteria – Vertical flows

- Experimental Nusselt numbers normalized with Jackson correlation (developed for forced convection)

$$Nu_{jackson} = 0.0183 Re_b^{0.82} Pr_b^{0.5} \left(\frac{\rho_w}{\rho_b} \right)^{0.3} \left(\frac{C_{av}}{C_{pb}} \right)^n$$

Where, n is defined as

$$n = 0.4 \quad \text{for } T_b < T_w < T_{pc} \text{ and } 1.2T_{pc} < T_b < T_w$$

$$n = 0.4 + 0.2 \left(\frac{T_w}{T_{pc}} - 1 \right) \quad \text{for } T_b < T_w < T_{pc}$$

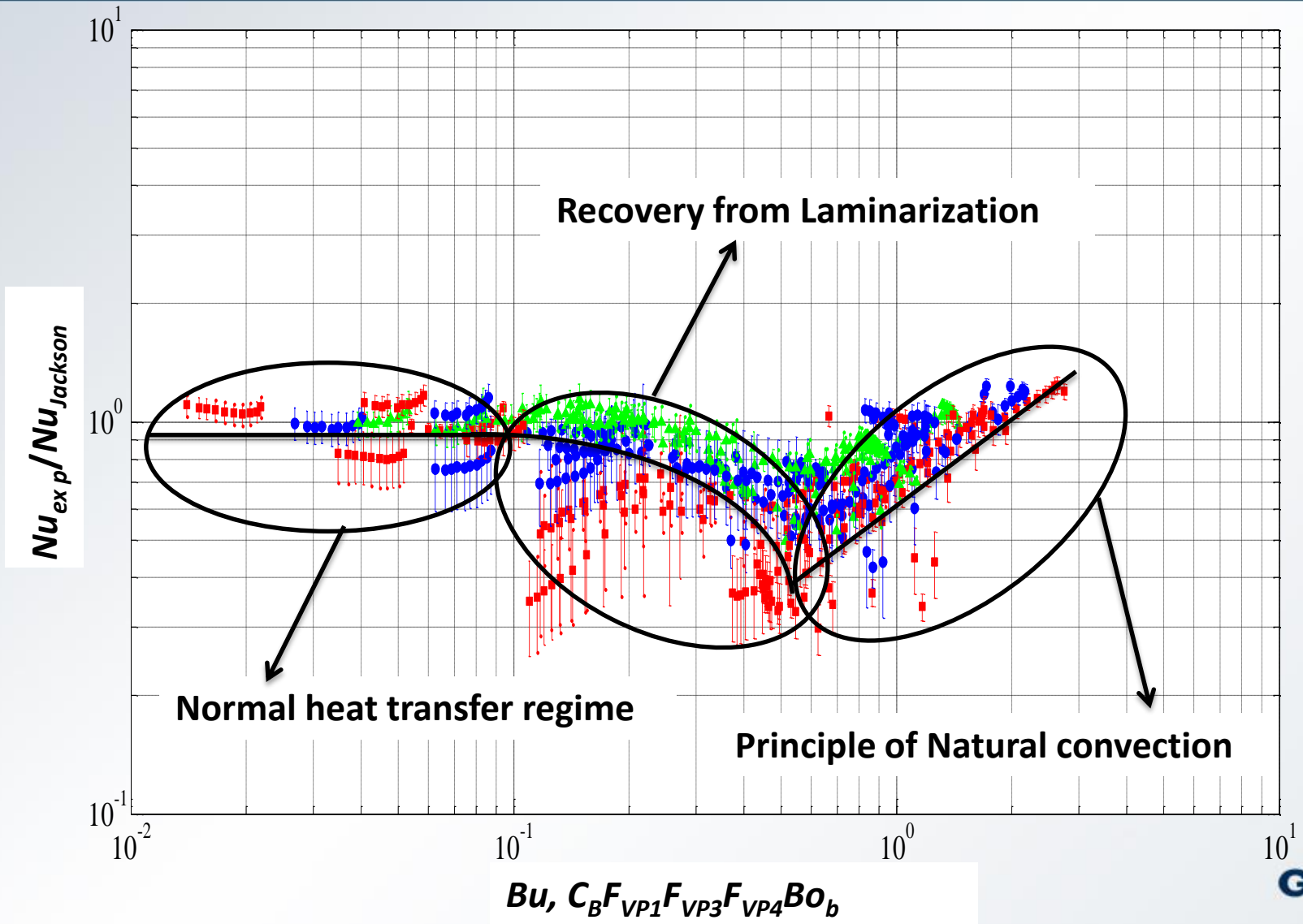
$$n = 0.4 + 0.2 \left(\frac{T_w}{T_{pc}} - 1 \right) \left(1 - 5 \left(\frac{T_b}{T_{pc}} - 1 \right) \right) \quad \text{for } T_{pc} < T_b < 1.2T_{pc}$$

- Jackson, 2013 buoyancy criteria

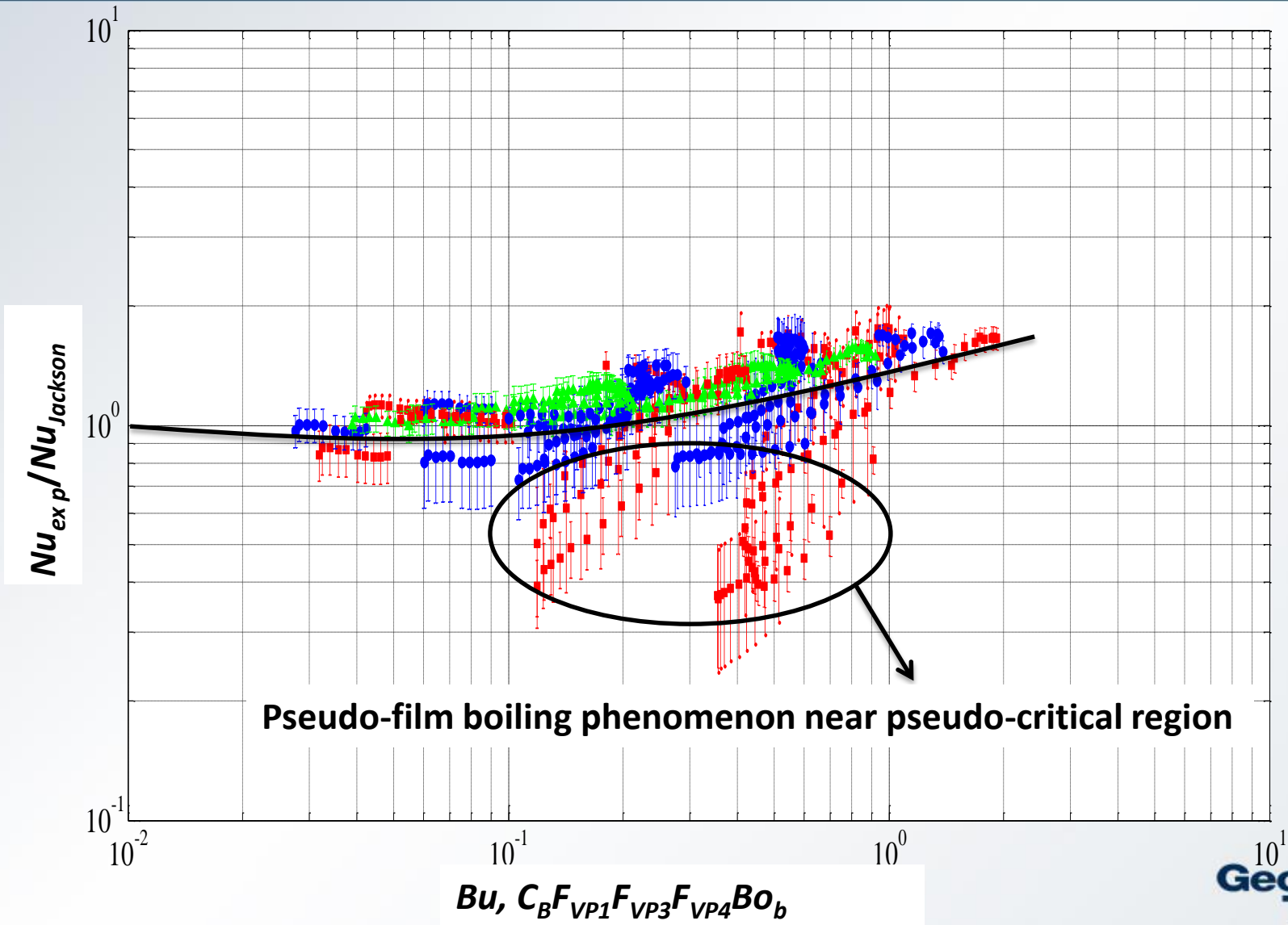
$$Bu = C_B Bo_b F_{VP1} F_{VP3} F_{VP4} < 0.04$$

$$C_B = 4600, \quad Bo_b = \frac{Gr_b}{Re_b^{2.625} Pr_b^{0.4}}, \quad F_{VP1} = \left(\frac{\mu_{av}}{\mu_b} \right) \left(\frac{\rho_{av}}{\rho_b} \right)^{-0.5}, \quad F_{VP3} = \left(\frac{Pr_{av}}{Pr_b} \right)^{-0.4}, \quad F_{VP4} = \frac{\rho_b - \rho_{av}}{\rho_b - \rho_w}$$

Buoyancy criteria – Upward flow



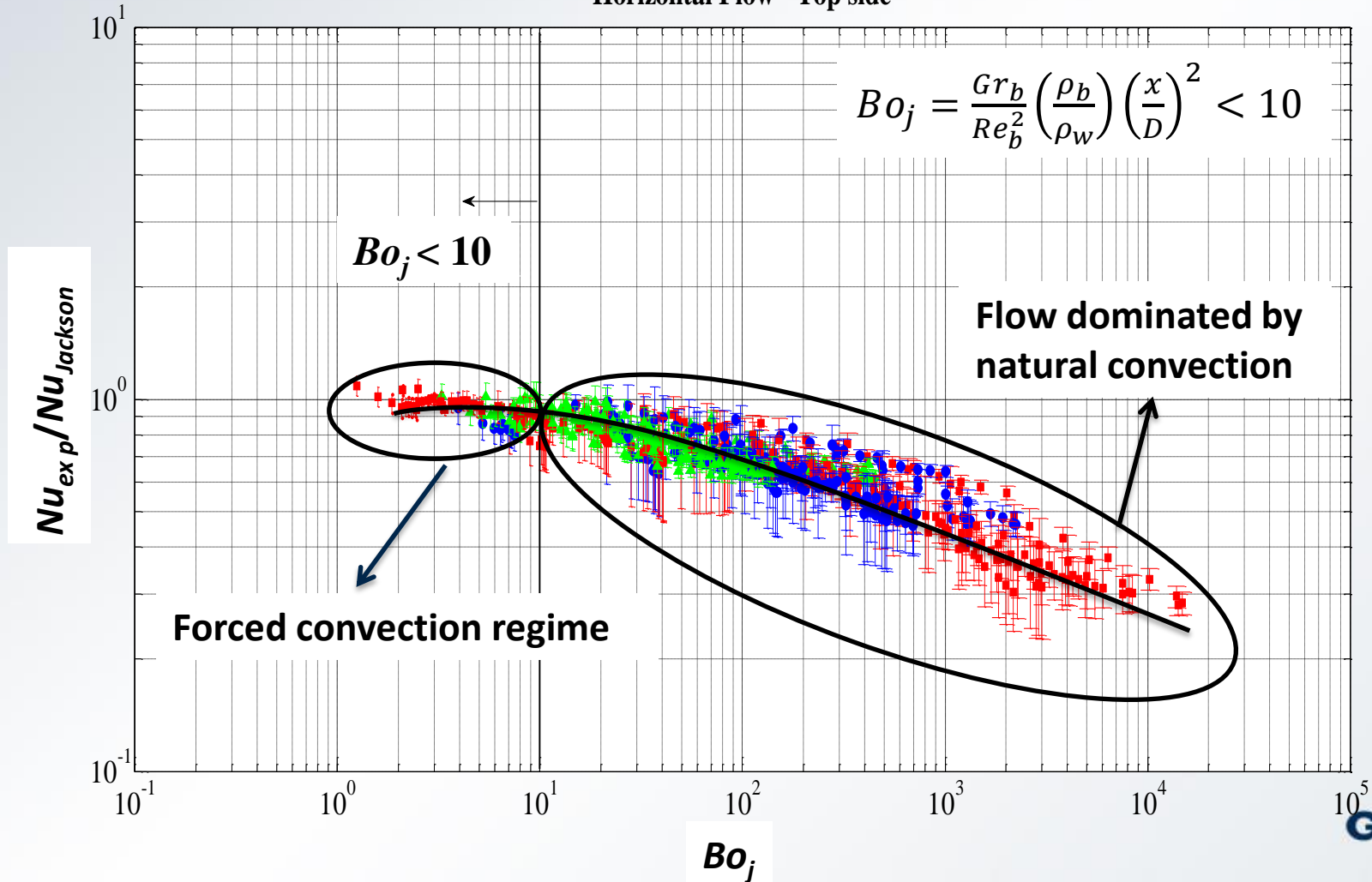
Buoyancy criteria – Downward flow



Buoyancy criteria – Horizontal flow

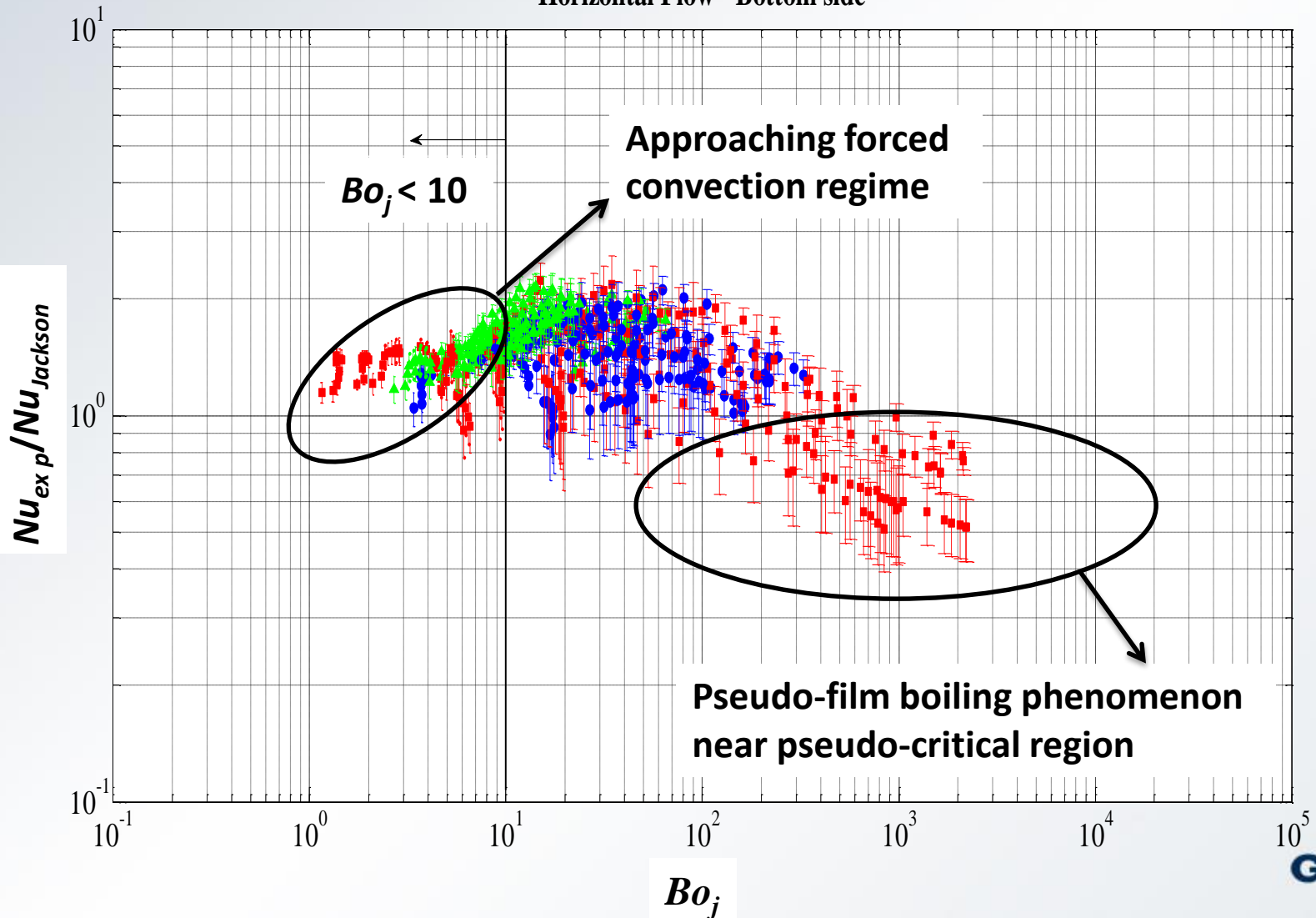
- Jackson, 1976 suggested a criteria to neglect buoyancy effects for horizontal flows

Horizontal Flow - Top side



Buoyancy criteria – Horizontal flow

Horizontal Flow - Bottom side



Summary

- Effect of buoyancy on heat transfer was investigated
- For $T_b < T_{pc}$, effect of buoyancy was significant resulting in
 - Circumferential variation of wall temperature for horizontal flow
 - Localized peaks in wall temperature for upward flow
 - Enhancement in heat transfer for downward flow
- For $T_b > T_{pc}$, effect of buoyancy was minimum leading to similar wall temperature profiles for all the flow orientations
- Buoyancy criteria suggested by Jackson can be used to predict the effect of buoyancy for both horizontal and vertical flows



Thank you for your time!

Questions?

